



MATHEMATICS

0580/41

Paper 4 (Extended)

May/June 2016

MARK SCHEME

Maximum Mark: 130

Published

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Abbreviations

cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfww	not from wrong working
soi	seen or implied

Question	Answer	Mark	Part marks
1	(a) (i) 48	2	M1 for $\frac{72}{3}$
	(ii) 32.4[0]	1	
	(iii) $\frac{13}{30}$	2	M1 for $\frac{72 - \text{their(ii)} - 8.4}{72}$ oe
	(iv) 24	3	M2 for $\frac{19.2}{0.8}$ oe or M1 for recognising 19.2 is 80%
	(b) 660	3	M2 for $\frac{550 \times 2 \times 10}{100} + 550$ oe or M1 for $\frac{550 \times 2 \times 10}{100}$ oe
	(c) 663.9[0]	2	M1 for 550×1.019^{10} oe
	(d) 1.5[0]	3	M2 for $\sqrt[10]{\frac{638.3[0]}{550}}$ oe or M1 for $550 \times m^{10} = 638.3[0]$
2	(a) (i) Triangle drawn, vertices (2, -4), (2, -5), (4, -4)	2	SC1 for translation $\begin{pmatrix} 5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -2 \end{pmatrix}$ or correct points not joined
	(ii) Triangle drawn, vertices (-3, 4), (-3, 5), (-1, 4)	2	SC1 for reflection in line $y = k$ or line $x = 1$ or correct points not joined
	(iii) Enlargement	1	
	[factor] 3	1	
	[centre] (-6, -5)	1	
(b) (i) $\begin{pmatrix} 2 & 5 \\ 3 & 10 \end{pmatrix}$	1		

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Question	Answer	Mark	Part marks		
(ii)	$\begin{pmatrix} 10 & 14 \\ 18 & 24 \end{pmatrix}$ final answer	2	SC1 for one row or one column correct		
(iii)	$\frac{1}{4}$ oe	3	M2 for $1 \times 4 - 2 \times 3 = 4 \times k - 3 \times 1$ or better or B1 for $1 \times 4 - 2 \times 3$ or $4 \times k - 3 \times 1$ seen		
(c) (i)	Rotation	1			
	90° [anti-clockwise] oe	1			
	(0, 0) oe	1			
(ii)	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	2	SC1 for one correct row or column		
3	(a) (i)	400	B1 for 30 seen		
	(ii)	350			
	(iii)	70			
	(iv)	170			
	(b) (i)	Mid-values 40, 80, 125, 200 soi		M1	
		Σfx with correct frequencies and x 's in correct intervals or on boundaries of correct intervals		M1	
		$\div 200$		M1(dep)	
	(ii)	106 nfw		A1	SC2 for correct answer without working
		Correct histogram		4	B1 for correct widths and B1 for each rectangle of correct height at 0.8, 1.6, 1.6 (up to B3) After 0 scored, SC1 for 3 correct frequency densities seen
	(iii)	$\frac{10712}{39800}$ oe isw		2	M1 for $\frac{104}{200} \times \frac{103}{199}$ oe
4	(a)	14 137 to 14 137.2 or 14 139	2	M1 for $\frac{4}{3} \times \pi \times 15^3$	
	(b) (i)	104 000 or 103 600 to 103 700	3	M2 for $\pi \times 25^2 \times 60 - 14140$ or M1 for $\pi \times 25^2 \times 60$	

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Question	Answer	Mark	Part marks
(ii)	52.8 or 52.75 to 52.81...	2	M1 for <i>their</i> (b)(i) $\div (\pi \times 25^2)$ or $14\,140 \div (\pi \times 25^2)$
(c) (i)	15.8 or 15.81.....	3	M2 for $[r^2 =] \frac{14140}{\frac{1}{3} \times \pi \times 54}$ or M1 for $\frac{1}{3} \times \pi \times r^2 \times 54 = 14\,140$ oe
(ii)	3580 or 3576 to 3581 nfw	4	M1 for $(\textit{their} \text{ (c)(i)})^2 + 54^2$ M1 for $\pi \times (\textit{their} \text{ (c)(i)}) \times \sqrt{\{(\textit{their} \text{ (c)(i)})^2 + 54^2\}}$ M1 for $\pi \times (\textit{their} \text{ (c)(i)})^2$
5 (a)	9 10.5	1 1	
(b)	Fully correct curve	5	SC4 for correct curve, but branches joined B3 FT for 9 or 10 points plotted or B2 FT for 7 or 8 points plotted or B1 FT for 5 or 6 points plotted and B1 for two separate branches not touching or cutting y-axis
(c)	2.1 to 2.6	1	
	8.5 to 9	1	
(d)	2, 3, 5, 7	2	SC1 for correct 4 values and no more than one extra positive integer or $\pm 2, \pm 3, \pm 5, \pm 7$ or 3 correct values and no extras
(e)	(-2, -12)	1	
(f) (i)	$20 + x^2 = x^3$	M1	Multiplication by x
	$x^3 - x^2 - 20 = 0$	A1	No errors or omissions
(ii)	Fully correct curve $y = x^2$	2	SC1 for U – shaped parabola, vertex at origin
(iii)	2.5 to 3.5	1	
(iv)	3.[0] to 3.1 or FT their answer to (iii)	1FT	FT dep on (iii) > 0

