UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS
General Certificate of Education
Advanced Subsidiary Level and Advanced Level

## THINKING SKILLS

Paper 1 Problem Solving

## Additional Materials: Multiple Choice Answer Sheet

Soft clean eraser
Soft pencil (type B or HB is recommended)

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
There are $\mathbf{3 0}$ questions on this paper. Answer all the questions.
For each question there are four possible answers $\mathbf{A}, \mathbf{B}, \mathbf{C}$ and $\mathbf{D}$. Choose the one you consider correct and record your choice in pencil on the separate answer sheet.
Read very carefully the instructions on the answer sheet. Ignore responses numbered 31-40 on the answer sheet.

## INFORMATION FOR CANDIDATES

Each correct answer will score one mark. A mark will not be deducted for a wrong answer.

1 The hardware superstore is selling the paint I want at " 3 tins for the price of 2 ". This weekend I can get a further $10 \%$ off with my loyalty card.

What will be the overall reduction from the full price if I buy three tins of paint this weekend?
A $40 \%$
B $43 \%$
C $55 \%$
D 60\%

2 The table below shows the dates of the reigns of the monarchs of Portugal from 1640 to the abolition of the monarchy in 1910. (Where the dates overlap, this indicates a King and Queen ruling together.)

| Monarch | Start date | End date |
| :--- | ---: | ---: |
| João IV | 15 December 1640 | 06 November 1656 |
| Afonso VI | 06 November 1656 | 12 September 1683 |
| Pedro II | 12 September 1683 | 09 December 1706 |
| João V | 09 December 1706 | 31 July 1750 |
| José | 31 July 1750 | 24 February 1777 |
| Maria I | 24 February 1777 | 20 March 1816 |
| Pedro III | 24 February 1777 | 25 May 1786 |
| João VI | 20 March 1816 | 10 March 1826 |
| Pedro IV | 10 March 1826 | 05 May 1826 |
| Maria II | 05 May 1826 | 30 June 1828 |
| Miguel | 30 June 1828 | 26 May 1834 |
| Maria II (again) | 26 May 1834 | 15 November 1853 |
| Fernando II | 16 September 1837 | 15 November 1853 |
| Pedro V | 15 November 1853 | 11 November 1861 |
| Luís | 11 November 1861 | 19 October 1889 |
| Carlos | 19 October 1889 | 01 February 1908 |
| Manuel II | 01 February 1908 | 05 October 1910 |

Which monarch ruled for the longest?
A Afonso VI
B João V
C Luís
D Marial

3 Ying wants to tile his kitchen floor and is trying to decide between his four favourite tiles. However, only three of them are suitable for the job as one of them won't cover the floor without leaving numerous gaps.

Which one is it?

B


C


D


4 The pie chart below represents the relative areas that different colours occupy on a flag.


Which one of the following flags would yield a similar pie chart to the one above?
A
B
C
D


| $\mathrm{CO}_{2}$ <br> emissions <br> $(\mathrm{g} / \mathrm{km})$ | Tax 2011(\$) | $\mathrm{CO}_{2}$ <br> emissions <br> $(\mathrm{g} / \mathrm{km})$ | Tax 2012 (\$) | Tax 2013 (\$) |
| :---: | :---: | :---: | :---: | :---: |
| Up to 100 | 0 | Up to 100 | 0 | 0 |
| $101-120$ | 35 | $101-110$ | 35 | 20 |
| $121-150$ | 120 | $111-120$ | 35 | 35 |
| $151-165$ | 145 | $121-130$ | 120 | 90 |
| $166-185$ | 170 | $131-140$ | 120 | 105 |
| $186-225$ | 210 | $141-150$ | 125 | 125 |
| Over 225 | 400 | $151-165$ | 150 | 155 |
|  |  | $166-175$ | 175 | 180 |
|  |  | $176-185$ | 175 | 200 |
|  |  | $186-200$ | 215 | 235 |
|  | $201-225$ | 215 | 245 |  |
|  |  | Over 225 | 405 | 425 |

In New Ecoland car owners pay a yearly tax on their vehicles that depends on how much carbon dioxide $\left(\mathrm{CO}_{2}\right)$ is emitted by the vehicle per kilometre travelled. The first two columns in the table above show how the tax depends upon emissions for 2011. For 2012 and 2013 the authorities are dividing the emission bands into smaller ranges, and the final three columns show the taxes for 2012 and 2013.

