## MARK SCHEME for the May/June 2014 series

## 0580 MATHEMATICS

0580/43
Paper 4 (Extended), maximum raw mark 130

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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## Abbreviations

| cao | correct answer only |
| :--- | :--- |
| dep | dependent |
| FT | follow through after error |
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| nfww | not from wrong working |
| soi | seen or implied |


| Qu |  | Answers | Mark | Part Marks |
| :---: | :---: | :---: | :---: | :---: |
| 1 | (a) <br> (b) <br> (c) <br> (d) <br> (e) | 62100[.00] Final answer <br> 39300 <br> 20436 <br> 4 <br> 25545 | $3$ <br> 2 <br> 3 | B1 for 62074[. 35] or 62070 <br> M2 for 45981:-1.17 oe or M1 for 45981 associated with 117 [\%] M1 for $45981 \div(3+4+2)$ or $45981 \times 4$ M2 for $\frac{1.5 \times 1000}{330}$ oe or M1 for figs 4545... or 455 <br> M1 for $45981 \times \frac{5}{9}$ |
| 2 | (a) | $\begin{aligned} & 10<x \leq 25 \quad 25<x \leq 30 \\ & 30<x \leq 35 \quad 35<x \leq 50 \\ & 50<x \leq 60 \\ & \\ & 133319[4] 156 \\ & 25.1[0] \text { or } 25.13 \text { to } 25.14 \mathrm{nfww} \end{aligned}$ | 3 | 5 correct <br> B1 for 3 or 4 correct <br> or SC1 for all correct but in the form 10 to <br> 25 or $10-25$ <br> B2 for 4 correct <br> or B1 for 3 correct <br> M1 for mid-values soi, condone one error or omission <br> 517.527 .532 .542 .555 soi <br> and M1 for $\Sigma f x$ for any $x$ in intervals including boundaries, but all $f$ s must be integers, condone one further error or omission <br> and M1 dep for $\Sigma f x \div 90$ <br> Dep on $2 \mathrm{nd} \mathbf{M}$ mark earned |


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| Qu |  | Answers | Mark | Part Marks |
| :---: | :---: | :---: | :---: | :---: |
| 3 | (a) (i) <br> (ii) <br> (b) <br> (c) | $72[.0]$ or 71.98 to 71.99 nfww <br> 16.2 or 16.18 to 16.19 nfww <br> 7.61 or $7.612 \ldots$ nfww <br> 50 <br> 130 | 1 | M2 for $[\sin \mathrm{P}=] \frac{97}{\frac{1}{2} \times 12 \times 17}$ oe or M1 for implicit version <br> M2 for $6^{2}+17^{2}-2 \times 6 \times 17 \times \cos$ (their 72 ) or M1 for implicit form and A1 for $\left[X R^{2}=\right] 261.8$ to 262 <br> M3 for $[a=] 9.4 \times \sin 37 \div \cos 42$ oe or $[a=] 9.4 \sin 37 / \sin (90-42)$ <br> or M2 for $[a=$ ] their height $\div \cos 42$ oe or $\frac{a}{\sin 37}=\frac{9.4}{\sin (90-42)}$ oe <br> or M1 for their height $\div a=\cos 42$ or for [their height $=$ ] $9.4 \times \sin 37$ oe <br> or B1 for $48^{\circ}$ correctly used or seen in correct position on diagram |
| 4 | (a) <br> (b) <br> (c) <br> (d) | $0,4.5,3.11[1 \ldots]$ <br> Complete correct curve with minimum below $y=2$ $\begin{array}{\|l} -0.5 \text { to }-0.6 \\ 0.6 \text { to } 0.7 \\ 2.8 \text { to } 2.9 \end{array}$ <br> Correct line or no line and -0.7 to -0.6 nfww | 5 $\begin{aligned} & 1 \\ & 1 \\ & 1 \\ & 3 \end{aligned}$ | B1, B1, B1 <br> B3 FT for 9 points correctly plotted <br> B2 FT for 7 or 8 points correctly plotted or B1 FT 5 or 6 points correctly plotted <br> and B1 indep two separate branches not touching or cutting $y$-axis <br> if $0 \mathbf{S C 1}$ for $y=3$ indicated <br> Must check line - not if wrong line B2 for $y=1-x$ ruled correctly <br> or SC1 for ruled line with either gradient -1 or $y$-intercept 1 but not line $\mathrm{y}=1$ or correct freehand line |


