## MARK SCHEME for the October/November 2013 series

## 0606 ADDITIONAL MATHEMATICS

0606/12

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.



Page 2	Mark Scheme	Syllabus	Paper
	IGCSE – October/November 2013	0606	12

## Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √<sup>h</sup> implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously 'correct' answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
   B2, 1, 0 means that the candidate can earn anything from 0 to 2.

	Page 3	Page 3 Mark Scheme					Paper
		IGCSE – October/Nov	ober/November 2013			0606	12
1	a = 3, b = 2,	<i>c</i> = 1	B1, B1, B1	, [3]	B1 for	each	
2	Using $b^2 - 4ac$ $4k^2 + 8k -$	$f, 9 = 4 (k+1)^2 -5 = 0$	M1 DM1			any use of $b^2 - 4ac$ or solution of their of	quadratic in k
	$k=-\frac{5}{2},$	$\left(\frac{1}{2}\right)$	A1		A1 for	critical value(s), $\frac{1}{2}$	not necessary
	To be below th	the x-axis $k < -\frac{5}{2}$	A1	[4]	A1 for	$k < -\frac{5}{2}$ only	
	To lie under th	$x = \frac{3}{2(k+1)}$ $\frac{9}{(k+1)^2} - \frac{9}{2(k+1)} + (k+1)$	M1		M1 for	a complete method	to this point.
	(	$4(k+1)^2$ or equivalent					

Page 4	e 4 Mark Scheme				Syllabus	Paper
	IGCSE – October/Nov	ember 20	)13		0606	12
3 $\frac{1+\sin\theta}{\cos\theta} + \frac{\cos\theta}{1+\sin\theta} + \frac{(1+\sin\theta)^2 + \cos^2\theta}{\cos\theta(1+\sin\theta)}$ $= \frac{1+2\sin\theta + \sin^2\theta + \cos^2\theta}{\cos\theta(1+\sin\theta)}$		M1		M1 for dealing with the fractions denominator must be correct, be with numerator		
$=\frac{2+2}{\cos\theta(1)}$		DM1			expansion and use $+\sin^2\theta = 1$	e of
$=\frac{2(1+)}{\cos\theta(1+)}$	$\frac{\sin \theta}{+\sin \theta}$	DM1		M1 for	attempt to factori	se
$=2 \sec \theta$		A1 [	[4]	A1 for	obtaining final and	swer correctly
$= \frac{(\sec \theta + t)}{\sec \theta}$ $= \frac{\sec^2 \theta + t}{\sec^2 \theta}$ $= \frac{2 \sec^2 \theta}{\sec^2 \theta}$ $= \frac{2 \sec^2 \theta}{\sec^2 \theta}$	$\theta + \frac{1}{\sec \theta + \tan \theta}$ $\frac{\operatorname{an} \theta}{\operatorname{tan} \theta}^{2} + \frac{1}{\operatorname{tan} \theta}$ $\frac{2 \sec \theta \tan \theta + \tan^{2} \theta + 1}{\sec \theta + \tan \theta}$ $\frac{2 \sec \theta \tan \theta}{\operatorname{tan} \theta}$ $\frac{2 \sec \theta \tan \theta}{\theta + \tan \theta}$ $\operatorname{ec} \theta + \tan \theta$	M1 DM1 DM1		M1 for $\tan^2 \theta$	dealing with the f expansion and use $+1 = \sec^2 \theta$ or attempt to facto	e of
$\sec\theta$ $= 2\sec\theta$	$\theta + \tan \theta$	A1		A1 for	obtaining final an	swer correctly
<b>4</b> (i) n (A) = 3		B1 [	1]	correct $n(A) =$	ents listed for (i), elements to get B 3. If they are not given then B1.	
(ii) n ( <i>B</i> ) = 4		B1	1]	correct	elements leading hey are not listed	then they must be to $n(B) = 4$ to get and correct answer
(iii) $A \cup B = \{$	{60°, 240°, 300, 420°, 600°}	√B1	1]		through on any se not allow any rep	ets listed in (i) and betitions.
(iv) $A \cap B = \{$	{60°, 420°}	√B1 [1	1]	Follow (ii).	through on any se	ets listed in (i) and

