Cambridge International Examinations<br>Cambridge International General Certificate of Secondary Education

MATHEMATICS
0580/43
Paper 4 (Extended)
May/June 2016
MARK SCHEME
Maximum Mark: 130

## Published

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Abbreviations
cao correct answer only
dep dependent
FT follow through after error
isw ignore subsequent working
oe or equivalent
SC Special Case
nfww not from wrong working
soi seen or implied

| Question | Answer | Mark | Part marks |
| :---: | :---: | :---: | :---: |
| 1 <br> (a) <br> (i) <br> (ii) <br> (b) <br> (c) | 36600 <br> $16 \frac{2}{3}$ or 16.7 [16.66 to 16.67 ] <br> 1231708 final answer nfww <br> 27.2[0] nfww | 5 | M2 for $6100 \div 2 \times(2+7+3)$ oe or M1 for $6100 \div 2$ soi <br> M4 for $5964 \times 15+28400 \times 35+8236 \times 18$ or M3 for $5964 \times 15$ and $28400 \times 35$ or for $5964 \times 15+42600 \times$ their decimal $\frac{2}{3}$ $\times 35+(42600-5964-42600 \times$ their decimal $\left.\frac{2}{3}\right) \times 18$ <br> or M2 for $5964 \times 15$ or $28400 \times 35$ or for $42600 \times$ their decimal $\frac{2}{3} \times 35$ or M1 for $0.14 \times 42600$ or $42600 \div 3 \times 2$ M2 for $23.80 \div 0.7$ oe or M1 for 23.80 associated with $70 \%$ oe and M2 for their $(23.80 \div 0.7) \times 0.8$ or M1 for their $(23.80 \div 0.7) \times 0.2$ |
| 2 (a) <br> (b) (i) <br> (ii) | $x>\frac{12}{5}$ oe final answer $(y-6)(x+3)$ final answer $8(x+3 y)(x-3 y)$ final answer | $2$ | B1 for $\frac{12}{5}$ oe in answer with incorrect or no sign <br> or M1 for one correct step e.g. $5 x>9+3$ <br> M1 for $y(x+3)-6(3+x)$ <br> or $x(y-6)+3(y-6)$ <br> M2 for $2(2 x+6 y)(2 x-6 y)$ or <br> $(8 x+24 y)(x-3 y)$ or $(8 x-24 y)(x+3 y)$ <br> or $4(2 x-6 y)(x+3 y)$ or $4(2 x+6 y)(x-3 y)$ <br> or $(4 x-12 y)(2 x+6 y)$ or $(4 x+12 y)(2 x-6 y)$ <br> or M1 for $8\left(x^{2}-9 y^{2}\right)$ or $(x+3 y)(x-3 y)$ |


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| Question | Answer | Mark | Part marks |
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| (c) | $r=\frac{1}{p+7}$ final answer nfww | 4 | M1 removes fraction correctly <br> M1 collects terms in $r$ <br> M1 removes $r$ as a factor from their terms in $r$ <br> M1dep divides by bracket to leave $r$ and denominator simplified |
| (iii) <br> (b) (i) <br> (ii) <br> (iii) <br> (c) <br> (d) | 10 <br> -3.4 to -3.3 and -0.4 to -0.3 and 1.6 to 1.7 $\begin{aligned} & y=-2.3 \text { to }-2.1 \mathrm{oe} \\ & y=10 \text { to } 10.1 \mathrm{oe} \end{aligned}$ $2,-1,4$ <br> Fully correct curve drawn <br> -3.4 to -3.2 and 1.8 to 1.9 <br> 3.2 oe <br> 1 | 3 <br> 2 <br> 3 <br> 4 <br> 2 <br> 2FT | B1 for each <br> B1 for each <br> B1 for each <br> SC3 for correct curves but branches joined or touching $y$-axis <br> or B2FT for 8 or 9 correct plots or B1FT for 6 or 7 correct plots <br> and B1 indep for two separate branches not touching or crossing $y$ - axis <br> B1 for each <br> FT $2 \div$ their (a)(i) +3 <br> M1 for $\mathrm{f}(-2)=10$ or their (a)(i) used |
| 4 (a) (i) <br> (ii) <br> (b) | $\begin{aligned} & 0.0025 \text { or } \frac{1}{400} \text { oe } \\ & 0.9975 \text { or } \frac{399}{400} \text { oe } \\ & 0.171 \text { or } 0.1714 \text { to } 0.1715 \text { or } \frac{6859}{40000} \end{aligned}$ | 1FT | M1 for $0.05^{2}$ oe <br> FT for 1 - (their (a)(i)) oe <br> M2 for $4\left(0.05 \times 0.95^{3}\right)$ oe <br> M1 for $0.05 \times 0.95^{3}$ oe seen or for the 4 combinations correctly identified |