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\begin{tabular}{|c|c|c|c|c|}
\hline Qu \& \& Answers \& Mark \& Part Marks <br>
\hline \& (e)

(f) \& tangent ruled at $x=2$ and

$$
0.62 \text { to } 0.8
$$

\[
$$
\begin{aligned}
& \frac{1}{x^{2}}=-x \text { or } 1+x^{3}=0 \\
& 1=-x^{3} \text { or } x^{3}=-1 \\
& x=\sqrt[3]{-1}
\end{aligned}
$$

\] \& | M1 |
| :--- |
| M1 |
| A1 | \& | Accept integer/integer provided in range B1 for correct tangent drawn |
| :--- |
| and M1 for change in $y /$ change in $x$ dep on any tangent or close attempt at tangent at any point |
| Must see correct or implied calculation from a drawn tangent |
| dep M1 |
| dep $\mathbf{M 2}$ | <br>


\hline 5 \& | (a) (i) |
| :--- |
| (ii) |
| (b) (i) |
| (ii) | \& \[

$$
\begin{aligned}
& \binom{2}{4} \\
& 5.83 \text { to } 5.831 \\
& -2 \mathbf{p}+\mathbf{q} \text { oe } \\
& \overrightarrow{P S}=-\mathbf{p}+2 \mathbf{q} \text { or } \overrightarrow{S P}=\mathbf{p}-2 \mathbf{q} \\
& \overline{M S}=-\frac{2}{3} \mathbf{p}+\frac{4}{3} \mathbf{q} \text { seen } \\
& \text { or } \overrightarrow{S M}=\frac{2}{3} \mathbf{p}-\frac{4}{3} \mathbf{q} \text { seen } \\
& \text { or } \overrightarrow{R M}=\frac{2}{3}(-2 \mathbf{p}+\mathbf{q}) \text { soi } \\
& \text { or } \overrightarrow{M R}=\frac{2}{3}(2 \mathbf{p}-\mathbf{q}) \text { soi } \\
& \text { or } \overrightarrow{M Q}=\frac{1}{3}(-2 \mathbf{p}+\mathbf{q}) \text { soi } \\
& \text { or } \overrightarrow{Q M}=\frac{1}{3}(2 \mathbf{p}-\mathbf{q}) \text { soi } \\
& \overrightarrow{P M}=\mathbf{p}+\overrightarrow{R M} \\
& \text { or } \mathbf{p}-\overrightarrow{M R} \\
& \text { or }-\mathbf{p}+\mathbf{q}+\overrightarrow{Q M} \\
& \text { or }-\mathbf{p}+\mathbf{q}-\overrightarrow{M Q} \\
& {\left[=-\frac{1}{3} \mathbf{p}+\frac{2}{3} \mathbf{q}\right]}
\end{aligned}
$$

\] \& | 2 |
| :--- |
| 1 |
| B1 |
| B1 |
| M1 | \& | M1 for $3^{2}+5^{2}$ seen accept unsimplified |
| :--- |
| Any correct route for $\overrightarrow{P M}$ eg $\overrightarrow{P R}+\overrightarrow{R M}$ | <br>