Page 5	Mark Scheme	Mark Scheme			Paper
	IGCSE – October/Nove	mber 2013		0606	12
<b>5</b> (i) $9x - \frac{1}{3}co$	s3x(+c)	B1, B1, B1 [3]	B1 for	9x, B1 for $\frac{1}{3}$ or co $-\frac{1}{3}\cos 3x$ the omission of $+c$	os3 <i>x</i>
(ii) $\left[9x - \frac{1}{3}cc\right]$	9				
	$-\cos 3\pi \left( -\frac{1}{3}\cos \frac{\pi}{3} \right)$	M1	M1 for to (i)	correct use of limi	its in their answer
$=8\pi + \frac{1}{2}$		A1, A1 [3]	A1 for	each term	
$6 \qquad \mathbf{f}\left(\frac{1}{2}\right) = \frac{a}{8} + 1 + \frac{a}{8} + 1 + \frac{a}{8} + 1 + \frac{a}{8} + \frac{a}{8}$	$-\frac{b}{2}-2$	M1	M1 for	substitution of <i>x</i> =	$=\frac{1}{2}$ into f(x)
leading to $a +$	4b - 8 = 0	A1	A1 for	correct equation in	any form
f(2) = 2f(-1)		M1		attempt to substitution $f(x)$ and use $f(x) + f(-1)$	
8a + 16 + 2b -	2 = 2(-a + 4 - b - 2)	A1		a correct equation	in any form
leading to $10a$ $\therefore a = -2, b =$	+4b+10 = 0 or equivalent = $\frac{5}{2}$	DM1 A1 [6]	attemp obtain	on both previous M t to solve simultance either <i>a</i> or <i>b</i> both correct	

Pa	Page 6 Mark Scheme			Syllabus	Paper				
		IGCSE – October/Nove	mber 20	)13	0606	12			
7 (a) (b)	<ul> <li>(i) 360</li> <li>(ii) 120</li> <li>(i) 924</li> </ul>	)	B1	1] 1]					
(~)	(i) 22 (ii) 28		[ B1	1] 1]					
		$4 - ({}^{8}C_{3} \times {}^{4}C_{3}) - ({}^{8}C_{2} \times {}^{4}C_{4})$ 4 - 3M 3W - 2M 4W)	M1		t 3 terms, at least 2 t in terms of <i>C</i> nota				
	92 = 672	4 - 224 - 28	A1 A1 [		any pair (must be final answer	evaluated)			
Or:		${}^{8}C_{4} \times {}^{4}C_{2} = 420$	M1		M1 for 3 terms, at least 2 of which must be correct in terms of <i>C</i> notation or evaluated				
	5M 1W ${}^{8}C_{5} \times {}^{4}C_{1} = 224$ 6M ${}^{8}C_{6} = 28$				A1 for any pair (must be evaluated)				
		Total $= 672$	A1	A1 for	final answer				
8 (i)			B1 B1		correct shape (-3, 0) or -3 seen	on graph			
			B1		(2, 0) or 2 seen on				
			B1		(0, 6) or 6 seen on	graph or in a table			
(ii)	$\left(-\frac{1}{2}, \frac{25}{4}\right)$		B1, B1	4] B1 for 2]	each				
(iii)	$k > \frac{25}{4}$ or	$r \frac{25}{4} < k \ (\le 14)$	B1 [	1]					

	Page 7	Mark Scheme		Syllabus	Paper	
		IGCSE – October/Nove	mber 2013		0606	12
9	(a) $12x^2 \ln(2$	$(x+1) + 4x^3 \left(\frac{2}{2x+1}\right)$	M1 A2, 1, 0 [3]		differentiation of a each error	correct product
	<b>(b) (i)</b> $\frac{dy}{dx}$	$\frac{1}{x} = \frac{(x+2)^{\frac{1}{2}}2 - 2x(x+2)^{-\frac{1}{2}}\frac{1}{2}}{x+2}$	M1, A1		differentiation of a ng $(x+2)^{\frac{1}{2}}$	quotient
		$=\frac{(x+2)^{-\frac{1}{2}}}{(x+2)}(2(x+2)-x)$	DM1		correct unsimplified or attempt to simpli	
	=-	$\frac{x+4}{\left(x+2\right)^{\frac{3}{2}}}$	A1 [4]	A1 for given a	correct simplificationswer	on to obtain the
	<b>Or:</b> $\frac{\mathrm{d}y}{\mathrm{d}x} = 2x\left($	$\left(-\frac{1}{2}\right)(x+2)^{-\frac{3}{2}}+(x+2)^{-\frac{1}{2}}(2)$	M1, A1		differentiation of a ng $(x+2)^{-\frac{1}{2}}$	product
	= <u>x</u>	$(+2)^{-\frac{3}{2}}(2(x+2)-x) + \frac{4}{(x+2)^{\frac{3}{2}}}$	DM1 A1	DM1 f	correct unsimplified or attempt to simpli correct simplificationswer	fy
	(ii) $\frac{10x}{\sqrt{x+2}}$ (	(+c)	M1,A1 [2]	A1 cor	$\frac{1}{5} \times \frac{2x}{\sqrt{x+2}} \text{ or } 5 \times \frac{2x}{\sqrt{x+2}}$ rect only, allow unside the omission of $+c$	
	(iii) $\left[\frac{10x}{\sqrt{x+2}}\right]$	-	M1		correct application to (b)(ii)	of limits in their
		$=\frac{40}{3}$	A1 [2]			

