## ADDITIONAL MATHEMATICS

0606/22
Paper 22
March 2017
MARK SCHEME
Maximum Mark: 80

## Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

## Types of mark

M Method marks, awarded for a valid method applied to the problem.
A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.

B Mark for a correct result or statement independent of Method marks.
When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

## Abbreviations

awrt answers which round to
cao correct answer only
dep dependent
FT follow through after error
isw ignore subsequent working
nfww not from wrong working
oe or equivalent
rot rounded or truncated
SC Special Case
soi seen or implied
www without wrong working

| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1 | $-\frac{5}{3}$ isw <br> Solve $5-3 x=-10$ or $(5-3 x)^{2}=100$ $x=5$ | B1 <br> M1 <br> A1 | or exact equivalent |
| 2 (i) <br> (ii) | $\$ 12000$ <br> $\frac{8000}{12000}=\mathrm{e}^{-0.2 t} \quad$ oe $[t=] 2(.0273 \ldots) \text { years }$ | B1 <br> M1 <br> A1 |  |


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| :---: | :---: | :---: | :---: |
| 3 (i) <br> (ii) | multiply out correctly <br> Finding another factor <br> Either $(x-1)^{2}\left(x^{2}-4\right)$ <br> Or $(x-1)(x+2)\left(x^{2}-3 x+2\right)$ <br> Or $(x-1)(x-2)\left(x^{2}+x-2\right)$ <br> Attempts to factorise quadratic $(x-1)^{2}(x+2)(x-2) \text { oe }$ | B1 <br> B1 <br> B1 <br> M1 <br> A1 | or divide out correctly <br> $(x-1)$ or $(x+2)$ or $(x-2)$; method must be seen <br> For stating a relevant quadratic factor for their linear factors <br> mark final answer <br> Alternative method: <br> B1 for finding a second linear factor using any valid method and <br> B1 for finding a third linear factor using any valid method and <br> B1 for finding the final linear factor using any valid method and <br> B1 for fully correct product stated; mark final answer <br> If fully correct product stated but no method shown then <br> B1 only. |
| 4 | Eliminates $y$ $3 x+k=2 x^{2}-3 x+4$ <br> Collects terms $2 x^{2}-6 x+4-k=0 \text { soi }$ <br> Applies $b^{2}-4 a c$ $(-6)^{2}-4(2)(4-k)$ or better $k<-\frac{1}{2}$ oe | A1 <br> M1 <br> A1 | Alternative calculus method: Equates gradients $4 x-3=3$ <br> Finds point of tangency $(1.5,4)$ <br> Substitutes into $y=3 x+k$ $4=3(1.5)+k$ |


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| 5 | $\sqrt{20}=\sqrt{4 \times 5}=2 \sqrt{5} \text { seen }$ $(3+\sqrt{5}) x+\frac{1}{2} x(\text { their } 2 \sqrt{5})=13+5 \sqrt{5} \text { oe }$ leading to $(3+$ their $2 \sqrt{5}) x=13+5 \sqrt{5}$ $[x=] \frac{13+5 \sqrt{5}}{3+\text { their } 2 \sqrt{5}} \times \frac{3-\text { their } 2 \sqrt{5}}{3-\text { their } 2 \sqrt{5}}$ $[x=] \frac{39-26 \sqrt{5}+15 \sqrt{5}-50}{9-20}$ $1+\sqrt{5} \mathrm{www}$ | B1 <br> M1 <br> M1 <br> M1 <br> A1 | may be later in working; must be convinced that calculator has not been used <br> equates their area to given area and factorises to collect $x$ terms; may still have $\sqrt{20}$ <br> divides and attempts to rationalise; may still have $\sqrt{20}$ <br> or forms a pair of simultaneous equations e.g. $3 p+10 q=13 \quad 2 p+3 q=5$ <br> numerator must have at least 3 terms; denominator may be -11 <br> or solves their simultaneous equations to find one unknown <br> or $p=1, q=1$ |
| (i) <br> (ii) <br> (b) <br> (i) <br> (ii) | $-2 x^{\frac{5}{2}}$ oe or $a=-2$ and $b=\frac{5}{2}$ oe <br> $[x=]\left(\frac{-6250}{\text { their }(-2)}\right)^{\text {their } \frac{2}{5}}$ oe <br> 25 <br> Valid explanation $1=\log _{a} a$ <br> $2 \log _{a}(4 x-3)=\log _{a}(4 x-3)^{2}$ soi completion to given result | B2 <br> M1 <br> A1 <br> B1 <br> M1 <br> M1 <br> A1 | mark final answer <br> B1 for -2 and B1 for $\frac{5}{2}$ <br> may be in steps <br> e.g. If $x>0.75$ then all the arguments are positive as required. oe <br> may be seen in e.g. $\log _{a}(a x)=1+\log x$ |