Daphne owns two cars, an Adoks Retsmoor ( $\mathrm{CO}_{2}$ emission $\left.125 \mathrm{~g} / \mathrm{km}\right)$ and a WMB d525 $\left(\mathrm{CO}_{2}\right.$ emission $180 \mathrm{~g} / \mathrm{km}$ ).

Over the three years (2011, 2012 and 2013), how much more tax will Daphne pay on the WMB than the Adoks?

A $\$ 150$
B $\$ 165$
C $\$ 215$
D $\$ 330$

6 A group of 6 people, including 5 senior citizens, go to a restaurant for a meal.
3 people have meals costing $\$ 12$ each
2 people have meals costing $\$ 13$ each
1 person has a meal costing \$14
The restaurant has two special offers:

- Groups of 6 or more can have one of the cheapest meals free.
- Senior citizens get a reduction of $\$ 2.50$ each.

Only one special offer may be used at a time.
If they take the better special offer for the group, how much is the total bill?
A $\$ 51.50$
B $\$ 63.00$
C $\$ 63.50$
D $\$ 64.00$

7 The individual digits on my digital clock appear as words rather than numerals.
For example, at 18:07 the display is as shown below.


How many times each day does the letter E not appear on the display?
A 3
B 6
C 7
D 9

8 An eccentric engraver charges according to the particular letters that she has to engrave. She puts the lowercase letters of the alphabet into these categories:

| Type $\mathbf{1}$ | $\mathrm{a}, \mathrm{c}, \mathrm{e}, \mathrm{i}, \mathrm{n}, \mathrm{o}, \mathrm{r}, \mathrm{s}, \mathrm{u}, \mathrm{v}, \mathrm{x}, \mathrm{z}$ |
| :--- | :--- |
| Type $\mathbf{2}$ | $\mathrm{m}, \mathrm{w}$ |
| Type 3 | $\mathrm{b}, \mathrm{d}, \mathrm{f}, \mathrm{h}, \mathrm{k}, \mathrm{l}, \mathrm{t}$ |
| Type 4 | $\mathrm{g}, \mathrm{j}, \mathrm{p}, \mathrm{q}, \mathrm{y}$ |

She charges as follows:
10 cents for every Type 1 letter that is followed by a Type 1 or Type 2 letter 15 cents for every Type 1 letter that is not followed by a Type 1 or Type 2 letter 20 cents for every Type 2 letter
25 cents for every Type 3 letter that is followed by a Type 1 letter
30 cents for every Type 3 letter that is not followed by a Type 1 letter
35 cents for every Type 4 letter
40 cents for every capital letter, regardless of its Type
I want to have this word engraved:

## Sweetie

How much will this cost?
A 95 cents
B 105 cents
C 120 cents
D 135 cents

9 One square has been removed from a net of a cube. The remaining five squares are shown below.


Which one of the cubes shown below can not have been made from the full net?
A
B

C



10 Peter's Pizza Shop calculates the price for its pizzas by charging either $\$ 4$ or $\$ 9$ for the base (depending on whether it is a small or large pizza) and then adding 80申 for each meat topping (chicken, ham, bacon or beef) and $40 \phi$ for anything else. If an individual pizza costs more than $\$ 10$ then its price is reduced by $10 \%$. Delivery of the order costs $\$ 5$ regardless of the number of pizzas.

I want to buy a large pizza with chicken, bacon and mushrooms and a small pizza with ham and mushrooms, and have them delivered.

