

## **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
MATHEMATICS			0580/43
Paper 4 (Extended)			May/June 2018
			2 hours 30 minutes
Candidates answer o	n the Question Paper.		
Additional Materials:	Electronic calculator Tracing paper (optional).	Geometrical instruments	5

## **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total of the marks for this paper is 130.



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(a)	Rov	wena buys and sells clothes.	
	(i)	She buys a jacket for \$40 and sells it for \$45.40.	
		Calculate the percentage profit.	
			. % [3]
	(ii)	She sells a dress for \$42.60 after making a profit of 20% on the cost price.	
		Calculate the cost price.	
	_	\$	[3]
<b>(b)</b>		ra invests \$500 for 15 years at a rate of 2% per year simple interest.	
	Calo	lculate the total interest Sara receives.	
		\$	[2]

	$(\mathbf{c})$	Tomas	haa	++++0	0040
- (	( -	i romas	11/48	IWO	Cars

(i)	The value, today, of one car is \$21 000.
	The value of this car <b>decreases</b> exponentially by 18% each year

Calculate the value of this car after 5 years. Give your answer correct to the nearest hundred dollars.

\$		3	
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(ii) The value, today, of the other car is \$15000. The value of this car **increases** exponentially by x% each year. After 12 years the value of the car will be \$42190.

Calculate the value of *x*.

$$x =$$
 [3]

2 (a) (i)  $y = 2^x$ 

Complete the table.

х	0	1	2	3	4
у		2	4	8	

[2]

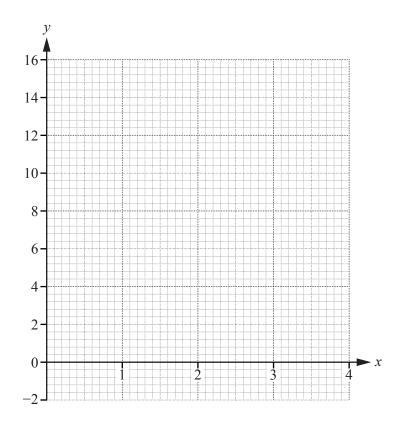
(ii)  $y = 14 - x^2$ 

Complete the table.

х	0	1	2	3	4
y		13	10	5	

[2]

**(b)** On the grid, draw the graphs of  $y = 2^x$  and  $y = 14 - x^2$  for  $0 \le x \le 4$ .



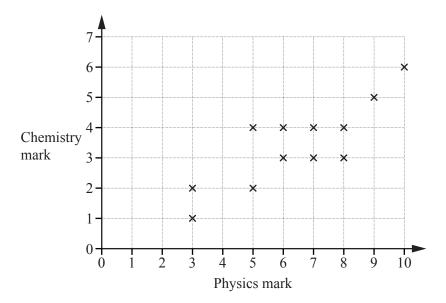
[6]

(c)	Use	your graphs to solve the equations.
	(i)	$2^x = 12$
		x =  [1]
	(ii)	$2^x = 14 - x^2$
		x =  [1]
(d)	(i)	On the grid, draw the line from the point $(4, 2)$ that has a gradient of $-4$ .
	(ii)	Complete the statement.
		This straight line is a to the graph of $y = 14 - x^2$

[2]

at the point ( ......... , ........).

3 (a) The scatter diagram shows the physics mark and the chemistry mark for each of 12 students.



(i) What type of correlation is shown in the scatter diagram?

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								 	 •	٠	•	•	•	•	•	٠	•						•	•	•	•	•			•	-		1	ı

(ii) On the scatter diagram, draw a line of best fit.

[1]

(iii) Find an estimate of the chemistry mark for another student who has a physics mark of 4.

Г1	1 -	1
 IJ	L	ı

**(b)** A teacher records the number of days each of the 24 students in her class are absent. The frequency table shows the results.

Number of days	0	1	2	3	4	5
Frequency	10	8	3	2	0	1

Find the mode, the median and the mean.

Mode =	
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(c) Three sizes of eggs are sold in a shop.

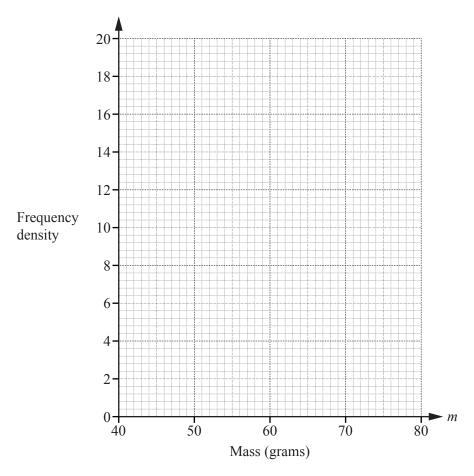
The table shows the number of eggs of each size sold in one day.

