## Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

## CANDIDATE NAME

CENTRE NUMBER


## MATHEMATICS

0580/42
Paper 4 (Extended)
May/June 2017
2 hours 30 minutes
Candidates answer on the Question Paper.
Additional Materials: Electronic calculator Geometrical instruments Tracing paper (optional)

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use an HB pencil for any diagrams or graphs.
Do not use staples, paper clips, glue or correction fluid.
DO NOT WRITE IN ANY BARCODES.
Answer all questions.
If working is needed for any question it must be shown below that question.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For $\pi$, use either your calculator value or 3.142 .
At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 130 .

1 (a) Annie and Dermot share $\$ 600$ in the ratio $11: 9$.
(i) Show that Annie receives $\$ 330$.
(ii) Find the amount that Dermot receives.
(b) (i) Annie invests $\$ 330$ at a rate of $1.5 \%$ per year compound interest.

Calculate the amount that Annie has after 8 years.
Give your answer correct to the nearest dollar.
\$
(ii) Find the amount of interest that Annie has, after the 8 years, as a percentage of the $\$ 330$.
(c) Dermot has $\$ 70$ to spend.

He spends $\$ 24.75$ on a shirt.
(i) Find $\$ 24.75$ as a fraction of $\$ 70$.

Give your answer in its lowest terms.
(ii) The $\$ 24.75$ is the sale price after reducing the original price by $10 \%$.

Calculate the original price.
\$
(d) After one year, the value of Annie's car had reduced by $20 \%$.

At the end of the second year, the value of Annie's car had reduced by a further $15 \%$ of its value at the end of the first year.
(i) Calculate the overall percentage reduction after the two years.
$\qquad$
(ii) After three years the overall percentage reduction in the value of Annie's car is $40.84 \%$.

Calculate the percentage reduction in the third year.

2 (a)


On the grid, draw the image of
(i) triangle $T$ after translation by the vector $\binom{6}{-5}$,
(ii) triangle $T$ after rotation through $90^{\circ}$ anticlockwise with centre $(4,10)$,
(iii) triangle $T$ after enlargement with scale factor $\frac{1}{2}$, centre $(10,0)$.
(b) Describe fully the single transformation that is represented by the matrix $\left(\begin{array}{rr}0 & -1 \\ -1 & 0\end{array}\right)$.
$\qquad$
$\qquad$
(c) $\mathbf{M}=\left(\begin{array}{ll}2 & 3 \\ 2 & 4\end{array}\right) \quad \mathbf{N}=\binom{2}{3} \quad \mathbf{P}=\left(\begin{array}{ll}1 & 5\end{array}\right)$
(i) Find
(a) MN ,

$$
\mathbf{M N}=
$$

(b) NP,

$$
\begin{equation*}
\mathbf{N P}= \tag{2}
\end{equation*}
$$

(c) $\mathbf{M}^{-1}$.

$$
\mathbf{M}^{-1}=\quad(
$$

(ii) Write down a product of two of the matrices $\mathbf{M}, \mathbf{N}$ and $\mathbf{P}$ which it is not possible to work out.

3 (a) 200 students estimate the capacity, $x$ millilitres, of a cup. The results are shown in the frequency table.

| Capacity $(x \mathrm{ml})$ | $0<x \leqslant 100$ | $100<x \leqslant 150$ | $150<x \leqslant 200$ | $200<x \leqslant 250$ | $250<x \leqslant 400$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 20 | 55 | 66 | 35 | 24 |

(i) Calculate an estimate of the mean.
(ii) Complete the histogram.

(b) The 200 students also estimate the mass, $m$ grams, of a small rock.

The results are shown in the cumulative frequency table.

| Mass ( $m$ grams) | $m \leqslant 50$ | $m \leqslant 100$ | $m \leqslant 150$ | $m \leqslant 200$ | $m \leqslant 250$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Cumulative frequency | 28 | 64 | 104 | 168 | 200 |

(i) On the grid, draw a cumulative frequency diagram.

[3]
(ii) Find
(a) the 65th percentile,
(b) the number of students who estimated more than 75 g .

$$
\mathrm{f}(x)=2 x^{2}-1
$$

The graph of $y=\mathrm{f}(x)$, for $-2 \leqslant x \leqslant 2$, is drawn on the grid.

