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MATHEMATICS 0580/43
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MARK SCHEME

Maximum Mark: 130

Published

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Abbreviations

correct answer only cao

dependent dep

FΤ follow through after error ignore subsequent working isw

or equivalent oe Special Case SC

not from wrong working seen or implied nfww

soi

Question	Answer	Marks	Partial Marks
1(a)(i)	$180 \div (2+3+5) \times 5 = 90$	1	with no errors seen
1(a)(ii)	7.05 or 7.053	3	M2 for $\frac{x}{12} = \sin 36$ oe or better or B1 for 36 or 54 seen
1(b)(i)	13	2	M1 for 7.8 ÷ 3 soi
1(b)(ii)	36.9 or 36.86 to 36.87	3	B1 for smallest angle identified M1 for $\sin[\] = \frac{3}{5}$ oe or $\sin[\] = \frac{7.8}{their(\mathbf{b})(\mathbf{i})}$ oe If zero scored, SC1 for calculation of 53.1
2(a)	343	1	
2(b)(i)	1	1	
2(b)(ii)	x^{10} final answer	1	
2(b)(iii)	$9x^{16}$ final answer	2	B1 for x^{12} or x^{16} or $(3x^8)^2$ seen
2(c)(i)	2(x-3)(x+3) final answer	2	M1 for $(2x+6)(x-3)$ or $(2x-6)(x+3)$ or $(x-3)(x+3)$
2(c)(ii)	$\frac{2(x+3)}{x+10} \text{ or } \frac{2x+6}{x+10}$ final answer nfww	3	M2 for $(x + 10)(x - 3)$ or M1 for $(x + a)(x + b)$ where $ab = -30$ or $a + b = 7$

Question	Answer	Marks	Partial Marks
3(a)(i)	1890	2	M1 for 126 ÷ 4 [× 60] oe If zero scored, SC1 for answer 31.5
3(a)(ii)	103.95	4	M3 for $0.5 \times \left(\frac{44}{60} + \frac{55}{60}\right) \times 126$ oe or SC3 for figs 10395 or figs 104
			or M2 for two correct area methods or for a full method without minutes to hours conversion
			or M1 for one correct area with or without minutes to hours conversion
3(b)(i)	$126 \times 1000 \div (60 \times 60)$	1	
3(b)(ii)	46.3 or 46.28 to 46.29	3	M2 for (1400 + 220) ÷ 35 oe or M1 for distance ÷ speed or 1400 + 220
3(c)	180 nfww	4	B3 for final answer 3 OR M3 for $\frac{217.5}{72.5} \times 60$ oe
			or M2 for 217.5 ÷ 72.5 oe or $\frac{210 \text{ to } 220}{72.5} \times 60$ or $\frac{217.5}{72 \text{ to } 74} \times 60$
			or M1 for 217.5 or 72.5 seen or $\frac{215}{73} \times 60$
4(a)	80 < <i>t</i> ≤ 100	1	
4(b)	86 nfww	4	M1 for midpoints soi
			M1 for use of Σfx with x in correct interval including both boundaries
			M1 (dep on 2nd M1) for $\Sigma fx \div 150$
4(c)(i)	Reference to not knowing the individual values so we do not know the highest or the lowest values	1	
4(c)(ii)	62.4	2	M1 for 26 ÷ 150 or 360 ÷ 150 soi
4(d)	$\frac{22}{150}$ oe	1	

Question	Answer	Marks	Partial Marks
4(e)(i)	$\frac{90}{22350}$ oe	2	M1 for $\frac{10}{150} \times \frac{9}{149}$ After zero scored, SC1 for answer $\frac{100}{22500}$ oe
4(e)(ii)	440 22350 oe	3	M2 for $\frac{10}{150} \times \frac{22}{149} + \frac{22}{150} \times \frac{10}{149}$ oe or M1 for $\frac{10}{150} \times \frac{22}{149}$ or $\frac{22}{150} \times \frac{10}{149}$ oe After zero scored, SC1 for answer $\frac{440}{22500}$ oe
4(f)	13, 8.5, 7.25, 1.1	3	B2 for 3 correct or B1 for 1 correct or for 3 correct FD.s 5.2, 3.4, 2.9, 0.44 oe
5(a)(i)	Image at (0, 1), (0, 2), (-3, 1)	2	B1 for reflection in $y = 0$ or $x = k$
5(a)(ii)	Image at $(0, 0), (0, -2), (6, -2)$	2	B1 for correct size and correct orientation wrong position or for 2 correct vertices plotted
5(a)(iii)	Image at (-5, 4), (-5, 5), (-2, 4)	2	B1 for translation by $\binom{-5}{k}$ or $\binom{k}{3}$
5(b)	Rotation 90° clockwise oe (4, -1)	3	B1 for each
5(c)(i)	(4, 1)	2	M1 for $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ -4 \end{pmatrix}$
5(c)(ii)	(8, -1)	2	$\mathbf{M1} \text{ for } \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 3 & 1 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} 1 \\ -4 \end{pmatrix}$ or $\begin{pmatrix} 0 & -2 \\ 3 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ -4 \end{pmatrix}$ or $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} -1 \\ -8 \end{pmatrix}$
5(c)(iii)	Rotation 90° anti-clockwise oe Origin oe	3	B1 for each

