Cambridge International AS Level

Cambridge International Examinations
Cambridge International Advanced Subsidiary Level

MATHEMATICS **9709/22**

Paper 2 **May/June 2017**

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2017 series for most Cambridge IGCSE®, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

  - Note: B2 or A2 means that the candidate can earn 2 or 0.
    B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking g equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
SOI	Seen or implied
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR –1	A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
PA –1	This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

Question	Answer	Marks	Guidance
1	State or imply non-modulus equation $(x+a)^2=(2x-5a)^2$ or pair of linear equations	**B1**	SR **B1** for $x=6a$
	Attempt solution of quadratic equation or of pair of linear equations	**M1**	Allow **M1** if $\frac{4}{3}$ and 6 seen
	Obtain, as final answers, $6a$ and $\frac{4}{3}a$	**A1**	
	Total:	**3**	
2	Apply logarithms to both sides and apply power law	***M1**	
	Obtain $(x+4)\log 3 = 2x\log 5$ or equivalent	**A1**	
	Solve linear equation for x	**DM1**	dep *M
	Obtain 2.07	**A1**	Allow greater accuracy
	Total:	**4**	
3(i)	Draw sketch of $y=x^3$	***B1**	May be implied by part graph in first quadrant
	Draw straight line with negative gradient crossing positive y-axis and indicate one intersection	**DB1**	dep *B
	Total:	**2**	
3(ii)	Use iterative formula correctly at least once	**M1**	
	Obtain final answer 1.926	**A1**	
	Show sufficient iterations to justify 4 sf or show sign change in interval $(1.9255, 1.9265)$	**A1**	
	Total:	**3**	

Question	Answer	Marks	Guidance
4	Use quotient rule (or product rule) to find first derivative	**M1**	
	Obtain $\dfrac{8xe^{4x}+10e^{4x}}{(2x+3)^2}$ or equivalent	**A1**	
	Substitute $x=0$ to obtain gradient $\frac{10}{9}$	**A1**	
	Form equation of tangent through $\left(0,\frac{1}{3}\right)$ with numerical gradient	**M1**	
	Obtain $10x-9y+3=0$	**A1**	
	Total:	**5**	

Question	Answer	Marks	Guidance
5	State or imply $\ln y = \ln K - 2x\ln a$	**B1**	
	EITHER:		
	Obtain -0.525 as gradient of line	**(M1**	
	Equate their $-2\ln a$ to their gradient and solve for a	**M1**	Allow $2\ln a$ = their gradient for **M1**
	Obtain $a = 1.3$	**A1**	
	Substitute to find value of K	**M1**	
	Obtain $K = 8.4$	**A1)**	
	OR:		
	Obtain two equations using coordinates correctly	**(M1**	
	Solve these equations to obtain $2\ln a$ or equivalent	**M1**	
	Obtain $a = 1.3$	**A1**	
	Substitute to find value of K	**M1**	
	Obtain $K = 8.4$	**A1)**	
	Total:	**6**	

Question	Answer	Marks	Guidance
6(i)	Evaluate expression when $x = -2$	**M1**	
	Obtain 0 with all necessary detail present	**A1**	Use of $\mathrm{f}(x) = (x+2)(ax^2+bx+c)$ to find a, b and c, allow **M1 A0** Use of $\mathrm{f}(x) = (x+2)(ax^2+bx+c)+d$ to find a, b and c, and show $d = 0$, allow **M1 A1**
	Carry out division, or equivalent, at least as far as x^2 and x terms in quotient	**M1**	
	Obtain $6x^2 + x - 35$	**A1**	
	Obtain factorised expression $(x+2)(2x+5)(3x-7)$	**A1**	
	Total:	**5**	
6(ii)	State or imply substitution $x = \frac{1}{y}$ or equivalent	**M1**	
	Obtain $-\frac{1}{2},\ -\frac{2}{5},\ \frac{3}{7}$	**A1**	
	Total:	**2**	
7(a)	Obtain $\int(2\cos^2\theta - \cos\theta - 3)\,\mathrm{d}\theta$	**B1**	
	Attempt use of identity to obtain integrand involving $\cos 2\theta$ and $\cos\theta$	**M1**	
	Integrate to obtain form $k_1 \sin 2\theta + k_2 \sin\theta + k_3\theta$ for non-zero constants	**M1**	
	Obtain $\frac{1}{2}\sin 2\theta - \sin\theta - 2\theta + c$	**A1**	
	Total:	**4**	

Question	Answer	Marks	Guidance
7(b)(i)	Integrate to obtain form $k_1\ln(2x+1)+k_2\ln(x)$ or $k_1\ln(2x+1)+k_2\ln(2x)$	M1	
	Obtain $2\ln(2x+1)+\frac{1}{2}\ln x$ or $2\ln(2x+1)+\frac{1}{2}\ln(2x)$	A1	
	Total:	**2**	
7(b)(ii)	Use relevant logarithm power law for expression obtained from application of limits	M1	
	Use relevant logarithm addition / subtraction laws	M1	
	Obtain $\ln 18$	A1	
	Total:	**3**	
8(i)	Obtain $\frac{dx}{dt}=2\sin 2t$	B1	
	Obtain $\frac{dy}{dt}=6\sin^2 t\cos t-9\cos^2 t\sin t$	B1	
	Use $\dfrac{dy}{dx}=\dfrac{dy}{dt}/\dfrac{dx}{dt}$ for their first derivatives	M1	
	Use identity $\sin 2t=2\sin t\cos t$	B1	
	Simplify to obtain $\frac{3}{2}\sin t-\frac{9}{4}\cos t$ with necessary detail present	A1	
	Total:	**5**	

Question	Answer	Marks	Guidance
8(ii)	Equate $\frac{dy}{dx}$ to zero and obtain $\tan t = k$	M1	
	Obtain $\tan t = \frac{3}{2}$ or equivalent	A1	
	Substitute value of t to obtain coordinates $(2.38,\ 2.66)$	A1	
	Total:	**3**	
8(iii)	Identify $t = \frac{1}{4}\pi$	B1	
	Substitute to obtain exact value for gradient of the normal	M1	
	Obtain gradient $\frac{4}{3}\sqrt{2}$, $\dfrac{8}{3\sqrt{2}}$ or similarly simplified exact equivalent	A1	
	Total:	**3**	