## Cambridge Assessment International Education

Cambridge International General Certificate of Secondary Education

## MATHEMATICS <br> 0580/43

Paper 4 (Extended)
October/November 2017
MARK SCHEME
Maximum Mark: 130

## Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.
Cambridge International is publishing the mark schemes for the October/November 2017 series for most Cambridge IGCSE ${ }^{\circledR}$, Cambridge International A and AS Level components and some Cambridge O Level components.

## Abbreviations

| cao | correct answer only |
| :--- | :--- |
| dep | dependent |
| FT | follow through after error |
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| nfww | not from wrong working |
| soi | seen or implied |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 1(a)(i) | $180 \div(2+3+5) \times 5[=90]$ | 1 | with no errors seen |
| 1(a)(ii) | 7.05 or 7.053.... | 3 | M2 for $\frac{x}{12}=\sin 36$ oe or better or B1 for 36 or 54 seen |
| 1(b)(i) | 13 | 2 | M1 for $7.8 \div 3$ soi |
| 1(b)(ii) | 36.9 or 36.86 to 36.87 | 3 | B1 for smallest angle identified <br> M1 for $\sin []=\frac{3}{5}$ oe <br> or $\sin []=\frac{7.8}{\text { their }(\mathbf{b})(\mathbf{i})}$ oe <br> If zero scored, $\mathbf{S C 1}$ for calculation of 53.1 |
| 2(a) | 343 | 1 |  |
| 2(b)(i) | 1 | 1 |  |
| 2(b)(ii) | $x^{10}$ final answer | 1 |  |
| 2(b)(iii) | $9 x^{16}$ final answer | 2 | B1 for $x^{12}$ or $x^{16}$ or $\left(3 x^{8}\right)^{2}$ seen |
| 2(c)(i) | $2(x-3)(x+3)$ final answer | 2 | $\begin{aligned} & \text { M1 for }(2 x+6)(x-3) \text { or }(2 x-6)(x+3) \\ & \text { or }(x-3)(x+3) \end{aligned}$ |
| 2(c)(ii) | $\frac{2(x+3)}{x+10} \text { or } \frac{2 x+6}{x+10}$ <br> final answer nfww | 3 | M2 for $(x+10)(x-3)$ <br> or <br> M1 for $(x+a)(x+b)$ where $a b=-30$ or $a+b=7$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 3(a)(i) | 1890 | 2 | M1 for $126 \div 4[\times 60]$ oe If zero scored, SC1 for answer 31.5 |
| 3(a)(ii) | 103.95 | 4 | M3 for $0.5 \times\left(\frac{44}{60}+\frac{55}{60}\right) \times 126$ oe or SC3 for figs 10395 or figs 104 or M2 for two correct area methods or for a full method without minutes to hours conversion <br> or M1 for one correct area with or without minutes to hours conversion |
| 3(b)(i) | $126 \times 1000 \div(60 \times 60)$ | 1 |  |
| 3(b)(ii) | 46.3 or 46.28 to 46.29 | 3 | M2 for $(1400+220) \div 35$ oe or M1 for distance $\div$ speed or $1400+220$ |
| 3(c) | 180 nfww | 4 | B3 for final answer 3 <br> OR <br> M3 for $\frac{217.5}{72.5} \times 60$ oe or M2 for $217.5 \div 72.5$ oe or $\frac{210 \text { to } 220}{72.5} \times 60$ or $\frac{217.5}{72 \text { to } 74} \times 60$ <br> or M1 for 217.5 or 72.5 seen or $\frac{215}{73} \times 60$ |
| 4(a) | $80<t \leqslant 100$ | 1 |  |
| 4(b) | 86 nfww | 4 | M1 for midpoints soi <br> M1 for use of $\Sigma f x$ with $x$ in correct interval including both boundaries <br> M1 (dep on 2 nd M1) for $\Sigma f x \div 150$ |
