

#### ADDITIONAL MATHEMATICS

0606/11 May/June 2017

Paper 1 MARK SCHEME Maximum Mark: 80

Published

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### MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

#### **Types of mark**

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

#### Abbreviations

answers which round to awrt correct answer only cao dep dependent follow through after error FT ignore subsequent working isw not from wrong working nfww or equivalent oe rounded or truncated rot Special Case SC seen or implied soi

Question	Answer	Marks	Guidance
1(i)	$kx - 5 = x^{2} + 4x$ $x^{2} + (4 - k)x + 5 = 0$	M1	equating line and curve equation and collecting terms to form an equation of the form $ax^2 + bx + c = 0$ x terms must be gathered together, maybe implied by later work
	For a tangent $(4-k)^2 = 20$	DM1	correct use of discriminant
	$k = 4 + 2\sqrt{5}$	A1	Accept $k = 4 + \sqrt{20}$
	Alternative		
	Gradient of line = k Gradient of curve = $\frac{dy}{dx} = 2x + 4$ Equating: $k = 2x + 4$	M1	
	substitution of $k = 2x + 4$ or $x = \frac{k - 4}{2}$ in $kx - 5 = x^2 + 4$ and simplify to a quadratic equation in k or x	DM1	
	$k = 4 + 2\sqrt{5}$	A1	Accept $k = 4 + \sqrt{20}$
1(ii)	Normal gradient = $-\frac{1}{4+2\sqrt{5}} \times \frac{4-2\sqrt{5}}{4-2\sqrt{5}}$	M1	use of negative reciprocal and attempt to rationalise using a form of $a - b\sqrt{5}$ or $a - \sqrt{20}$ or <i>their</i> equivalent from (i)
	$= -\frac{4 - 2\sqrt{5}}{-4}$ oe $= 1 - \frac{\sqrt{5}}{2}$	A1	$-\frac{4-2\sqrt{5}}{-4}$ oe leading to $1-\frac{\sqrt{5}}{2}$
2	p(3) = 27 + 9a + 3b - 48	M1	attempt to find p(3)
	3a+b=9 oe	A1	
	$p'(x) = 3x^2 + 2ax + b$ p'(1) = 3 + 2a + b	M1	attempt to differentiate and find $p'(1)$ must have 2 terms correct
	2a + b = -3 oe	A1	
	a = 12, b = -27	A1	for both
3(a)	$x^3y^7$	B2	B1 for each term

#### 0606/11

Question	Answer	Marks	Guidance
3(b)(i)	for $(t-2)^{\frac{3}{2}} = (t-2)^{\frac{1}{2}}(t-2)$ soi	M1	
	$(t-2)^{\frac{1}{2}}(4+5(t-2))$	A1	
	$(t-2)^{\frac{1}{2}}(5t-6)$	A1	
3(b)(ii)	2 and $\frac{6}{5}$	B1	<b>FT</b> on <i>their</i> $(t-2)^{\frac{1}{2}}(5t-6)$ , must have 2
4(a)(i)	f > 5, f(x) > 5	B1	
4(a)(ii)	$\frac{y-5}{3} = e^{-4x}$ or $\frac{x-5}{3} = e^{-4y}$	B1	
	$-4x = \ln\left(\frac{y-5}{3}\right) \text{ or } -4y = \ln\left(\frac{x-5}{3}\right)$	B1	
	leading to $f^{-1}(x) = -\frac{1}{4} ln \left( \frac{x-5}{3} \right)$	B1	
	or $f^{-1}(x) = \frac{1}{4} \ln \left( \frac{3}{x-5} \right)$		
	or $f^{-1}(x) = \frac{1}{4}(\ln 3 - \ln(x-5))$		
	or $f^{-1}(x) = -\frac{1}{4}(\ln(x-5) - \ln 3)$		
	Domain $x > 5$	B1	
4(b)	$\ln\left(x^2+5\right)=2$	B1	
	$x^2 + 5 = e^2$	B1	
	$x = 1.55$ or better or $\sqrt{e^2 - 5}$	B1	
5(a)(i)	$\overrightarrow{OM} = \overrightarrow{OC} + \frac{1}{2} \left( \overrightarrow{OA} - \overrightarrow{OC} \right)$ oe	M1	may be implied by correct answer.
	$\frac{1}{2}(\mathbf{a}+\mathbf{c})$	A1	

Question	Answer	Marks	Guidance
5(a)(ii)	$\mathbf{b} = \frac{5}{2} \overline{OM} \text{ oe }, \frac{5}{2} (their (i))$ or $\overline{OM} = \frac{2}{3} (\mathbf{b} - \overline{OM})$	M1	dealing with ratio correctly to relate <b>b</b> or $\overrightarrow{OB}$ to $\overrightarrow{OM}$
	$=\frac{5}{4}(\mathbf{a}+\mathbf{c})$	A1	
5(b)(i)	$ -10\mathbf{i} + 24\mathbf{j}  = 26$ $\mathbf{p} = \frac{39}{26}(-10\mathbf{i} + 24\mathbf{j})$	M1	magnitude of $-10\mathbf{i} + 24\mathbf{j}$ and use with 39
	$\mathbf{p} = -15\mathbf{i} + 36\mathbf{j}$	A1	
5(b)(ii)	If parallel to the <i>y</i> -axis, <b>i</b> component is zero	M1	realising i component is zero
	so $2\mathbf{p} + \mathbf{q} = 12\mathbf{j}$	DM1	use of 12
	$\mathbf{q} = 30\mathbf{i} - 60\mathbf{j}$	A1	
5(b)(iii)	$ \mathbf{q}  = 30\sqrt{1^2 + (-2)^2} \text{ or } \sqrt{900} \times \sqrt{5}$	M1	attempt at magnitude of <i>their</i> <b>q</b>
	$ \mathbf{q}  = 30\sqrt{5}$	A1	Answer Given: must have full and correct working
6(i)	$\frac{1}{2} \times 12^2 \times \theta = 150$	M1	use of sector area
	$\theta = 2.083$ , so $\theta = 2.08$ to 2dp	A1	
6(ii)	Area of triangle $AOB = \frac{1}{2} \times 12^2 \sin 2.08$	M1	correct method for area of triangle
	Area of segment = $150 - \frac{1}{2} \times 12^2 \times \sin 2.08$	A1	allow unsimplified, using $\theta = 2.08, \ 2.083 \text{ or } \frac{150}{72}$
	$\sin 1.04 = \frac{\frac{AB}{2}}{12}$	M1	correct trigonometric statement using $\theta = 2.08$ , 2.083 or $\frac{150}{72}$ with attempt to obtain <i>AB</i>
	AB = awrt 20.7	A1	
	Shaded area = <i>their</i> $AB \times 8 - their$ segment area	M1	execution of a correct 'plan'(rectangle – segment)
	awrt 78.4 or 78.5	A1	

