

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS General Certificate of Education Advanced Level

THINKING SKILLS

Paper 3 Problem Analysis and Solution

9694/33 May/June 2012 1 hour 30 minutes

Additional Materials:

Answer Booklet/Paper Electronic Calculator

READ THESE INSTRUCTIONS FIRST

If you have been given an Answer Booklet, follow the instructions on the front cover of the booklet. Write your Centre number, candidate number and name on all the work you hand in. Write in dark blue or black pen. Do not use staples, paper clips, highlighters, glue or correction fluid. DO **NOT** WRITE ON ANY BARCODES. Calculators should be used where appropriate.

Answer **all** the questions. Start each question on a new answer sheet.

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question.

This document consists of 8 printed pages and 4 blank pages.



www.papaCambridge.com The gold ducat is a coin currently worth 40 silver pennies, but, because of the scarcity King Offa is going to decree an increase in its value relative to the silver penny. Ethelred k that this will be done overnight on one of the next four nights (Mon, Tue, Wed, Thu), and that t value will go up once by 1, 2, or 3 pennies. All possibilities are equally likely.

Ethelred only has 30 silver pennies. He could get one or more overnight loans, but it costs a half penny to get a loan of 10 pennies from one day to the next.

His first thought was to take a loan of 10 pennies to obtain a ducat, and renew the loan each night until the revaluation. Then he would convert the ducat back to pennies.

(a)	(i)	What is the most he could gain with this strategy?	[1]
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(ii) What is the most he could lose? [1]

Ethelred tells Greta that the value of the ducat will change. She also has 30 pennies, but cannot afford to lose any money. She selects the strategy which gives the best chance of making some gain whilst ensuring that she will not lose any money.

(b) ((i)	Describe the strategy that Greta selects.	[2]
(ii)	What is the probability that she will make some gain?	[1]
(i	ii)	What is the most that she can gain?	[1]

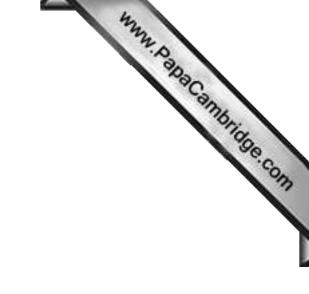
(iv) On Monday, what is the probability that she will have gained the maximum possible by Friday? [1]

On Tuesday, after no increase was announced on Monday night, Ethelred shares his insight with his friend Harold. Harold only has 20 pennies, and cannot afford to lose any money. He decides to wait until Thursday, because by then either the change will have happened, or he can be sure that he will not lose if he gets an overnight loan of 20 pennies.

(c) On Tuesday, what is Harold's chance of having more than 20 pennies on Friday? [2]

On Thursday, after three nights without a change, the money-lender decides to increase the cost of an overnight loan.

(d) How high would the cost have to be for a loan of 10 pennies before a borrower could not gain by taking a loan on the final night? [1]



[Question 2 is printed on the next page]

www.papaCambridge.com The first character of the serial number on Euro banknotes is a letter which indicates the which commissioned the note. Not all countries in the EU have adopted the Euro, but letters been allocated as follows:

Е	Slovakia	L	L Finland		France	
F	Cyprus	М	Portugal	V	Spain	
G	Malta	N Austria W D		Denmark		
Н	Slovenia	Р	P Netherlands		Germany	
J	UK	S	S Italy		Greece	
Κ	Sweden	Т	T Ireland		Belgium	
R	Luxembourg	ABCDIOQ			Not used	

The standard typewriter layout for an English-language keyboard is:

					/	r y	· ·				P
2						G				L	
ZXCVBNM											

A poor typist will sometimes miss a letter and get one of the surrounding ones. For example, G might be mistyped as T Y F H V or B, as shown above.

The current checking mechanism on the Euro notes will detect an error unless a letter is replaced by one 9 or 18 places along the normal alphabetical order, e.g. Y would not be detected if replaced by either G or P. Any other mistyped letter would be detected. An error would always be spotted if one of the 'not used' letters were typed.

A	В	С	D	Е	F	G	н	Ι
J	В К Т	L	Μ	N	0	P	Q	R
S	т	U	v	W	х	Y	z	

- (a) (i) If all 26 letters were in use, for which three pairs of letters would a mistyping of an adjacent key on the typewriter not be detectable? [2]
 - (ii) Given that the 19 letters specified above are allocated, for which two pairs of countries would a mistyping of an adjacent key **not** be detectable using the check? [1]

At present, only 19 letters are allocated, and yet some errors cannot be detected. In future, more countries may adopt the Euro. By reallocating the letters that are used for each country, it would be possible to choose a set of more than 19 letters such that a mistyping of an adjacent key would always be detectable.

- (b) (i) What is the largest possible size of a set of letters of the alphabet for which such errors would always be detectable? [2]
 - (ii) Give an example of such a set by listing the letters **not** used. [1]

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www.papaCambridge.com A new checking system and a reallocation of the letters are under consideration for the of Euro notes.

(c) A proposed new check only fails to detect shifts along the alphabetical order of multiples

А	В	С	D	E	F	G
H	I	J	к	L	Μ	N
0	Р	Q	R	S	т	U
V	W	х	Y	Z		

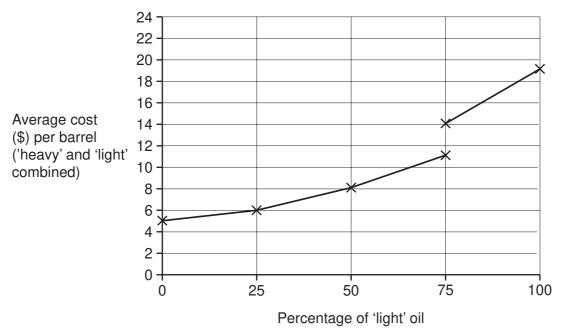
If the allocation of the letters remains as it currently is, which letter has the most possible undetectable errors when mistyping one of the surrounding keys? [2]

The current system splits the alphabet into 9 groups, yet has some adjacent keys in the same group. To detect errors from mistyping, it would be better to have a system designed to take account of the keyboard layout, rather than one based on alphabetical order.