(a) Use the graph to solve the equation $\mathrm{f}(x)=5$.

$$
\begin{equation*}
x=\ldots . . . . . . . . . . . . . . . . . . . . . ~ o r ~ x= \tag{2}
\end{equation*}
$$

(b) (i) Draw the tangent to the graph of $y=\mathrm{f}(x)$ at the point $(-1.5,3.5)$.
(ii) Use your tangent to estimate the gradient of $y=\mathrm{f}(x)$ when $x=-1.5$.
(c) $\quad \mathrm{g}(x)=2^{x}$
(i) Complete the table for $y=\mathrm{g}(x)$.

| $x$ | -2 | -1 | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 0.25 | 0.5 |  | 2 | 4 |

(ii) On the grid opposite, draw the graph of $y=\mathrm{g}(x)$ for $-2 \leqslant x \leqslant 2$.
(d) Use your graphs to solve
(i) the equation $\mathrm{f}(x)=\mathrm{g}(x)$,

$$
x=\ldots . \ldots . . . . . . . . . . . . . . . . . . . ~ o r ~ x=.
$$

(ii) the inequality $\mathrm{f}(x)<\mathrm{g}(x)$.
(e) (i) Write down the three values.
$g(-3)=$ $\qquad$

$$
\mathrm{g}(-5)=
$$

$\qquad$ $g(-10)=$
(ii) Complete the statement.

As $x$ decreases, $g(x)$ approaches the value


The diagram shows a hollow cone with radius 3 cm and slant height 10 cm .
(a) (i) Calculate the curved surface area of the cone.
[The curved surface area, $A$, of a cone with radius $r$ and slant height $l$ is $A=\pi r l$.]
$\qquad$ $\mathrm{cm}^{2}$ [2]
(ii) Calculate the perpendicular height of the cone.
$\qquad$ cm [3]
(iii) Calculate the volume of the cone.
[The volume, $V$, of a cone with radius $r$ and height $h$ is $V=\frac{1}{3} \pi r^{2} h$.]
$\qquad$
(b)


NOT TO
SCALE

The cone is cut along the line $O P$ and is opened out into a sector as shown in the diagram.
Calculate the sector angle $x$.

$$
x=
$$

(c)


NOT TO
SCALE

The diagram shows the same sector as in part (b).
Calculate the area of the shaded segment.

6 Each morning the probability that it rains is $\frac{2}{3}$.
If it rains, the probability that Asha walks to school is $\frac{1}{7}$.
If it does not rain, the probability that Asha walks to school is $\frac{4}{7}$.
(a) Complete the tree diagram.

(b) Find the probability that it rains and Asha walks to school.
(c) (i) Find the probability that Asha does not walk to school.
(ii) Find the expected number of days Asha does not walk to school in a term of 70 days.
(d) Find the probability that it rains on exactly one morning in a school week of 5 days.

7 (a) In this part, all lengths are in centimetres.

(i) Find the value of $x$ when the perimeter of the rectangle is equal to the perimeter of the square.

$$
x=
$$

(ii) Find the value of $x$ when the area of the rectangle is equal to the area of the square. Show all your working.

$$
x=
$$

(b) (i) Factorise $x^{2}+4 x-5$.
(ii) Solve the equation $\frac{5}{x}-\frac{8}{x+1}=1$.

Show all your working.

$$
x=
$$

or $x=$


The diagram shows a pyramid on a rectangular base $A B C D$.
$A C$ and $B D$ intersect at $M$ and $P$ is vertically above $M$.
$A B=8 \mathrm{~cm}, B C=6 \mathrm{~cm}$ and $P M=9 \mathrm{~cm}$.
(a) $N$ is the midpoint of $B C$.

Calculate angle $P N M$.
(b) Show that $B M=5 \mathrm{~cm}$.
(c) Calculate the angle between the edge $P B$ and the base $A B C D$.
(d) A point $X$ is on $P C$ so that $P X=7.5 \mathrm{~cm}$.

Calculate $B X$.
$B X=$
cm [6]
$9 \quad$ (a)


The distance-time graph shows the journey of a train.
(i) Find the speed of the train between 0700 and 0730 .
$\qquad$ $\mathrm{km} / \mathrm{h}$ [1]
(ii) Find the average speed for the whole journey.
$\qquad$
(b)


The speed-time graph shows the first 30 minutes of another train journey.
The distance travelled is 100 km .
The maximum speed of the train is $V \mathrm{~km} / \mathrm{h}$.
(i) Find the value of $V$.

$$
\begin{equation*}
V=. \tag{3}
\end{equation*}
$$

(ii) Find the acceleration of the train during the first 5 minutes. Give your answer in $\mathrm{m} / \mathrm{s}^{2}$.
$\qquad$
$\mathrm{f}(x)=3 x-2$
$g(x)=x^{2}$
$\mathrm{h}(x)=3^{x}$
(a) Find $\mathrm{f}(-3)$.
$\qquad$
(b) Find the value of $x$ when $\mathrm{f}(x)=19$.

$$
x=
$$

(c) Find fh(2).
$\qquad$
(d) Find $\operatorname{gf}(x)+\mathrm{f}(x)+x$.

Give your answer in its simplest form.
(e) Find $\mathrm{f}^{-1}(x)$.

$$
\mathrm{f}^{-1}(x)=
$$

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