\hline
\end{tabular}

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| Qu |  | Answers | Mark | Part Marks |
| :---: | :---: | :---: | :---: | :---: |
| 6 | (a) (i) <br> (ii) <br> (iii) <br> (b) <br> (c) | $\frac{1}{6}$ <br> $\frac{4}{6}$ oe <br> $\frac{2}{6}$ oe <br> $\frac{16}{36}$ oe $\frac{48}{360} \text { oe }$ | 1 <br> 1 <br> 3 | M2 $\frac{2}{6} \times \frac{4}{6}+\frac{4}{6} \times \frac{2}{6}$ only oe or M1 for one of $\frac{2}{6} \times \frac{4}{6}$ or $\frac{4}{6} \times \frac{2}{6}$ soi by $\frac{2}{9}$ M2 for $\frac{4}{6} \times \frac{3}{5} \times \frac{2}{4} \times \frac{2}{3}$ only oe or M1 for denominators 6, 5, 4, 3 soi in product of four fractions |
| 7 | (a) (i) <br> (ii) <br> (iii) <br> (iv) <br> (b) (i) <br> (ii) | 148 <br> 122 <br> 148 <br> 106 nfww <br> 63 <br> 54 | 2 <br> 1 <br> 3 <br> 2 <br> 2 | B1 for 58 seen at $A$ or 32 seen at $Y$ <br> B1 for [sum of interior angles =] 720 and M1 for $\frac{1}{2}\{($ their 720$)-(p+q+t+90)\}$ <br> B1 for angle $R P S=27$ or 90 at $P$ or at $S$ seen or stated <br> B1 for their $x$ or 63 or letter $x$ at $Q$ seen or state |


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| Qu |  | Answers | Mark | Part Marks |
| :---: | :---: | :---: | :---: | :---: |
| 8 | (a) (i) <br> (ii) <br> (b) | $\begin{aligned} & 7 \times 2+(2 x-3)(x+4)=2(x+4) \\ & 2 x^{2}+8 x-3 x-12 \text { or better seen } \\ & 2 x^{2}+3 x-6=0 \\ & \sqrt{(3)^{2}-4(2(-6))} \text { or better } \\ & p=-3 \text { and } r=2(2) \end{aligned}$ <br> 1.14 and -2.64 cao $\begin{aligned} & \pi \times x^{2}+\pi \times x \times 3 x \\ & 4[\pi] x^{2}=[\pi] r^{2} \\ & 2 x=r \end{aligned}$ | M1 <br> B1 <br> A1 <br> B1 <br> B1 <br> B1B1 <br> M2 <br> M1 <br> A1 | Allow if bracket[s] omitted but recovers <br> with no errors seen and brackets correctly expanded on both sides and no omission of brackets <br> or $\left(x+\frac{3}{4}\right)^{2}$ <br> Must see $\frac{p+\sqrt{q}}{r}$ or $\frac{p-\sqrt{q}}{r}$ or both $\text { Or }-\frac{3}{4}+\text { or }-\sqrt{\frac{57}{16}}$ <br> SC1 for 1.1 and - 2.6 final answer or 1.137 and -2.637 final answer or 1.14 and -2.64 seen in working or for -1.14 and 2.64 as final ans <br> or M1 for $\pi \times x \times 3 x$ <br> Dep on M2 <br> with no errors seen |
| 9 | (a) <br> (b) <br> (c) <br> (d) <br> (e) | 4-6x final answer $9 x-8$ final answer $\frac{1}{27}$ final answer $\frac{4-x}{3}$ oe final answer $\frac{4}{3}$ or $1 \frac{1}{3}$ or 1.33 or better | 1 <br> 2 <br> 3 <br> 2 <br> 3 | M1 for $4-3(4-3 x)$ seen <br> M2 for $3^{-3}$ soi by final answer $0.037037 \ldots$ to 3 sf or better or M1 for $[g(-1)=] 3$ soi <br> M1 for a correct first step $3 x=4-y$ oe or $x=4-3 y$ or $\frac{y}{3}=\frac{4}{3}-x$ <br> M2 for $3 x-4=0$ or better <br> or M1 for $3^{-(4-3 x)}$ |


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