Cambridge International AS & A Level

Cambridge Assessment International Education
Cambridge International Advanced Subsidiary and Advanced Level

MATHEMATICS **9709/61**

Paper 6 **May/June 2019**

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2019 series for most Cambridge IGCSE™, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

PUBLISHED

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5: Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).
GENERIC MARKING PRINCIPLE 6: Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

  - Note: B2 or A2 means that the candidate can earn 2 or 0.
    B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only – often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

SOI Seen or implied

SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

Question	Answer	Marks	Guidance
1(i)	$\Sigma(t-120) = -25+6-3+15+0+5-6-1+16 = 7$	**M1**	Attempt to sum both $(t-120)$ and $(t-120)^2$ Correct ans using $\Sigma t - 9\times 120$ and $\Sigma (t-120)^2$ M1A1
	$\Sigma(t-120)^2 = 25^2+6^2+3^2+15^2+0^2+5^2+6^2+1^2+16^2$ $= 1213$	**A1**	Both correct, www, **SC** correct ans no working **B1B1**
		2	
1(ii)	$\text{Var} = \frac{\Sigma(t-120)^2}{9} - \left(\frac{\Sigma(t-120)}{9}\right)^2 = \frac{their\,1213}{9} - \left(\frac{their\,7}{9}\right)^2$	**M1**	Using two coded values in correct formula including finding Σt from 7 etc
	$= 134(.2)$	**A1**	Correct answer **SC** if correct variance obtained by another method from raw data give **SCB1**
		2	

Question	Answer	Marks	Guidance
2	Jameel: P(plum) $= \frac{5}{8}$, Rosa: P(plum) $= \frac{x}{x+6}$ $\frac{5}{8}\times\frac{x}{x+6} = \frac{1}{4}$	**M1**	*Their* 2 probabilities for P(plum) multiplied and equated to 1/4
		A1	Correct equation oe
	$(x =)\ 4$	**A1**	**SC** correct answer with no appropriate equations i.e. common sense **B1**
		3	

Question	Answer	Marks	Guidance
3	P(X) = $\frac{3}{36}$ $\left(\frac{1}{12} oe\right)$	**B1**	
	P(Y) = $\frac{12}{36}$ $\left(\frac{1}{3} oe\right)$	**B1**	
	P(X∩Y) = $\frac{1}{36}$	**M1**	Independent method to find P($X \cap Y$) without multiplication, either stated or by listing or circling numbers on a probability space diagram. OR condititional prob with a single fraction numerator
	P(X) × P(Y) = P(X∩Y), independent	**A1**	Numerical comparison and conclusion, www
		4	

Question	Answer	Marks	Guidance
4	Median Maths = 40	**M1**	Indication of finding medians, such as mark on graph or reference marks to 700 pupils, condone poor terminology such as 'mean'
	Median English = 55	**A1**	Both values correct, condone 54<English<56 but 54, 56 get A0
	Median of English is larger than median of Maths	**B1**	Correct statement, median must be referenced within answer. No credit if statement references 'means'
	Range Maths is 100 or IQ range Maths = 80 – 12 = 68	**M1**	Evidence of finding either both ranges or both IQ ranges i.e. see a minus
	Range English is 60 or IQ range English = 62 – 42 = 20	**A1**	Both ranges or IQR correct
	Maths marks have more spread then English marks	**B1**	Correct conclusion. Accept standard deviation but must see some figures
		6	

Question	Answer	Marks	Guidance
5(i)	(P > 12) = P(13, 14, 15)	**M1**	Binomial term of form ${}^{15}C_x p^x(1-p)^{15-x}$ $0 < p < 1$ any p, $x \neq 15,0$
	$= {}^{15}C_{13}(0.65)^{13}(0.35)^2 + {}^{15}C_{14}(0.65)^{14}(0.35)^1 + (0.65)^{15}$	**A1**	Correct unsimplified answer
	= 0.0617	**A1**	SC if use np and npq with justification give (12.5 – 9.75)/√3.41 M1 1–F(1.489) A1 0.0681 A0
		3	
5(ii)	mean = 250 × 0.65 = 162.5 variance = 250 × 0.65 × 0.35 = 56.875	**B1**	Correct unsimplified *np* and *npq*
	$P(< 179) = P(z < \frac{178.5-162.5}{\sqrt{56.875}}) = P(z < 2.122)$	**M1**	Substituting *their* μ and σ (condone σ^2) into the Standardisation Formula with a numerical value for *'178.5'*. Continuity correct not required for this M1. Condone ± standardisation formula
	Using continuity correction 178.5 or 179.5	**M1**	
	= 0.983	**A1**	Correct final answer
		4	

