

Cambridge International A Level

MATHEMATICS
Paper 5 Probability & Statistics 1

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2020 series for most Cambridge IGCSE[™], Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

Cambridge International A Level – Mark Scheme

PUBLISHED

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

© UCLES 2020 Page 2 of 16

Ma	Mathematics Specific Marking Principles						
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.						
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.						
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.						
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).						
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.						
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.						

© UCLES 2020 Page 3 of 16

Cambridge International A Level – Mark Scheme

PUBLISHED

Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- **B** Mark for a correct result or statement independent of method marks.
- DM or DB When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
 - A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
 - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
 - The total number of marks available for each question is shown at the bottom of the Marks column.
 - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
 - Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

© UCLES 2020 Page 4 of 16

Cambridge International A Level – Mark Scheme

PUBLISHED

Abbreviations

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

CAO Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)

CWO Correct Working Only

ISW Ignore Subsequent Working

SOI Seen Or Implied

SC Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the

light of a particular circumstance)

WWW Without Wrong Working

AWRT Answer Which Rounds To

© UCLES 2020 Page 5 of 16

Question	Answer					er		Ma	arks	Guidance				
1(a)								R	ed				M1	Complete outcome space or or listing A and B outcomes
			1	2	3	4	5	6			or listing A∩B outcomes			
		1	2	3	4	5	6	7						
		2	3	4	5	6	7	8						
	le	3	4	5	6	7	8	9						
	Blue	4	5	6	7	8	9	10						
		5	6	7	8	9	10	11						
		6	7	8	9	10	11	12						
	P(A∩I	$(3) = \frac{3}{3}$	<u>5</u>							A1	With evidence			
										2				

© UCLES 2020 Page 6 of 16

Question	Answer	Marks	Guidance
1(b)	$P(A) \times P(B) = \frac{1}{3} \times \frac{10}{36}$	M1	Their $\frac{1}{3} \times their \frac{10}{36}$ seen
	$\frac{5}{54} \neq \frac{5}{36}$ so not independent	A1	$\frac{5}{54}, \frac{5}{36}$, P(A) × P(B) and P(A \cap B) seen in workings and correct conclusion stated Condone $\frac{5}{36}$ being stated in (a)
	Alternative method for question 1(b)		
	$P(B A) = P(B)$ $P(B A) = \frac{P(A \cap B)}{P(A)} = \frac{\frac{5}{36}}{\frac{1}{3}}$	M1	OE, $\frac{their1(a)}{theirP(A)}$ seen
	$\frac{5}{12} \neq \frac{5}{18}$ so not independent	A1	P(A B), P(B), $\frac{5}{12}$, $\frac{5}{18}$ seen in workings and correct conclusion stated Condone $\frac{5}{18} = \frac{10}{36}$ being identified in (a)
		2	

© UCLES 2020 Page 7 of 16

Question	Answer	Marks	Guidance
2(a)	$0.6 \times 0.7 + 0.4(1 - x) = 0.58$ = 0.42 + 0.4(1 - x) = 0.58	M1	Equation of form $0.6 \times a + 0.4 \times b = 0.58$; a = 0.3, 0.7, b = x, (1 - x)
		B1	Single correct product seen, condone 0·42, in an equation of appropriate form
	x = 0.6	A1	
	Alternative method for question 2(a)		
	$0.6 \times 0.3 + 0.4x = 0.42$ = 0.18 + 0.4x = 0.42	M1	Equation of form $0.6 \times a + 0.4 \times b = 0.42$; $a = 0.3, 0.7, b = x, (1 - x)$
		B1	Single correct product seen, condone 0·18, in an equation of appropriate form
	x = 0.6	A1	
		3	
2(b)	$(0.6 \times 0.3)^2$	M1	$(a \times b)^2$, $a = 0.6$, 0.4 and $b = 0.7$, 0.3 , x , $(1-x)$ or 0.18^2 , alone.
	0.0324	A1	
		2	
3(a)	$P(X > 6) = 0.75^6$	M1	$p^{n}, n = 6, 7 0$
	$0.178, \frac{729}{4096}$	A1	0·17797
		2	