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| Question | Answer | Mark | Part marks |
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| (c) <br> (d) (i) <br> (ii) | 376 nfww <br> 16 <br> 33 | $2$ | M1 for midpoints soi (condone 1 error or omission) $(225,275,325,375,425,475)$ <br> and <br> M1 for use of $\Sigma f x$ with $x$ in correct interval including both boundaries (condone 1 further error or omission) <br> and <br> M1 (dependent on second M) for $\Sigma f x \div 200$ <br> M1 for $0.8 \times 50+0.26 \times 100$ |
| $5 \quad \text { (a) } \quad \text { (i) }$ <br> (ii) <br> (b) <br> (c) | 275 <br> 095 <br> 464.66 to 464.67 [ $=464.7$ ] <br> 44.9 or 44.86 to $44.87 \ldots$ | 2FT <br> 4 <br> 3 | M1 for 360-40-45 oe <br> FT their (a) - 180 <br> M1 for their (a) - 180 oe or $180-40-45$ <br> M2 for $510^{2}+720^{2}-2 \times 510 \times 720 \cos 40$ <br> or M1 for correct implicit equation <br> A1 for 215900 to 215920 <br> M2 for $\frac{510 \sin (40)}{464.7}$ <br> or M1 for correct implicit equation |
| 6 <br> (a) (i) <br> (ii) <br> (iii) <br> (iv) <br> (b) (i) <br> (ii) | Correct image $(2,-5)(4,-5)(4,-1)$ <br> Correct image $(-2,1)(-6,1)(-6,-1)$ <br> Translation by $\binom{1}{9}$ <br> Enlargement <br> [SF] - $1 / 2$ oe <br> [Centre] $(2,1)$ $\left(\begin{array}{cc} -1 & 0 \\ 0 & 1 \end{array}\right)$ <br> Reflection $x=0 \mathrm{oe}$ | 2 <br> 2 <br> 1 1 1 <br> 2 <br> 1 | SC1 for reflection in $y=0$ or 3 correct points not joined <br> SC1 for rotation 90 clockwise any centre or 3 correct points not joined <br> B1 for each <br> B1 for one correct row or column but not the identity matrix |