Question	Answer	Marks	Guidance
6(i)	P(loses \$1) = P(F and F) = 0.8 × 0.8	**M1**	0.8 x 0.8 or (1 – 0.2)(1-0.2) or P(F) × P(F) or P(F)+P(F) seen or implied
	= 0.64 AG	**A1**	Must see probabilities multiplied together with final answer and a clear probability statement or implied by labelled tree diagram
		2	

Question	Answer	Marks	Guidance
6(ii)	<table><tr><td>Amount gained ($)</td><td>–1</td><td>0.50</td><td>2</td></tr><tr><td>Prob</td><td></td><td>0.16</td><td>0.2</td></tr></table>	**B1**	–1 linked with 0.64 in table
		B1	0.5 seen in table
		B1	0.16 seen in table linked to their 0.5
		B1	**FT** P(2.00 gained) = 0.36 – P(0.50 gained) or correct, and all amount gained linked correctly in table
		4	
6(iii)	E(winnings) = $–1 \times 0.64 + 0.5 \times 0.16 + 2 \times 0.2$ = –($)0.16, –16 cents	**B1**	**FT** Accept ($)0.16 or 16 cents **loss.** FT unsimplified E(winnings) from their table provided $\Sigma p = 1$
		1	

Question	Answer	Marks	Guidance
7(i)	$P(< 700) = P\left(z < \frac{700 - 830}{120}\right) = P(z < -1.083)$	**M1**	Using ± standardisation formula, no continuity correction, not σ^2 or $\sqrt{\sigma}$
	= 1 – 0.8606	**M1**	Appropriate area Φ from standardisation formula P(z<….) in final probability solution, (<0.5 if z is –ve, >0.5 if z is +ve)
	= 0.1394	**A1**	Correct final probability rounding to 0.139
	Expected number of female adults = 430 × *their* 0.1394 = 59.9 So 59 or 60	**B1**	**FT** *their* 3 or 4 SF probability, rounded or truncated to integer
		4	

Question	Answer	Marks	Guidance
7(ii)	P(giraffe < 830+w) = 95% so z = 1.645	**B1**	±1.645 seen (critical value)
	$\frac{(830+w)-830}{120} = \frac{w}{120} = 1.645$	**M1**	An equation using the standardisation formula with a z-value (not $1-z$), condone σ^2 or $\sqrt{\sigma}$ not 0.8519, 0.8289
	w = 197	**A1**	Correct answer
		3	
7(iii)	P(male > 950) = 0.834, so z = –0.97	**B1**	± 0.97 seen
	$\frac{950-1190}{\sigma} = -0.97$	**M1**	Using ± standardisation formula, condone continuity correction, σ^2 or $\sqrt{\sigma}$, condone equating with non z-value not 0.834, 0.166
	σ = 247	**A1**	Condone $-\sigma = -247$. www.
		3	

Question	Answer	Marks	Guidance
8(i)	$({}^9C_4 =)$ 126	**B1**	
		1	
8(ii)	${}^7C_2$	**B1**	${}^7C_x$ or ${}^yC_2$ (implied by correct answer) or ${}^7P_x$ or ${}^7P_y$, seen alone
	= 21	**B1**	correct answer
		2	

Question	Answer	Marks	Guidance
8(iii)	_ C_1 (B_1 B_2 B_3) C_2 _ C_3 _ C_4 _ C_5 _ C_6	**B1**	3! or 6! seen alone or multiplied by k > 1 need not be an integer
	3! × 6! × 7	**B1**	3! and 6! seen multiplied by k > 1, integer, no division
	= 30240	**B1**	Exact value
	Alternative method for question 8(iii)		
	C_1 (B_1 B_2 B_3) C_2 C_3 C_4 C_5 C_6	**B1**	3! or 7! seen alone or multiplied by k > 1 need not be an integer
	3! × 7!	**B1**	3! and 7! seen multiplied by k > or = 1, no division
	= 30240	**B1**	Exact value
		3	
8(iv)	C_1 _ C_2 _ C_3 _ C_4 _ C_5 _C_6	**B1**	6! or 4! X 6P2 seen alone or multiplied by k > 1, no division (arrangements of cars)
	6! × 5P3 *or* 6! × 5 × 4 × 3 or 6! x 3! x10	**B1**	Multiply by 5P3 oe i.e. putting Bs in between 4 of the Cs OR multiply by 3! x n where n = 7, 8, 9, 10 (number of options)
	= 43200	**B1**	Correct answer
		3	