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| (iii) | $x^{2}(16 x-24)=0$ oe or $x(16 x-24)=0$ oe $[x=] \frac{24}{16}$ or $\frac{3}{2}$ oe | M1 <br> A1 | e.g. equates, anti-logs, rearranges and factorises or divides OR rearranges, combines using correct log law, anti-logs and factorises or divides <br> inclusion of $x=0$ is $\mathbf{A 0}$ |
| $7 \quad$ (a) <br> (b) | $\left[r^{2}=\right] 5^{2}+10^{2}-2 \times 5 \times 10 \times \cos 120 \mathrm{oe}$ <br> [ $r=$ ] 13.2 or 13.22875.... rot to 4 or more sf <br> $\frac{\sin x}{5}=\frac{\sin 120}{\text { their } 13.2}$ or better <br> [ $x=$ ] awrt 19.1 <br> 360-120-their $x$ <br> $94[\mathrm{~km} / \mathrm{h}]$ west | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ \text { A1FT } \\ \hline \text { B2 } \end{gathered}$ | or for $\left[r^{2}=\right] 5^{2}+10^{2}-2 \times 5 \times 10 \times \cos 60^{\circ}$ or for $\left[r^{2}=\right] 5^{2}+10^{2}-2 \times 5 \times 10 \times \cos 240^{\circ}$ not from wrong working <br> or $\frac{\sin y}{10}=\frac{\sin 120}{\text { their } 13.2}$ or better or [ $y=$ ] awrt 40.9 <br> or $180+$ their $y$ <br> B1 for $94[\mathrm{~km} / \mathrm{h}]$ |
| 8 (i) | $\begin{aligned} & y-(-4)=\frac{1}{6}(x-6) \\ & {\left[m_{A B}=\right] \frac{7-4}{3-8} \text { or }-\frac{3}{5} \text { oe }} \\ & y-7=-\frac{3}{5}(x-3) \text { or } y-4=-\frac{3}{5}(x-8) \\ & \text { their }\left(\frac{1}{6} x-5\right)=\text { their }\left(-\frac{3}{5} x+\frac{44}{5}\right) \\ & x=18 \\ & y=-2 \text { isw } \end{aligned}$ | B1 <br> M1 <br> A1 <br> M1 <br> A1 <br> A1 | or $y=\frac{1}{6} x+c$ and $c=-5$ <br> or $y=-\frac{3}{5} x+c$ and $c=\frac{44}{5}$ <br> valid method of solution for their equations; must be of equivalent difficulty |


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| (ii) | $[m=]-\frac{3}{2}$ <br> $y-$ their $(-2)=-\frac{3}{2}(x-$ their 18$)$ isw | M1 <br> A1FT | FT their $D ; y=-\frac{3}{2} x+c$ and $c=$ their 25 |
| $9 \quad$ (a) <br> (b) (i) <br> (ii) | $\begin{aligned} & k \mathrm{e}^{2 x+1}(+c) \\ & k=\frac{1}{2} \\ & \frac{\mathrm{~d}(\ln x)}{\mathrm{d} x}=\frac{1}{x} \text { soi } \\ & {\left[\frac{\mathrm{d} y}{\mathrm{~d} x}=\right] \frac{(\text { their } 1) \ln x-x\left(\text { their } \frac{1}{x}\right)}{(\ln x)^{2}}} \end{aligned}$ <br> correct, isw $\begin{aligned} & \int \frac{\ln x-1}{(\ln x)^{2}} \mathrm{~d} x+\int \frac{1}{x^{2}} \mathrm{~d} x=\frac{x}{\ln x}+\int \frac{1}{x^{2}} \mathrm{~d} x \\ & \int \frac{1}{x^{2}} \mathrm{~d} x=-\frac{1}{x}(+c) \\ & \frac{x}{\ln x}+\left(\text { their }-\frac{1}{x}\right)(+c) \end{aligned}$ | M1 <br> A1 <br> B1 <br> M1 <br> A1 <br> M1 <br> B1 <br> A1FT | for some non-zero integer $k$ where $k \neq 2$ <br> correct form of quotient rule or equivalent product rule applied; brackets may be omitted or misplaced for M1 <br> may be unsimplified; allow recovery of brackets <br> rearranges and uses their answer to (i) <br> correct or correct FT completion; their $-\frac{1}{x}$ must not be $\frac{1}{x^{2}}$ |