How much will I have to pay?
A $\$ 19.08$
B $\$ 19.58$
C $\quad \$ 20.10$
D $\$ 21.20$

11 A 'perpetual calendar' consists of 6 slots in a holder into which numbered cards are placed.


The year is shown by two digits (e.g. 2013 would be shown as " 13 "). If the day or month has just one digit, it is shown, for example, as " 07 ".

If this is to be genuinely perpetual (i.e. to work for any future date), which row of the following table correctly shows the minimum number of each card needed?

|  | Card |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| A | 3 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 5 |
| B | 3 | 5 | 5 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| C | 4 | 6 | 5 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| D | 4 | 6 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |

12 Deena takes 15 minutes to cycle to school, and her brother Callum walks there taking 30 minutes. Normally, Deena leaves home 6 minutes after Callum.

For how long does Deena cycle until she catches up with Callum?
A 6 minutes
B 9 minutes
C 12 minutes
D 15 minutes

13 Tops and tips are the only two ways of scoring points in the sport of T-Ball. In a thrilling T-Ball match this afternoon the Eagles beat the Panthers $48-47$. The Panthers had taken the lead in the third minute, scoring what proved to be the only top of the day. They then led right up to the last play of the game, which resulted in a victory-snatching tip for the Eagles.

Which one of the following could not be T-Ball's scoring system?
A A top scores 5 points, a tip scores 2 points.
B A top scores 5 points, a tip scores 3 points.
C A top scores 7 points, a tip scores 2 points.
D A top scores 7 points, a tip scores 3 points.

14 I have forgotten the 4-digit PIN for my cash card.
Each of the four digits can be $0,1,2,3,4,5,6,7,8$ or 9 .
However, I do remember these four facts:

- The second and third digits are the same.
- The first digit is one less than the fourth digit.
- The total of all four digits is 7 .
- The third digit is larger than the fourth digit.

What is the last digit in my PIN?
A 0
B 1
C 3
D 4

15 Geoffrey's mobile phone provider offers a choice of four plans. In each case there is a fixed price per month and a number of free minutes included in the price. There is then a fixed price for any further minutes used. The options are listed in the table below.

| Plan | Price per month (\$) | Number of free <br> minutes | Price per additional <br> minute $(\phi)$ |
| :---: | :---: | :---: | :---: |
| Cat | 30 | 300 | 10 |
| Dog | 30 | 450 | 20 |
| Horse | 50 | 300 | 5 |
| Llama | 50 | 450 | 15 |

It has now been announced that all of the prices per month will increase by $\$ 5$ and all of the prices for additional minutes will increase by $5 \phi$. Geoffrey's last bill was $\$ 70$, but it would have been $\$ 85$ with the new prices.

Which plan is Geoffrey currently using?
A Cat
B Dog
C Horse
D Llama

16 Central College started taking female students in 2004, having previously been all male. The numbers of male and female students admitted for subsequent years are shown in the table below:

| Year | Male | Female |
| :---: | :---: | :---: |
| 2004 | 120 | 35 |
| 2005 | 111 | 41 |
| 2006 | 102 | 52 |
| 2007 | 93 | 62 |
| 2008 | 111 | 89 |
| 2009 | 104 | 97 |
| 2010 | 99 | 101 |
| 2011 | 100 | 100 |

Which of the following graphs shows the percentage of students admitted in each year that were female?





17 Juan and Pilar have a cycle race. The course consists of a flat stretch followed by an uphill, then a downhill and finally another flat road. Juan goes faster than Pilar on the flat but Pilar goes uphill quicker than Juan. Downhill they go at approximately the same speed as each other. The result of the race is that they cross the finishing line at exactly the same time.

Which one of the following graphs best represents Juan's lead over Pilar from the start of the race to the finish?

A


B


C


D


18 I have a 24 -hour digital clock beside my bed which shows times from 00:00 to $23: 59$. When I woke up during the night, I noticed, to my surprise, that the product of the two hours digits was the same as the product of the two minutes digits. None of them was a zero.

