



Cambridge International AS & A Level

CANDIDATE
NAME

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CENTRE
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FURTHER MATHEMATICS

9231/04

Paper 4 Further Probability & Statistics

For examination from 2020

SPECIMEN PAPER

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **12** pages. Blank pages are indicated.

- 3 Employees at a particular company have been working seven hours each day, from 9 am to 4 pm. To try to reduce absence, the company decides to introduce 'flexi-time' and allow employees to work their seven hours each day at any time between 7 am and 9 pm. For a random sample of 10 employees, the numbers of hours of absence in the year before and the year after the introduction of flexi-time are given in the following table.

Employee	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>F</i>	<i>G</i>	<i>H</i>	<i>I</i>	<i>J</i>
Before	42	35	96	74	20	5	78	45	146	0
After	34	32	100	72	31	2	61	35	140	0

Test, at the 10% significance level, whether the population mean number of hours of absence has decreased following the introduction of flexi-time, stating any assumption that you make. [8]

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A series of horizontal dotted lines for writing.

- 4 The number, x , of a certain type of sea shell was counted at 60 randomly chosen sites, each one metre square, along the coastline in country A . The number, y , of the same type of sea shell was counted at 50 randomly chosen sites, each one metre square, along the coastline in country B . The results are summarised as follows, where \bar{x} and \bar{y} denote the sample means of x and y respectively.

$$\bar{x} = 29.2 \quad \Sigma(x - \bar{x})^2 = 4341.6 \quad \bar{y} = 24.4 \quad \Sigma(y - \bar{y})^2 = 3732.0$$

Find a 95% confidence interval for the difference between the mean number of sea shells, per square metre, on the coastlines in country A and in country B . [7]

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5 The continuous random variable X has probability density function f given by

$$f(x) = \begin{cases} 0 & x < 0, \\ \frac{6}{5}x & 0 \leq x \leq 1, \\ \frac{6}{5}x^{-4} & x > 1. \end{cases}$$

(a) Find $P(X > 1)$. [1]

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(b) Find the median value of X . [2]

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The random variable Z is the total number of red balls selected by Aisha and Basant.

- (c) Find the probability generating function of Z , expressing your answer as a polynomial. [3]

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- (d) Use the probability generating function of Z to find $E(Z)$ and $\text{Var}(Z)$. [5]

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