#### 0606/11

Question	Answer	Marks	Guidance
6(iii)	Arc $AB = 25$ or 24.96	B1	
	Perimeter = $25 + their AB + 16$	M1	correct 'plan' ( arc + <i>their</i> $AB$ + 2×8)
	awrt 61.7	A1	
7	differentiation to obtain answer in the form	M1	
	$p(3x^2+8)^{\frac{2}{3}}$ or $qx(3x^2+8)^{\frac{2}{3}}$		
	$6x\left(3x^2+8\right)^{\frac{2}{3}}$	B1	
	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{5}{3} \times 6x \left(3x^2 + 8\right)^{\frac{2}{3}}$	A1	all correct
	When $\frac{dy}{dx} = 0$ only solution is $x = 0$	DM1	$qx(3x^2+8)^{\frac{2}{3}} = 0$ and attempt to solve
	$x = 0$ and $3x^2 + 8 = 0$ has no solutions	A1	
	Stationary point at (0,32)	A1	
	correct gradient method with substitution of $x$ values either side of zero or equivalent valid method	M1	
	correct conclusion from correct work using a correct $\frac{dy}{dx}$	A1	
8(i)		B5	<b>B1</b> for shape of modulus function <b>B1</b> for <i>y</i> intercept = 5 (for modulus graph only) <b>B1</b> for <i>x</i> intercept = 2.5 at the V of a modulus graph <b>B1</b> for shape of quadratic function for $-1 \le x \le 6$ <b>B1</b> for intercepts at <i>x</i> = 0 and <i>x</i> = 5 for a quadratic graph
8(ii)	$2x - 5 = \pm 4$	B1	one correct answer
	$x = \frac{9}{2}$	M1	solution of two different correct linear equations or solution of an equation obtained from squaring both sides or use of symmetry from first solution.
	$x = \frac{1}{2}$	A1	second correct solution

Question	Answer	Marks	Guidance
8(iii)	$16\left(\frac{1}{2}\right)^{2} - 80\left(\frac{1}{2}\right) + 36 = 4$	B1	verification using both x values or for forming and solving $16x^2 - 80x + 36 = 0$
	and $16\left(\frac{9}{2}\right)^2 - 80\left(\frac{9}{2}\right) + 36 = 4$		
8(iv)	using <i>their</i> values from (ii) in an equality of the form $a \le x \le b$ or $a < x < b$	M1	
	$\frac{1}{2} \leqslant x \leqslant \frac{9}{2}  \text{cao}$	A1	
9(i)	$5+4\left(\sec^2\left(\frac{x}{3}\right)-1\right)$ leading to given answer	B1	use of correct identity
9(ii)	$3\tan\left(\frac{x}{3}\right)$ (+c)	B1	
9(iii)	attempt to integrate using (i) and/or (ii)	M1	
	Area = $\int_{\frac{\pi}{2}}^{\pi} 4\sec^2\left(\frac{x}{3}\right) + 1  dx$	A1	all correct
	$\left[12\tan\left(\frac{x}{3}\right) + x\right]_{\frac{\pi}{2}}^{\pi}$	DM1	correct method for evaluation using limits in correct order
	$=\left(12\tan\frac{\pi}{3}+\pi\right)-\left(12\tan\frac{\pi}{6}+\frac{\pi}{2}\right)$	A1	
	$=8\sqrt{3}+\frac{\pi}{2}$	A1	
10(a)	differentiation of a quotient or equivalent product	M1	
	correct differentiation of $e^{3x}$	B1	
	$\frac{dy}{dx} = \frac{3e^{3x}(4x^2+1) - 8xe^{3x}}{(4x^2+1)^2}$	A1	everything else correct including brackets where needed, allow unsimplified
	or $\frac{dy}{dx} = \frac{3e^{3x}}{4x^2 + 1} - \frac{8xe^{3x}}{(4x^2 + 1)^2}$		

Question	Answer	Marks	Guidance
10(b)(i)	one term differentiated correctly	M1	
	$\frac{\mathrm{d}y}{\mathrm{d}x} = -4\sin\left(x + \frac{\pi}{3}\right) + 2\sqrt{3}\cos\left(x + \frac{\pi}{3}\right)$	A1	all correct
	When $x = \frac{\pi}{2}$ , $\frac{dy}{dx} = -5$	A1	
10(b)(ii)	$\frac{dy}{dx} \times \frac{dx}{dt} = \frac{dy}{dt}$ $-5 \times \frac{dx}{dt} = 10 \text{ oe}$	M1	correct use of rates of change
	$\frac{\mathrm{d}y}{\mathrm{d}t} = -2$	A1	FT answer to (i)