Not counting times which include a zero, or where the hours and minutes use exactly the same digits (e.g. 12:21), how many times does this happen during a 24 -hour period?

A 6
B 7
C 9
D 10

19 Giles works at his local shop in his spare time. He always works for a whole number of hours, but receives a different rate of pay for working at weekends than in the week (both pay rates are a whole number of dollars per hour). Giles has worked for the same number of hours in each of the last two weeks, but his pay was $\$ 67$ in the first week and $\$ 79$ in the second week.

Which of the following could not explain Giles's pay in the last two weeks?
A Giles worked for 3 extra hours at the weekend in the second week.
B Giles is paid $\$ 4$ per hour more for working at the weekend.
C Giles worked for 5 extra hours at the weekend in the second week.
D Giles is paid $\$ 6$ per hour more for working at the weekend.

20 Colin said to Bill that the sum of the digits in his 3 -figure house number was 12 , and each digit was bigger than the one to the left of it. Bill said that was not enough information for him to work out the number.

Which one of the following additional pieces of information, on its own, would enable Bill to work out Colin's house number?

A One digit is equal to the difference of the other two.
B Colin's house number is even.
C Two of the digits multiply to 12 .
D The product of the digits is not a multiple of 6 .

21 A fleet of UFOs was observed, and pictures taken of them at the same time from different places: one looking from the north and the other looking from the west.


What is the largest number of UFOs that could be in the fleet?
A 3
B 5
C 6
D 9

22 My old mobile phone plan cost me $\$ 20$ per month, plus $3 \phi$ for each minute. I have just changed to a new plan which has no monthly charge, but costs $8 \phi$ per minute for the first 500 minutes and then $5 \phi$ per minute for all minutes after that.

Which of the following graphs shows the money that I save each month by changing to the new plan?





23 John travels to school every day by bus and train. As a senior student, his day can start at different times. He has to walk for 5 minutes to the bus stop, and the bus runs every 15 minutes starting on the hour. The bus journey lasts 15 minutes, and then he has to wait either 5 or 20 minutes for his train. The train journey takes 20 minutes.

Which of the following could explain the time he has to wait for his train?
A The trains run every 15 minutes starting at 07:05.
B The trains run every 20 minutes starting at 07:00.
C The trains run every 25 minutes starting at 07:00.
D The trains run every 30 minutes starting at 07:05.

24 My two daughters have plans to attend separate parties on Friday night.
Alice wants to go to the party at Charlie's house. It starts at 7 pm and finishes at 10:30 pm.
Elizabeth wants to attend Rhiannon's party at a club which is 15 minutes away from our home. It finishes at 10:40 pm.
They want me to drive them so that they arrive at the precise start times, and collect them at the precise end times.
I want us all to be home no later than 11 pm .
Which extra piece of information on its own would mean that not all of the above requirements can be satisfied?

A Charlie's house is 20 minutes from ours.
B Rhiannon's party starts at 7:15 pm.
C The club is 15 minutes away from Charlie's house.
D I do not get home from work until 6:30 pm.

25 A football league is comprised of 22 teams. Over the course of a season, each team plays each of the other teams twice (home and away). For every game that is played, 3 points are awarded to the winning side, 0 points to the losing side, and 1 point to each side if the match is drawn (equal score). There are no other possible outcomes to a game. Each team's total points from all their matches played are added together at the end of the season and the three clubs with the fewest points are relegated to a lower league. If two or more clubs finish with the same number of points, their positions are decided by goal difference, i.e. the difference between the total number of goals they have scored and the total number scored against them over the course of the season. A side with a higher goal difference finishes above one with a lower one.

What is the lowest number of points that a club can get in one season and not necessarily be relegated?