Size	Small	Medium	Large
Mass (m grams)	46 < <i>m</i> ≤ 52	52 < <i>m</i> ≤ 62	62 < <i>m</i> ≤ 80
Number of eggs sold	78	180	162

(i) Calculate an estimate of the mean mass.

..... g [4]

(ii) On the grid, draw a histogram to show the information in the table.



[4]

α ,								
Set	A	1	1	2		2		2
G .			1	] 1		1		2
Set	В	0	1	1		1		2
(i)	Jojo chooses t	two cards at	random from	Set A withou	t replac	ement.		
	Find the proba	ability that t	he two cards l	nave the same	numbe	er.		
<b>44</b> 0							• • • • • • • • • • • • • • • • • • • •	•••••
(ii)	Jojo replaces	the two card	C					
	Kylie then cho			from Set A ar	nd one o	eard at rando	m from	Set B.
		ooses one ca	ard at random				m from	Set B.
	Kylie then cho	ooses one ca	ard at random				m from	Set B.
	Kylie then cho	ooses one ca	ard at random				m from	Set B.
	Kylie then cho	ooses one ca	ard at random				m from	Set B.
	Kylie then cho	ooses one ca	ard at random				m from	Set B.
	Kylie then cho	ooses one ca	ard at random				m from	Set B.
	Kylie then cho	ooses one ca	ard at random					
(iii)	Kylie then che Find the proba	ooses one can ability that to	ard at random	nave the same	numbe	ег.		
(iii)	Kylie then che Find the proba	ooses one can ability that to	ard at random	nave the same	numbe	ег.		
(iii)	Kylie then che Find the proba	ooses one can ability that to	ard at random	nave the same	numbe	ег.		
(iii)	Kylie then che Find the proba	ooses one can ability that to	ard at random	nave the same	numbe	ег.		

(b)				1		
Set C	4	4	5		5	5

Lena chooses three cards at random from Set C without replacement.

Find the probability that the third card chosen is numbered 4.

[	3	1
	J	ı

(a)	There are 18	match, the price of an adult tick 500 adults and 2400 children are count paid for the tickets is \$320	ttending the footh		<i>−</i> 2.50).
	Find the price	ee of an adult ticket.			
(b)	(i) Factori	se $y^2 + 5y - 84$ .		\$	[4]
					[2]
	(ii)		y cm	NOT TO SCALE	
		(y+5) cm			
	The are	ea of the rectangle is 84 cm <sup>2</sup> .			
	Find th	e perimeter.			
					cm [3]

(c)	In a shop, the price of a monthly magazine is $m$ and the price of a weekly magazine is $(m-0.75)$ .
	One day, the shop receives

- \$168 from selling monthly magazines
- \$207 from selling weekly magazines.

The total number of these magazines sold during this day is 100.

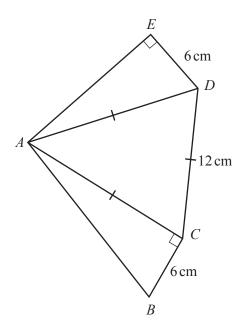
(i) Show that  $50m^2 - 225m + 63 = 0$ .

[3]

(ii) Find the price of a monthly magazine. Show all your working.

\$ ......[3]

6 (a)



NOT TO SCALE

In the pentagon ABCDE, angle ACB = angle AED = 90°. Triangle ACD is equilateral with side length 12 cm. DE = BC = 6 cm.

(i) Calculate angle *BAE*.

$Angle BAE = \dots [4]$
-------------------------

(ii) Calculate AB.

 $AB = \dots$  cm [2]

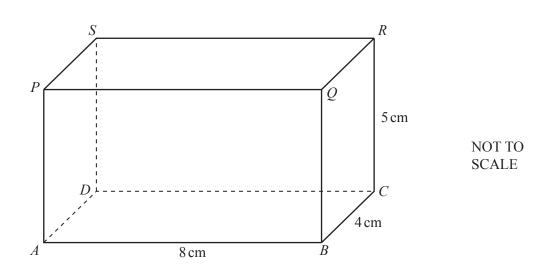
(iii) Calculate AE.