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| 10 <br> (i) <br> (ii) | $\begin{aligned} & \tan (2 x-10)=\frac{4}{3} \\ & 2 x-10=\tan ^{-1}\left(\frac{4}{3}\right) \text { soi } \end{aligned}$ <br> 31.6 and 121.6 isw <br> 211.6 and 301.6 isw $\begin{aligned} & 1-\cos ^{2} x-\cos ^{2} x=\cos x \\ & 2 \cos ^{2} x+\cos x-1=0 \text { oe } \\ & (2 \cos x-1)(\cos x+1)[=0] \\ & {[x=] 60,300,180} \end{aligned}$ | B1 <br> M1 <br> A1 <br> A1 <br> M1 <br> A1 <br> M1 <br> A2 | or for 31.6 and 211.6 isw or for 121.6 and 301.6 isw <br> Penalty of 1 mark if all 4 angles given correctly but prematurely approximated OR if any extra angles are given besides the correct 4 <br> If A0 A0 then allow SC1 for 53.1(30...), 233.1(30...), 413.1(30...), 593.1(30...) seen OR for 63.1(30...), 243.1(30...), 423.1(30...), 603.1(30...) seen uses $\sin ^{2} x=1-\cos ^{2} x$ <br> factorises or solves their 3-term quadratic in $\cos x$ <br> A1 for any two correct |
| 11 (i) <br> (ii) <br> (iii) | $\begin{aligned} & g \geqslant-\frac{1}{2} \\ & g(1)=0 \end{aligned}$ <br> valid comment e.g. domain of f is $x \geqslant 2$ $\begin{aligned} & \frac{\left(\frac{x^{2}-2}{x}\right)^{2}-1}{2} \\ & \left(\frac{x^{2}-2}{x}\right)^{2}=\frac{x^{4}-4 x^{2}+4}{x^{2}} \text { soi } \\ & \frac{1}{2} x^{2}-\frac{5}{2}+\frac{2}{x^{2}} \end{aligned}$ | B1 <br> B1 <br> B1 <br> M1 <br> B1 <br> A1 | B1 for either <br> or $\frac{\left(x-\frac{2}{x}\right)^{2}-1}{2}$ <br> or $\left(x-\frac{2}{x}\right)^{2}=x^{2}-4+\frac{4}{x^{2}}$ <br> or correct 3 term equivalent or $a=0.5, b=-2.5, c=2$ |


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| (iv) <br> (v) | $x \geqslant 2$ $x^{2}-y x-2=0$ $[x=] \frac{-(-y) \pm \sqrt{(-y)^{2}-4(1)(-2)}}{2}$ <br> Explains why negative square root should be discarded $\mathrm{f}^{-1}(x)=\frac{x+\sqrt{x^{2}+8}}{2}$ | B1 <br> B1 <br> M1 <br> B1 <br> A1 | or $y^{2}-x y-2=0$ <br> or $[y=] \frac{-(-x) \pm \sqrt{(-x)^{2}-4(1)(-2)}}{2}$ <br> at some point <br> allow $y=\frac{x+\sqrt{x^{2}+8}}{2}$ <br> If zero scored, allow SC2 for showing correctly that the inverse of the given $\mathrm{f}^{-1}$ is $f$. |
| 12 (i) <br> (ii) | $\begin{aligned} & {[\text { length of rectangle }=] \frac{20-3 x}{2}} \\ & {[A=] x \times \text { their } \frac{20-3 x}{2}-\frac{1}{2} \times x \times x \times \sin 60 \text { oe }} \end{aligned}$ <br> Correct completion to given answer $\begin{aligned} & A=10 x-\left(\frac{6+\sqrt{3}}{4}\right) x^{2} \\ & 10-2\left(\frac{6+\sqrt{3}}{4}\right) x \text { oe } \\ & \text { their }\left(10-2\left(\frac{6+\sqrt{3}}{4}\right) x\right)=0 \text { oe } \\ & x=2.6 \\ & A=13 \end{aligned}$ | B1 <br> M1 <br> A1 <br> B1 <br> M1 <br> A1 <br> A1 | allow 2.586635... rot to 3 or more sf allow $12.9331 \ldots$... rot to 3 or more sf |