© UCLES 2020 Page 8 of 16

Question	Answer						Marks					Guio	dance
3(b)	1 – P(0, 1	$\mathbb{C}_2 0.25^2 0.75^8)$	M1		nial ter $x \neq 0$,		orm ¹⁰	$C_x p^x$	$(1-p)^{10-x}, \ 0$				
	1 - (0.05	63135 + 0.1	1877117 +	0.2815670	5)		A1	Corre	ct unsi	mplifie	ed exp	ression	1
	0.474						A1	0.474	≤ <i>p</i> ≤	0.474	4		
							3						
4(a)	y	1	2	3	4		B1		1	2	3	4	
	prob	$\frac{7}{16}$	<u>5</u>	$\frac{3}{16}$	$\frac{1}{16}$	-		1	1	1	2	3	
		10	10	10	10			2	1	2	1	2	_
								3	2	1	3	1	-
								4	3	2	1	4	
									robabil				ith correct scores with at least re values if probability of zero
							B1	One p	robabi	lity (lii	nked v	vith co	rrect score) correct
							B1	2 mor	e prob	s (linke	ed witl	1 corre	ect scores) correct
							B1 FT	4 th pro	b corr	ect, FT	sum	of 3 or	4 terms = 1
							4						

© UCLES 2020 Page 9 of 16

Question	Answer	Marks	Guidance
4(b)	$P(2 \text{even}) = \frac{\frac{5}{16}}{\frac{6}{16}}$	M1	$\frac{\textit{their} P(2)}{\textit{their} P(2) + \textit{their} P(4)}$ seen or correct outcome space.
	$\frac{5}{6}$ or 0.833	A1	
		2	
5(a)	$P(X > 4.2) = P(z > \frac{4.2 - 3.5}{0.9})$ = P(z > 0.7778)	M1	Using \pm standardisation formula, no $\sqrt{\sigma}$ or σ^2 , continuity correction
	1 – 0.7818	M1	Appropriate area Φ , from standardisation formula $P(z>)$ in final solution
	0.218	A1	
		3	
5(b)	z = -1.282	B1	±1.282 seen (critical value)
	$\frac{t - 3.5}{0.9} = -1.282$	M1	An equation using ±standardisation formula with a z-value, condone $\sqrt{\sigma}$, σ^2 and continuity correction
	t = 2.35	A1	AWRT, only dependent on M mark
		3	

© UCLES 2020 Page 10 of 16

Question	Answer	Marks	Guidance					
5(c)	$P(2.8 < X < 4.2) = 1 - 2 \times their 5(a)$ $\equiv 2(1 - their 5(a)) - 1$ $\equiv 2(0.5 - their 5(a))$ $= 0.5636$	B1 FT	FT from <i>their</i> 5(a) < 0.5 or correct Accept unevaluated probability OE Accept 0.564					
	Number of days = $365 \times 0.5636 = 205.7$	M1	$365 \times their p$					
	So, 205 (days)	A1 FT	Accept 205 or 206, not 205·0 or 206·0 no approximation/rounding stated FT must be an integer value					
	Alternative method for question 5(c)							
	$P\left(\frac{2.8-3.5}{0.9} < z < \frac{4.2-3.5}{0.9}\right)$ $= \Phi(0.7778) - (1 - \Phi0.7778)$ $= 0.7818 - (1 - 0.7818)$ $= 0.5636$	В1	$0.5635 OE$					
	Number of days = $365 \times 0.5636 = 205.7$	M1	$365 \times their p$					
	So, 205 (days)	A1 FT	Accept 205 or 206, not 205·0 or 206·0 no approximation/rounding stated FT must be an integer value					
		3						

© UCLES 2020 Page 11 of 16

Question	Answer	Marks	Guidance
6(a)	350 340 350 300 300 300 300 300 300 30	M1	At least 4 points plotted at upper end points, with both scales linear with at least 3 values indicated
	Correct cumulative frequency curve	A1	All plotted correctly with curve drawn joined to (0, 0), axes labelled cumulative frequency, time, minutes
		2	
6(b)	$150 \times 0.76 = 114$	M1	114 SOI, may be on graph
	k = 45 (mins)	A1 FT	Clear indication that <i>their</i> graph has been used, tolerance ±1mm
		2	