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| Question | Answer | Mark | Part marks |
| :---: | :---: | :---: | :---: |
| 7 (a) (i) | $\frac{12}{x-1}-\frac{10}{x}=0.5 \mathrm{oe}$ <br> $12 x-10(x-1)=0.5 x(x-1)$ or better <br> Brackets expanded <br> $x^{2}-5 x-20=0$ with no errors or omissions seen | M2 <br> M1 <br> A1 | M1 for $\frac{12}{x-1}$ or $\frac{10}{x}$ <br> FT $\frac{10}{x}-\frac{12}{x-1}=0.5$ only <br> Dep on M3 and brackets expanded |
| (ii) <br> (iii) <br> (b) (i) <br> (ii) | $\sqrt{(-5)^{2}-4(1)(-20)}$ or better $p=-(-5), r=2(1)$ or better $-2.62,7.62$ final answers 1 [ hr] 49 [mins] 2.5 1312.5 final answer | B1 <br> B1 <br> B1B1 <br> 2FT <br> 1 <br> 3 | Seen anywhere or $\left(x-\frac{5}{2}\right)^{2}$ oe <br> Must be in the form $\frac{p+\sqrt{q}}{r}$ or $\frac{p-\sqrt{q}}{r}$ <br> or for $\frac{5}{2}+\sqrt{\left(\frac{5}{2}\right)^{2}+20}$ or $\frac{5}{2}-\sqrt{\left(\frac{5}{2}\right)^{2}+20}$ <br> SC1 for -2.6 or -2.623 to -2.624 and 7.6 or 7.623 to 7.624 or -2.62 and 7.62 seen in working or answers 2.62 and - 7.62 <br> FT $12 \div($ their + ve root -1$)$ or $0.5+10 \div($ their 7.62$)$ in hrs and mins, rounded to nearest min <br> M1 for $12 \div($ their + ve root -1$)$ <br> or $0.5+10 \div$ (their 7.62 ) <br> M2 for any complete correct method e.g $25 \times 10 \div 2+45 \times 25+5 \times 25 \div 2$ <br> M1 for any correct method for a relevant area under the graph |
| 8 <br> (a) <br> (i) <br> (ii) <br> (iii) <br> (iv) <br> (v) | Not possible <br> $\left(\begin{array}{cc}4 & 0 \\ -2 & 10 \\ 6 & -8\end{array}\right)$ final answer <br> $\left(\begin{array}{cc}14 & 35 \\ -8 & -20\end{array}\right)$ final answer <br> (-6) final answer <br> $\left(\begin{array}{ll}-2 & 18 \\ -6 & 22\end{array}\right)$ final answer | $2$ | M1 for one correct column or row <br> M1 for $14-20$ <br> M1 for one correct column or row |


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| Question | Answer | Mark | Part marks |
| :---: | :---: | :---: | :---: |
| (b) | $\frac{1}{8}\left(\begin{array}{cc}5 & -3 \\ 1 & 1\end{array}\right)$ or better isw | 2 | B1 for $k\left(\begin{array}{cc}5 & -3 \\ 1 & 1\end{array}\right)$ seen or implied, $k \neq 0$ or $\frac{1}{8}\left(\begin{array}{ll}a & b \\ c & d\end{array}\right)$ seen |
| 9 (a) <br> (b) | 270 or 270.17 to 270.22 <br> 518 or 517.6 to 517.8 nfww | $3$ <br> 6 | M2 for $\frac{360-145}{360} \times \pi 12^{2}$ oe or B1 for 215 seen or M1 for $\frac{\theta}{360} \times \pi 12^{2}$ used <br> B4 for vertical height $=9.62$ to 9.63 <br> or $\mathbf{B 3}$ for radius $=7.166$ to 7.17 <br> or B2 for length of sector $=45$.[0] or 45.02 to 45.04 <br> or M1 for $\frac{360-145}{360} \times 2 \times \pi \times 12$ oe <br> or for $\sqrt{12^{2}-\text { their radius }^{2}}$ <br> and M1 indep for $\frac{1}{3} \pi \times \text { their radius }{ }^{2} \times \text { their } h$ <br> $(h \neq 12$ or $r \neq 12)$ |
| 10 (a) <br> (b) (i) <br> (ii) <br> (c) | $10 \quad 15$ <br> 1521 <br> 3548 <br> 3 <br> 143 <br> $a=\frac{1}{2}$ oe $b=\frac{3}{2}$ oe nfww | 2 <br> 1FT <br> 5 | B1 for each correct entry <br> M1 for any correct substitution in $n^{2}+4 n+p$ $=$ number of tiles eg $2^{2}+4(2)+p=15$ <br> FT $140+$ their (b)(i) <br> B1 for a correct simplified equation e.g. $a+b+1=3,4 a+2 b+1=6$, $9 a+3 b+1=10$ etc <br> B1 for a $2^{\text {nd }}$ correct simplified equation <br> M1 for correctly eliminating one variable for their equations in $a$ and $b$ <br> A1 for $a=\frac{1}{2}$ nfww <br> A1 for $b=\frac{3}{2}$ nfww |


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| Question | Answer | Mark | Part marks |
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| (d) (i) | 171 | 2FT | FT their $a \times 17^{2}+$ their $b \times 17+1$ <br> M1 for their $a \times 17^{2}+$ their $b \times 17+1$ |
| (ii) | 673 | 1FT | FT their (d)(i) $\times 4-11$ |


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