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Question	Answer	Mark	Part marks	
6	(a) (i)	$[y =] \frac{1}{2}(80 - 2x)$	M1	40 - x is enough
		$A = \text{their } \frac{1}{2}(80 - 2x) \times x$ oe	M1	
	(ii)	$A = 40x - x^2$ and $x^2 - 40x + A = 0$	A1	No errors or omissions
		$(x - 30)(x - 10)$	B2	B1 for $x(x - 30) - 10(x - 30) [= 0]$ or $x(x - 10) - 30(x - 10) [= 0]$ or SC1 for $(x + a)(x + b)$ where $ab = 300$ or $a + b = -40$
	(iii)	30, 10	B1	
		$\sqrt{(-40)^2 - 4(1)(200)}$ or better	B1	or for $(x - 20)^2$
		$p = -40$ and $r = 2(1)$	B1	Must see $\frac{p + \sqrt{q}}{r}$ or $\frac{p - \sqrt{q}}{r}$ or both or for $20 \pm \sqrt{200}$
	(b) (i)	5.86 34.14	B1 B1	If B0, SC1 for 5.9 or 5.857 to 5.858 and 34.1 or 34.14... or 5.86 and 34.14 seen in working or -5.86 and -34.14 as final answers
		$\frac{200}{x} - \frac{200}{x + 10}$ $\frac{200(x + 10) - 200x}{x(x + 10)} = \frac{2000}{x(x + 10)}$	M2 A1	or M1 for $\frac{200}{x}$ or $\frac{200}{x + 10}$ soi No errors or omissions
	(b) (ii)	16 [min] 40 [s]	3	B2 for $0.2\dot{7}$ or 0.278 or 0.2777 to 0.2778 or $\frac{5}{18}$ [h] oe or $16.\dot{6}$ or 16.7 or 16.66 to 16.67 or $\frac{50}{3}$ [min] or M1 for $2000 \div 80(80 + 10)$ or $\frac{200}{80} - \frac{200}{90}$

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Question	Answer	Mark	Part marks	
7	(a) (i)	$\frac{1}{2}\mathbf{p}$	1	
	(ii)	$\frac{1}{2}\mathbf{p} - \frac{1}{3}\mathbf{r}$	1	
	(iii)	$\mathbf{p} + \frac{2}{3}\mathbf{r}$	1	
	(b)	$\mathbf{r} + \frac{3}{2}\mathbf{p}$	2	
	(c)	6 nfww	3	
8	(a)	2	2	M1 for $2x + 1 = 1 + 4$
	(b)	17	2	B1 for $[h(3) =] 8 \text{ soi or } 2 \times 2^x + 1 \text{ oe}$
	(c)	$\frac{x-1}{2}$ oe final answer	2	M1 for $y-1 = 2x$ or $\frac{y}{2} = x + \frac{1}{2}$ or $x = 2y + 1$
	(d)	$4x^2 + 4x + 5$ final answer	3	M1 for $(2x+1)^2 + 4$ and B1 for $[(2x+1)^2 =] 4x^2 + 2x + 2x + 1$ or better
	(e)	$\sqrt{2}$ or 1.41 or 1.414....	1	
	(f)	-1	1	
9	(a) (i)	$-\frac{1}{2}x + 2$ oe	3	SC2 for $y = -\frac{1}{2}x + c$ oe or SC1 for $y = kx + 2$ oe, $k \neq 0$ or M1 for [gradient =] $\frac{-2}{4}$ and M1 for substituting (4, 0) or (0, 2) into $y = (\text{their } m)x + c$
	(ii)	$\frac{16}{a^2} \left[+ \frac{0^{[2]}}{b^2} \right] = 1$ or $\frac{4^2}{a^2} \left[+ \frac{0^{[2]}}{b^2} \right] = 1$ and $a^{[2]} = 4^{[2]}$ $\left[\frac{0^{[2]}}{a^2} \right] + \frac{4}{b^2} = 1$ or $\left[\frac{0^{[2]}}{a^2} \right] + \frac{2^2}{b^2} = 1$ and $b^{[2]} = 2^{[2]}$	1 1	

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Question	Answer	Mark	Part marks
(b) (i)	1.73 or 1.732.. or $\sqrt{3}$	3	M2 for $\frac{k^2}{4} = \frac{3}{4}$ or better or M1 for $\frac{2^2}{16} + \frac{k^2}{4} = 1$ oe
(ii)	81.8 or 81.78 to 81.79	3	M2 for $2 \times \tan^{-1}\left(\frac{\text{their}\sqrt{3}}{2}\right)$ oe or M1 for $\tan = \frac{\text{their}\sqrt{3}}{2}$ oe
(c) (i)	8π final answer	1	
(ii)	72π final answer	2FT	FT <i>their</i> (c)(i) $\times 9$ in terms of π M1 for area factor of 3^2 or 9 or [new a] = 12, [new b] = 6