(d) When all 26 letters are used, it is possible to have a system in which any mistyping of an adjacent letter would be detectable, using only three groups. Q, W and E must be in different groups. List all the letters in each of the three groups. [2]

www.papaCambridge.com The only oil refinery in Bolandia is the small one at Riebeeck. It can produce two grade 'light' and 'heavy'. All the oil from Riebeeck is sold in Bolandia. The total number of ba produced per day is constant.

If the percentage of 'light' required is above 75, the cost of production is higher because extra processing is needed.



Production costs

(The lines joining the points on the graph are straight.)

Initially, the government sets the selling price at \$20 per barrel for 'light' and \$10 per barrel for 'heavy'.

- (a) (i) When producing 25% 'light', the output of 'heavy' is 6000 barrels per day. What is the total daily profit? [2]
 - (ii) What proportion of 'light' oil should the refinery choose in order to maximise its profits?

[2]

The government changes its policy, and allows the price of 'light' to be set by the market, whilst keeping 'heavy' at \$10 per barrel.

- (b) What is the price for 'light' above which the refinery's profit becomes greatest by producing 75% 'light' and 25% 'heavy'? [3]
- (c) What is the lowest price for 'light' above which the refinery's maximum profit would always be gained by only producing 'light'? [3]

The crude oil used to make imported oil has a different chemical composition from the in Bolandia, so the costs of the two grades are not the same as for the Bolandian Imported oil has production costs of \$6 per barrel for 'heavy' and \$17 per barrel for regardless of the proportions produced.

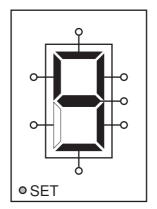
www.papaCambridge.com The consumption of oil in Bolandia is constant at 16000 barrels per day, of which half is imported Half of the total consumption is 'light' and half is 'heavy'. The price of 'light' is set by the importers (while the price of 'heavy' is fixed at \$10 per barrel). The refinery then decides what proportions of 'light' and 'heavy' to produce (seeking to maximise its own profit), and the importers supply the remainder.

(d) Determine what the importers' total daily profit would be if they set the price of 'light' at

(i)	\$43 per barrel,	[2]
(ii)	\$29 per barrel,	[2]
(iii)	\$21 per barrel.	[1]

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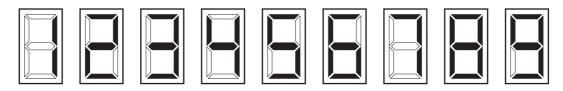
This is the apparatus that is used in Digitadd, a game for two players.



Each of the seven segments of the digital display (currently displaying the number 9) is controlled by its own button which reverses the state of the segment (i.e. turns it on or off) whenever it is pressed. When the SET button is pressed, a number between 1 and 9 inclusive, generated at random, is displayed.

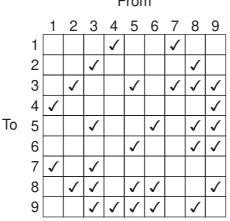
Rules of the Game of Digitadd

- 1 The game begins with a press of the SET button.
- 2 The two players take it in turns to press **one** or **two** of the segment buttons so that a different number is displayed. The new number is the player's score for the turn.
- 3 Each turn **must** produce one of the following displays:



- 4 No player may reverse the previous number change (e.g. if one player changes the display from 9 to 8, the other player cannot change it back to 9).
- 5 The first player to exceed a total of 50 (i.e. score at least 51) wins the game.

This table summarises all the number changes that are possible within the rules of Digitadd.



From

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The score of the player who takes the first turn is always given first. For example number is 8, the first player changes from 8 to 5 and the second player changes from scoreline after both players have had one turn is 5-6.

- www.papaCambridge.com (a) For a game where the SET number is 7, list all the different scorelines that are possible a both players have had one turn.
- (b) Oliver and Tamsin have just started a game of Digitadd. Oliver played first, but Tamsin is leading 8 – 9 now they have both had one turn.

State the four different numbers that the SET number could have been. [1]

- (c) When the SET number is 9, what number should the first player play in order to guarantee a lead of 7 points after both players have had two turns? [2]
- (d) After winning six consecutive games against him, Fiona has agreed to give Trevor a chance. In the game they are currently playing she has promised only to make changes that require just one button to be pressed whenever possible.

Trevor has just changed from 8 to 9. What options are now available to Fiona? [2]

When two newcomers to the game play together, the tendency is for both of them to score the greatest allowable amount every turn. If the SET number is 2, 3, 4, 5, 6, 8 or 9, this will always result in a final scoreline of either 54 - 46 or 55 - 46.

- (e) If both players in a game of Digitadd keep scoring the greatest allowable amount every turn, what are the other two possible final scorelines? [3]
- (f) Fay and Simon have just finished a game of Digitadd. Simon changed from 9 to 8 to lead 47 - 40, but Fay won the game.

[3]

Work out and explain how Fay managed to snatch victory.

Susan is teaching her little brother Edward how to play Digitadd. She wants to encourage him by allowing him to win, so she tells him to play the highest possible each time, while she decides to play the lowest. Edward plays first.

(g) When the SET number is 2, which numbers will not be played by either player during the game? [2]







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