A 4
B 5
C 6
D 9

26 Tony makes ornaments which he sells in boxes that are cuboid in shape. The dimensions are either $5 \mathrm{~cm} \times 5 \mathrm{~cm} \times 12 \mathrm{~cm}$ or $5 \mathrm{~cm} \times 6 \mathrm{~cm} \times 10 \mathrm{~cm}$. He needs to package them in larger boxes to send out to the shops that sell the ornaments for him and he wants to buy just one size of box. The box needs to hold exactly 6 ornaments of the same type (regardless of which type it is).

The price of a box in cents is calculated by multiplying together the shortest two dimensions and then adding on the third. For example, a $2 \mathrm{~cm} \times 3 \mathrm{~cm} \times 4 \mathrm{~cm}$ box would cost $2 \times 3+4=10 \phi$. Tony wants to get the cheapest box possible.

What will be the price of one box?
A $\$ 0.86$
B $\quad \$ 0.90$
C $\quad \$ 0.97$
D $\$ 1.35$

27 When Mary won $\$ 3360$ on a TV quiz programme she decided to give it to her two grandchildren, Susan and Luke, to be shared between them in the ratio of their ages.

5 -year-old Luke complained that it wasn't fair that his older sister should get more than him. His mother sympathised, but told him to be thankful that his grandmother hadn't won the money next month (after Susan's birthday) when he would have received $\$ 70$ less, or last month (before his birthday) when he would have received $\$ 160$ less.

How much of Mary's $\$ 3360$ did Luke receive?
A $\$ 1050$
B $\$ 1120$
C $\$ 1200$
D $\$ 1400$

28 The hotel reception is staffed for 24 hours a day, 7 days a week, by one of the four receptionists. Whenever a receptionist comes to work he will work for 8 hours before the next receptionist takes over. The manager has a chart in her office which shows the availabilities for the receptionists, upon which they mark with a cross each shift for which they are unavailable. Wherever the manager has a choice of receptionist, she will assign the one whose previous shift was the longest time ago.

Karl is one of the receptionists and he worked on the first shift of the week both last Monday and this Monday. Karl was available for every shift last week, and all of the receptionists were available for the first shift this Monday.

What is the smallest number of crosses that there could be on the manager's chart for last week?
A 0
B 1
C 2
D 3

29 In the early stages of the Fantasy-World Cup the 24 competing teams are divided into four Groups of six. In each Group all teams play each other once, and the Group Winner progresses to the semi-finals. Teams gain 3 points for a win, 2 points for a score draw (1-1, $2-2$ etc.) and 1 point for a scoreless draw ( $0-0$ ).

This is the final table for Group 3:

|  | Played | Won | Drawn | Lost | Goals For | Goals Against | Points |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Narnia | 5 | 3 | 2 | 0 | 10 | 2 | 12 |
| Omnia | 5 | 3 | 1 | 1 | 8 | 2 | 11 |
| Xanadu | 5 | 2 | 1 | 2 | 8 | 6 | 8 |
| Utopia | 5 | 2 | 1 | 2 | 5 | 6 | 7 |
| Lilliput | 5 | 1 | 1 | 3 | 2 | 9 | 5 |
| Ruritania | 5 | 0 | 2 | 3 | 2 | 10 | 4 |

Narnia were losing $2-0$ during their last match, but two late goals from Tumnus, Narnia's striker, ensured qualification for the semi-finals.

Against which team did Narnia draw $2-2$ in their last group match?
A Lilliput
B Omnia
C Ruritania
D Xanadu

30 A computer's filing system uses a label with each file to determine who is allowed to use that file, and in what way. A label consists of nine characters: the first three for the user; the next three for the user's group; the last three for everyone. Each set of three covers the three functions 'read', 'write', and 'execute'.

For example, $r$ w $x$ r $w-r-\quad$ would permit the user to read, write or execute; any member of the group could read or write; and others could only read the file.

It is not valid to allow the group to do something but forbid the user. It is also not valid to allow everyone and forbid the group. All other combinations are valid, although these include some options which are unlikely to be useful.

How many valid labels are possible?
A 64
B 81
C 512
D 777

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