| 4(c)(i) | Reference to not knowing the individual values so we do not know the highest or the lowest values | 1 |  |
| 4(c)(ii) | 62.4 | 2 | M1 for $26 \div 150$ or $360 \div 150$ soi |
| 4(d) | $\frac{22}{150} \text { oe }$ | 1 |  |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 4(e)(i) | $\frac{90}{22350} \text { oe }$ | 2 | M1 for $\frac{10}{150} \times \frac{9}{149}$ <br> After zero scored, SC1 for answer $\frac{100}{22500}$ oe |
| 4(e)(ii) | $\frac{440}{22350} \text { oe }$ | 3 | M2 for $\frac{10}{150} \times \frac{22}{149}+\frac{22}{150} \times \frac{10}{149}$ oe or M1 for $\frac{10}{150} \times \frac{22}{149}$ or $\frac{22}{150} \times \frac{10}{149}$ oe After zero scored, SC1 for answer $\frac{440}{22500}$ oe |
| 4(f) | 13, 8.5, 7.25, 1.1 | 3 | B2 for 3 correct <br> or <br> B1 for 1 correct or for 3 correct FD.s 5.2, 3.4, 2.9, 0.44 oe |
| 5(a)(i) | Image at (0, 1), (0, 2), ( $-3,1$ ) | 2 | B1 for reflection in $y=0$ or $x=k$ |
| 5(a)(ii) | Image at ( 0,0$),(0,-2),(6,-2)$ | 2 | B1 for correct size and correct orientation wrong position or for 2 correct vertices plotted |
| 5(a)(iii) | Image at (-5, 4), (-5, 5), (-2, 4) | 2 | B1 for translation by $\binom{-5}{k}$ or $\binom{k}{3}$ |
| 5(b) | Rotation $90^{\circ}$ clockwise oe $(4,-1)$ | 3 | B1 for each |
| 5(c)(i) | $(4,1)$ | 2 | M1 for $\left(\begin{array}{cc}0 & -1 \\ 1 & 0\end{array}\right)\binom{1}{-4}$ |
| 5(c)(ii) | $(8,-1)$ | 2 | $\begin{aligned} & \text { M1 for }\left(\begin{array}{cc} 0 & -1 \\ 1 & 0 \end{array}\right)\left(\begin{array}{ll} 3 & 1 \\ 0 & 2 \end{array}\right)\binom{1}{-4} \\ & \text { or }\left(\begin{array}{cc} 0 & -2 \\ 3 & 1 \end{array}\right)\binom{1}{-4} \\ & \text { or }\left(\begin{array}{cc} 0 & -1 \\ 1 & 0 \end{array}\right)\binom{-1}{-8} \end{aligned}$ |
| 5(c)(iii) | Rotation $90^{\circ}$ anti-clockwise oe Origin oe | 3 | B1 for each |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 6(a)(i) | 25.5 or $25.46 \ldots$ | 2 | M1 for $\pi \times 5^{2} \times h=2000$ oe |
| 6(a)(ii) | 9.85 or 9.847... | 3 | M2 for $\left[r^{3}=\right] 2000 \div\left(\frac{2}{3} \pi\right)$ oe or M1 for $\frac{2}{3} \pi r^{3}=2000$ oe |
| 6(a)(iii) | 952 or 952.4.... | 3 | M2 for $[6 \times] \sqrt[3]{2000}^{2}$ <br> or <br> M1 for $\sqrt[3]{2000}$ or 6 times their area of one face |
| 6(b)(i) | 22.5 or $22.49 \ldots$ | 2 | M1 for $\frac{1}{2} \times 7 \times 10 \times \sin 40$ |
| 6(b)(ii) | $\begin{aligned} & \sqrt{ }\left(10^{2}+7^{2}-2 \times 10 \times 7 \cos 40\right)+7 \\ & +10 \end{aligned}$ | M3 | M2 for $10^{2}+7^{2}-2 \times 10 \times 7 \cos 40$ or M1 for correct implicit cosine rule |
|  | 23.46... | A2 | A1 for $6.46 \ldots$ or 41.7 to 41.8 |
| 6(c) | 64.9 or 64.92 to 64.94 | 3 | $\begin{aligned} & \text { M2 for } 28.2-2 \times 9=\frac{c}{360} \times 2 \times \pi \times 9 \text { oe } \\ & \text { or M1 for } \frac{c}{360} \times 2 \times \pi \times 9 \text { soi } \end{aligned}$ |