Question	Answer	Marks	Partial Marks
6(a)(i)	25.5 or 25.46	2	M1 for $\pi \times 5^2 \times h = 2000$ oe
6(a)(ii)	9.85 or 9.847	3	M2 for $[r^3=] 2000 \div \left(\frac{2}{3}\pi\right)$ oe or M1 for $\frac{2}{3}\pi r^3 = 2000$ oe
6(a)(iii)	952 or 952.4	3	M2 for $[6 \times] \sqrt[3]{2000}^2$ or M1 for $\sqrt[3]{2000}$ or 6 times <i>their</i> area of one face
6(b)(i)	22.5 or 22.49	2	M1 for $\frac{1}{2} \times 7 \times 10 \times \sin 40$
6(b)(ii)	$\sqrt{(10^2 + 7^2 - 2 \times 10 \times 7 \cos 40) + 7} + 10$	М3	M2 for $10^2 + 7^2 - 2 \times 10 \times 7 \cos 40$ or M1 for correct implicit cosine rule
	23.46	A2	A1 for 6.46 or 41.7 to 41.8
6(c)	64.9 or 64.92 to 64.94	3	M2 for $28.2 - 2 \times 9 = \frac{c}{360} \times 2 \times \pi \times 9$ oe or M1 for $\frac{c}{360} \times 2 \times \pi \times 9$ soi
7(a)	9, -6, 9	3	B1 for each
7(b)	Correct graph	4	B3FT for 6 or 7 correct points or B2FT for 4 or 5 correct points or B1FT for 2 or 3 correct points
7(c)	-3.5 to -3.35 and 0.8 to 0.9	2FT	FT their graph B1FT for either
7(d)	$a = \frac{5}{4} \text{ or } 1\frac{1}{4} \text{ or } 1.25$ $b = -\frac{49}{8} \text{ or } -6\frac{1}{8} \text{ or } -6.125$	3	B2 for either correct or M1 for $[2]\left(x + \frac{5}{4}\right)^2$ seen isw or for $2x^2 + 4ax + 2a^2 + b$
8(a)(i)	5	1	
8(a)(ii)	$-\frac{3}{2}$ oe	1	
8(b)	$\left(\frac{4}{5},\ 0\right)$ oe	2	M1 for $5x - 4 = 0$ soi

Question	Answer	Marks	Partial Marks
8(c)	y = -0.2x + 11 final answer	4	M2 for $y = -0.2x + c$ oe (any form) FT their (a) or B1FT for grad = $\frac{-1}{their}$ soi and M1 for substitution of (10, 9) into their equation
8(d)	(2, 6)	3	M1 for elimination of one variable A1 for $x = 2$ or $y = 6$
8(e)	13	3	M2 for (4 + 9) × their 2 ÷ 2 oe or B1 for 9 oe or 4 or –4 seen
9(a)	$\frac{10}{x-0.5}$ oe final answer	1	Accept $\frac{20}{2x-1}$
9(b)(i)	$\frac{10}{x - 0.5} - \frac{10}{x} = 0.25 \text{ oe}$	M1	FT their (a)
	10x - 10(x - 0.5) = 0.25x (x - 0.5) oe	M1	Clears algebraic denominators or collects as a single fraction FT <i>their</i> algebraic fractions dep on two fractions with algebraic denominators
	$10x - 10x + 5 = 0.25x^2 - 0.125x \text{ or}$ better	B1	Expands brackets
	$2x^2 - x - 40 = 0$	A1	Dep on M1M1B1 and no errors seen
9(b)(ii)	$\frac{-1\pm\sqrt{(-1)^2-4\times2\times-40}}{2\times2} \text{ oe}$	B2	B1 for $\sqrt{(-1)^2 - 4(2)(-40)}$ or better or B1 for $\frac{1 + \sqrt{q}}{2 \times 2}$ or $\frac{1 - \sqrt{q}}{2 \times 2}$ or both
	-4.23 and 4.73 final answers	B1 B1	SC1 for -4.229 and 4.729 or for -4.23 and 4.73 seen in working or for -4.73 and 4.23 as final answer or for -4.2 or -4.22 and 4.7 or 4.72 as final answer
9(b)(iii)	2 [hours] 7 [minutes]	3	B2 for 2.11 or 2.114 to 2.115 or 126.8 to 126.9 or 127 or M1 for 10 ÷ <i>their</i> positive root from (b)(ii)
10(a)(i)	$2^2 \times 3^2 \times 5$ oe	2	M1 for 3 correct prime factors in a tree or table seen before the first error or for 2, 3, 5 identified
10(a)(ii)	540	2	M1 for $2^2 \times 3^3 \times 5$ or 2×3^3 shown or answer $540k$

Question	Answer	Marks	Partial Marks
10(b)	<i>X</i> = 8575	4	B3 for $X = 8575$ or $Y = 6125$
	<i>Y</i> = 6125		or B2 for $a = 5$ or $b = 1$ soi or B1 for $1225 = 5^2 \times 7^2$ or $42875 = 5^3 \times 7^3$ or M1 for $a^2 \times 7^2$ [= 1225] or $a^3 \times 7^{b+2}$ [= 42875]