CANDIDATE NAME



MATHEMATICS
0580/22
Paper 2 (Extended)
May/June 2013
1 hour 30 minutes
Candidates answer on the Question Paper.
Additional Materials: Electronic calculator Geometrical instruments Tracing paper (optional)

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
DO NOT WRITE IN ANY BARCODES.
Answer all questions.
If working is needed for any question it must be shown below that question.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For $\pi$, use either your calculator value or 3.142.
At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 70 .

1 Shade the required region on each Venn diagram.


2 Factorise completely.

$$
k p+3 k+m p+3 m
$$

3 The first five terms of a sequence are shown below.

$$
\begin{array}{lllll}
13 & 9 & 5 & 1 & -3
\end{array}
$$

Find the $n$th term of this sequence.

4 Calculate $\left(4.3 \times 10^{8}\right)+\left(2.5 \times 10^{7}\right)$.
Give your answer in standard form.

5


NOT TO
SCALE

Triangle $A B C$ has a height of 8 cm and an area of $42 \mathrm{~cm}^{2}$.

Calculate the length of $B C$.

6 George and his friend Jane buy copies of the same book on the internet.
George pays $\$ 16.95$ and Jane pays $£ 11.99$ on a day when the exchange rate is $\$ 1=£ 0.626$.
Calculate, in dollars, how much more Jane pays.
Answer \$

7 (a) Use your calculator to work out $\sqrt{65}-1.7^{2}$.
Write down all the numbers displayed on your calculator.

> Answer(a)
(b) Write your answer to part (a) correct to 2 significant figures.
Answer(b)

8 Joe measures the side of a square correct to 1 decimal place.
He calculates the upper bound for the area of the square as $37.8225 \mathrm{~cm}^{2}$.
Work out Joe's measurement for the side of the square.

9 A car, 4.4 metres long, has a fuel tank which holds 65 litres of fuel when full.
The fuel tank of a mathematically similar model of the car holds 0.05 litres of fuel when full.
Calculate the length of the model car in centimetres.

10


NOT TO
SCALE
$A, B, C, D$ and $E$ are points on a circle.
Angle $A B D=58^{\circ}$, angle $B A E=85^{\circ}$ and angle $B D C=19^{\circ}$.
$B D$ and $C A$ intersect at $N$.
Calculate
(a) angle $B D E$,
(b) angle $A N D$.

11 Without using a calculator, work out $\frac{6}{7} \div 1 \frac{2}{3}$.
Write down all the steps in your working.

12 Solve the equation.

$$
5(2 y-17)=60
$$

Answer $y=$

13 Carol invests $\$ 6250$ at a rate of $2 \%$ per year compound interest.
Calculate the total amount Carol has after 3 years.
$14 y$ is inversely proportional to $x^{3}$. $y=5$ when $x=2$.

Find $y$ when $x=4$.

Answer $y=$

15 Use the quadratic equation formula to solve

$$
2 x^{2}+7 x-3=0
$$

Show all your working and give your answers correct to 2 decimal places.
$\qquad$ or $x=$

16


The diagram shows the speed-time graph of a train journey between two stations.

The train accelerates for 3 minutes, travels at a constant maximum speed of $40 \mathrm{~km} / \mathrm{h}$, then takes 4 minutes to slow to a stop.

Calculate the distance in kilometres between the two stations.

17 The owner of a small café records the average air temperature and the number of hot drinks he sells each day for a week.

| Air temperature $\left({ }^{\circ} \mathrm{C}\right)$ | 18 | 23 | 19 | 23 | 24 | 25 | 20 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of hot drinks sold | 12 | 8 | 13 | 10 | 9 | 7 | 12 |

(a) On the grid, draw a scatter diagram to show this information.

(b) What type of correlation does your scatter diagram show?

Answer(b)
(c) Draw a line of best fit on the grid.

18 Solve $6 x+3<x<3 x+9$ for integer values of $x$.


Scale: 1 cm to 8 m
The rectangle $A B C D$ is a scale drawing of a rectangular football pitch.
The scale used is 1 centimetre to represent 8 metres.
(a) Construct the locus of points 40 m from $A$ and inside the rectangle.
(b) Using a straight edge and compasses only, construct the perpendicular bisector of $D B$.
(c) Shade the region on the football pitch which is more than 40 m from $A$ and nearer to $D$ than to $B$.

20 The heights, in metres, of 200 trees in a park are measured.

| Height $(h \mathrm{~m})$ | $2<h \leqslant 6$ | $6<h \leqslant 10$ | $10<h \leqslant 13$ | $13<h \leqslant 17$ | $17<h \leqslant 19$ | $19<h \leqslant 20$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 23 | 47 | 45 | 38 | 32 | 15 |

(a) Find the interval which contains the median height.
Answer(a)
(b) Calculate an estimate of the mean height.

Answer(b) $\qquad$ m [4]
(c) Complete the cumulative frequency table for the information given in the table above.

| Height $(h \mathrm{~m})$ | $2<h \leqslant 6$ | $h \leqslant 10$ | $h \leqslant 13$ | $h \leqslant 17$ | $h \leqslant 19$ | $h \leqslant 20$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Cumulative <br> frequency | 23 |  |  |  |  |  |

Question 21 is printed on the next page.

$$
\mathrm{f}(x)=5 x+4
$$

$\mathrm{g}(x)=\frac{1}{2 x}, \quad x \sqcap 0$

$$
\mathrm{h}(x)=\left(\frac{1}{2}\right)^{x}
$$

Find
(a) $\operatorname{fg}(5)$,
(b) $\operatorname{gg}(x)$ in its simplest form,

$$
\begin{equation*}
\text { Answer }(b) \operatorname{gg}(x)= \tag{2}
\end{equation*}
$$

$\qquad$
(c) $\mathrm{f}^{-1}(x)$,

$$
\begin{equation*}
\operatorname{Answer}(c) \mathrm{f}^{-1}(x)= \tag{2}
\end{equation*}
$$

(d) the value of $x$ when $\mathrm{h}(x)=8$.

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