| 7(a) | 9, -6, 9 | 3 | B1 for each |
| 7(b) | Correct graph | 4 | B3FT for 6 or 7 correct points or B2FT for 4 or 5 correct points or B1FT for 2 or 3 correct points |
| 7(c) | -3.5 to -3.35 and 0.8 to 0.9 .. | 2FT | FT their graph B1FT for either |
| 7(d) | $\begin{aligned} & a=\frac{5}{4} \text { or } 1 \frac{1}{4} \text { or } 1.25 \\ & b=-\frac{49}{8} \text { or }-6 \frac{1}{8} \text { or }-6.125 \end{aligned}$ | 3 | B2 for either correct or M1 for [2] $\left(x+\frac{5}{4}\right)^{2}$ seen isw or for $2 x^{2}+4 a x+2 a^{2}+b$ |
| 8(a)(i) | 5 | 1 |  |
| 8(a)(ii) | $-\frac{3}{2} \text { oe }$ | 1 |  |
| 8(b) | $\left(\frac{4}{5}, 0\right)$ oe | 2 | M1 for $5 x-4=0$ soi |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 8(c) | $y=-0.2 x+11$ final answer | 4 | M2 for $y=-0.2 x+c$ oe (any form) FT their <br> (a) <br> or <br> B1FT for grad $=\frac{-1}{\text { their } \mathbf{( a ) ( i )}}$ soi <br> and M1 for substitution of $(10,9)$ into their equation |
| 8(d) | $(2,6)$ | 3 | M1 for elimination of one variable A1 for $x=2$ or $y=6$ |
| 8(e) | 13 | 3 | M2 for $(4+9) \times$ their $2 \div 2$ oe or <br> B1 for 9 oe or 4 or -4 seen |
| 9(a) | $\frac{10}{x-0.5}$ oe final answer | 1 | $\text { Accept } \frac{20}{2 x-1}$ |
| 9(b)(i) | $\frac{10}{x-0.5}-\frac{10}{x}=0.25$ oe | M1 | FT their (a) |
|  | $10 x-10(x-0.5)=0.25 x(x-0.5)$ <br> oe | M1 | Clears algebraic denominators or collects as a single fraction FT their algebraic fractions dep on two fractions with algebraic denominators |
|  | $10 x-10 x+5=0.25 x^{2}-0.125 x$ or better | B1 | Expands brackets |
|  | $2 x^{2}-x-40=0$ | A1 | Dep on M1M1B1 and no errors seen |
| 9(b)(ii) | $\frac{--1 \pm \sqrt{(-1)^{2}-4 \times 2 \times-40}}{2 \times 2} \mathrm{oe}$ | B2 | B1 for $\sqrt{(-1)^{2}-4(2)(-40)}$ or better or B1 for $\frac{--1+\sqrt{q}}{2 \times 2}$ or $\frac{--1-\sqrt{q}}{2 \times 2}$ or both |
|  | -4.23 and 4.73 final answers | B1 B1 | SC1 for $-4.229 \ldots$ and 4.729... <br> or for -4.23 and 4.73 seen in working or for -4.73 and 4.23 as final answer or for -4.2 or -4.22 and 4.7 or 4.72 as final answer |
| 9(b)(iii) | 2 [hours] 7 [minutes] | 3 | B2 for 2.11 or 2.114 to 2.115 or 126.8 to 126.9 or 127 <br> or M1 for $10 \div$ their positive root from (b)(ii) |
| 10(a)(i) | $2^{2} \times 3^{2} \times 5$ oe | 2 | M1 for 3 correct prime factors in a tree or table seen before the first error or for $2,3,5$ identified |
| 10(a)(ii) | 540 | 2 | M1 for $2^{2} \times 3^{3} \times 5$ or $2 \times 3^{3}$ shown or answer 540k |


| Question | Answer | Marks | Partial Marks |
| :---: | :--- | ---: | :--- |
| $10(\mathrm{~b})$ | $X=8575$ | $\mathbf{4}$ | B3 for $X=8575$ or $Y=6125$ <br> or <br> B2 for $a=5$ or $b=1$ soi <br> or <br> B1 for $1225=5^{2} \times 7^{2}$ or $42875=5^{3} \times 7^{3}$ <br> or <br>  <br> $Y=6125$ |
|  |  | M1 for $a^{2} \times 7^{2}[=1225]$ or $a^{3} \times 7^{b+2}[=42875]$ |  |