 $AE = \dots$  cm [3]

(iv) Calculate the area of the pentagon.

..... cm<sup>2</sup> [4]

**(b)** 



The diagram shows a cuboid. AB = 8 cm, BC = 4 cm and CR = 5 cm.

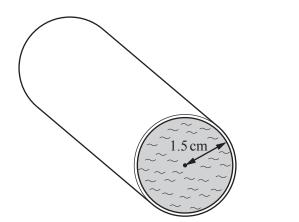
(i) Write down the number of planes of symmetry of this cuboid.

.....[1]

(ii) Calculate the angle between the diagonal AR and the plane BCRQ.

.....[4]

7 (a)



NOT TO SCALE

Water flows through a cylindrical pipe at a speed of 8 cm/s.

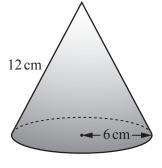
The radius of the circular cross-section is 1.5 cm and the pipe is always completely full of water.

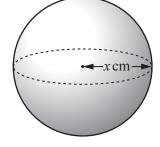
Calculate the amount of water that flows through the pipe in 1 hour. Give your answer in litres.

..... litres [4]

**(b)** 

NOT TO SCALE





The diagram shows three solids.

The base radius of the cone is 6 cm and the slant height is 12 cm.

The radius of the sphere is x cm and the radius of the hemisphere is y cm.

The **total** surface area of each solid is the same.

(i) Show that the total surface area of the cone is  $108\pi$  cm<sup>2</sup>.

[The curved surface area, A, of a cone with radius r and slant height l is  $A = \pi r l$ .]

[2]

(ii) Find the value of x and the value of y.

[The surface area, A, of a sphere with radius r is  $A = 4\pi r^2$ .]

 $x = \dots$ 

$$y = \dots$$
 [4]

8	(a)	$\mathbf{M} = \begin{pmatrix} 2 & 1 \\ 4 & 3 \end{pmatrix}$	$\mathbf{N} = \begin{pmatrix} 1 & 2 \end{pmatrix}$	$\mathbf{P} = \begin{pmatrix} 4 \\ 1 \end{pmatrix}$
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(i) For the following calculations, put a tick (✓) if it is possible or put a cross (x) if it is not possible. There is no need to carry out any of the calculations.

Calculation	✓ or ×
N + P	
NP	
$\mathbf{M}^2$	
$\mathbf{N}^2$	
MN	
NM	

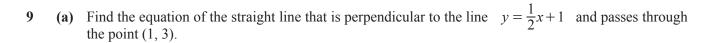
		L <sup>4</sup> .
(ii)	Work out $\binom{1}{2}$ + <b>P</b> .	

F13	
111	
±	

(iii) Work out PN.

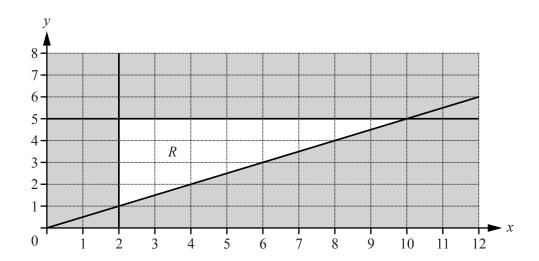
(iv) Work out  $\mathbf{M}^{-1}$ .

(b) Describe fully the **single** transformation represented by the matrix 
$$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$
.



.....[3]

**(b)** 



(i) Find the three inequalities that define the region R.

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						•	•	 			•	•	 	 												•				
																												4	ŀ	

(ii) Find the point (x, y), with integer co-ordinates, inside the region R such that 3x + 5y = 35.

10	(a)	f(x) = 2x - 3	$g(x) = x^2 + 1$	
	(i)	Find gg(2).		
	(ii)	Find $g(x+2)$ , giving y	our answer in its simplest form.	[2]
	(iii)	Find $x$ when $f(x) = 7$ .		[2]
	(iv)	Find $f^{-1}(x)$ .		<i>x</i> =[2]

$$f^{-1}(x) =$$
 [2]

	(b	)	h(x) = x	$x^x$ ,:	x >	0
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(i) Calculate h(0.3). Give your answer correct to 2 decimal places.

[	2]
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(ii) Find *x* when h(x) = 256.

$$x = \dots$$
 [1]

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