© UCLES 2020 Page 12 of 16

Question	Answer	Marks	Guidance
6(c)	Frequencies: 12 36 58 28 16	B1	Correct frequencies seen
	Mean = $\frac{10 \times 12 + 25 \times 36 + 35 \times 58 + 50 \times 28 + 80 \times 16}{150}$	B1	At least 4 correct midpoints seen and used
	$\frac{120 + 900 + 2030 + 1400 + 1280}{150}$	M1	Correct formula with <i>their</i> midpoints (not upper boundary, lower boundary, class width or frequency density).
	$38.2, 38\frac{1}{5}$	A1	
	Variance = $\frac{12 \times 10^2 + 36 \times 25^2 + 58 \times 35^2 + 28 \times 50^2 + 16 \times 80^2}{150} - mean^2$ $= \frac{1200 + 22500 + 71050 + 70000 + 102400}{150} - mean^2$	M1	Substitute <i>their</i> midpoints and frequencies (condone use of cumulative frequency) in correct variance formula, must have '– <i>their</i> mean ² '
	(Standard deviation = $\sqrt{321.76}$) = 17.9	A1	
		6	
7(a)	<u>8!</u> <u>2!</u>	M1	$\frac{8!}{k} = \frac{7 \times 8}{k} \text{, where } k \in \mathbb{N}, \ \frac{a!}{2(!)}, \text{ where } a \in \mathbb{N}$
	20160	A1	
		2	

© UCLES 2020 Page 13 of 16

Question	Answer	Marks	Guidance					
7(b)	Total number of ways: $\frac{10!}{2!3!}$ (=302400) (A)	B1	Accept unsimplified					
	With Ps together: $\frac{9!}{3!}$ (= 60 480) (B)	B1	Accept unsimplified					
	With Ps not together: 302 400 – 60 480	M1	$\frac{10!}{m} - \frac{9!}{n}$, m, n integers or (A) – (B) if clearly identified					
	241 920	A1						
	Alternative method for question 7(b)							
	<u>8!</u>	B1	$k \times 8!$ in numerator, k a positive integer, no \pm					
	3!	B1	$m \times 3!$ in denominator, m a positive integer, no \pm					
	$\times \frac{9\times 8}{2}$	M1	Their $\frac{8!}{3!}$ multiplied by ${}^{9}C_{2}$ or ${}^{9}P_{2}$ no additional terms					
	241 920	A1	Exact value, WWW					
		4						

© UCLES 2020 Page 14 of 16

Question	Answer	Marks	Guidance						
7(c)	Probability = $\frac{\text{Number of ways Es at beginning and end}}{\text{Total number of ways}}$ Probability = $\frac{\frac{8!}{2!}}{\frac{10!}{2 \times 3!}} = \frac{20160}{302400}$	M1	$\frac{\left(\frac{8!}{k!}\right)}{\frac{10!}{k!l!}} \ 1 \leqslant k, l \in \mathbb{N} \leqslant 3, \text{ FT denominator from 7(b) or correct}$						
	$\frac{1}{15}$, 0.0667	A1							
	Alternative method for question 7(c)								
	Probability = $\frac{3}{10} \times \frac{2}{9}$	M1	$\frac{a}{10} \times \frac{a-1}{9} a = 3,2$						
	$\frac{1}{15}$, 0.0667	A1							
	Alternative method for question 7(c)								
	Probability = $\frac{1}{10} \times \frac{1}{9} \times 3!$	M1	$\frac{1}{10} \times \frac{1}{9} \times m!, m = 3, 2$						
	$\frac{1}{15}$, 0.0667	A1							
		2							

© UCLES 2020 Page 15 of 16

Question	Answer	Marks	Guidance
7(d)	Scenarios: $P \to E \to C_0 = 1$	M1	${}^{5}C_{x}$ seen alone, $1 \le x \le 4$
	PEEE $C_0 = 1$ PEEE $S_0 = 1$	M1	Summing the number of ways for 3 or 4 correct scenarios (can be unsimplified), no incorrect scenarios
	Total = 26	A1	
		3	

© UCLES 2020 Page 16 of 16