Page 8	Mark Scheme			Syllabus	Paper
IGCSE – October/November 2013				0606	12
<b>10 (i)</b> $\sqrt{20}$ or 4	.47	B1 [1]			
(ii) Grad AB	$=\frac{1}{2}, \perp \text{grad} = -2$	M1	M1 for	attempt at a perp g	gradient
	y - 4 = -2(x - 1)	M1, A1		e attempt at straight e perpendicular and	<b>.</b> .
(y = -2x -	+ 6)	[3]		ow unsimplified	
$(x-1)^2 +$	(iii) Coords of $C(x, y)$ and $BC^2 = 20$ $(x-1)^2 + (y-4)^2 = 20$ or Coords of $C(x, y)$ and $AC^2 = 40$		M1 for attempt to obtain relationship using an appropriate length and the point $(1, 4)$ or (-3, 2)		
$(x+3)^2 +$	$(y-2)^2 = 40$	A1	A1 for a correct equation		
Need inte	ersection with $y = -2x + 6$ ,	DM1	DM1 for attempt to solve with $y = -2x + 6$ and obtain a quadratic equation in terms of one variable only		
leads to 5 $5y^2 - 40y$	$x^2 - 10x - 15 = 0$ or -= 0			Ĵ	
	giving $x = 3, -1$ and $y = 0, 8$		M1 for attempt to solve quadratic A1 for each 'pair'		
	ector approach:				
$\overrightarrow{AB} = \begin{pmatrix} 4\\2 \end{pmatrix}$		B1	May be implied		
$\overrightarrow{OC} = \begin{pmatrix} 1\\4 \end{pmatrix} + \begin{pmatrix} -2\\4 \end{pmatrix} = \begin{pmatrix} -1\\8 \end{pmatrix}$		M1 A1, A1		correct approach each element corre	ect
$\overrightarrow{OC} = \begin{pmatrix} 1 \\ 4 \end{pmatrix} +$	$\begin{pmatrix} 2 \\ -4 \end{pmatrix} = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$	A1,A1	A1 for	each element corre	ect

Page 9	Mark Schem	е		Syllabus	Paper
	IGCSE – October/Nove		0606	12	
<b>11 (a) (i)</b> $\begin{pmatrix} 4\\4 \end{pmatrix}$	$\begin{pmatrix} 3\\3 \end{pmatrix}$	B1 [1]			
(ii) A <sup>2</sup>	$\mathbf{P} = \begin{pmatrix} 16 & 9\\ 12 & 13 \end{pmatrix}$	B1, B1 [2]		nny 2 correct elemaill correct	ents
	s the inverse matrix of $\mathbf{A}^2$ $\frac{1}{00} \begin{pmatrix} 13 & -9 \\ -12 & 16 \end{pmatrix}$	√B1, √B1 [2]	Follow	through on their A	2
(b) det $\mathbf{C} = x_0$ = 2:	$(x-1) - (-1)(x^2 - x + 1)$ $x^2 - 2x + 1$	M1 A1	A1 for t	attempt to obtain o his correct quadra correct det C	
$b^2 - 4ac <$	< 0, 4 – 8 < 0	DM1	solve us complet	r use of discriminations using the formula, on the the square in ord eal roots.	or attempt to
No real so	blutions (so det $\mathbf{C} \neq 0$ )	A1 [4]		correct reasoning of e no real roots.	or statement that

	Pag	je 10				Syllabus	Paper		
			IGCSE – (	October/Novembe	er 2013	0606	12		
12	(a)	(i)	f(-10) = 299, f(8) = 19 Min point at (0, -1) or ∴ range $-1 \le y \le 299$	when $y = -1$ B1		M1 for substitution of either $x = -10$ or $x = 8$ , may be seen on diagram B1 May be implied from final answer, may be seen on diagram Must have $\leq$ for A1, do not allow x			
		(ii)	$x \ge 0$ or equivalent	B1	[3] [1]	<ul> <li>Must have \$\leq\$ for A1, do not allow x</li> <li>Allow any domain which will make f a one-one function</li> <li>Assume upper and lower bound when necessary.</li> <li>M1 for complete method to find the form inverse function, must involve ln or lg if appropriate. May still be in terms of y.</li> <li>A1 must be in terms of x</li> </ul>			
	<b>(b)</b>	(i)	$g^{-1}(x) = \ln\left(\frac{x+2}{4}\right)$ or $\frac{\lg\left(\frac{x+2}{4}\right)}{\lg e}$	M1 A1	[2]				
		(ii)	gh(x) = g(1n5x) = $4e^{1n5x} - 2$ 20x - 2 = 18, x = 1	M1 A1 A1	[3]	M1 for correct order A1 for correct expression A1 for correct solution fro working			
			<b>Or</b> $h(x) = g^{-1}(18)$ 1n5x = 1n5 leading to $x = 1$	M1 A1 A1		M1 for correct order A1 for correct equation A1 for correct solution <b>fr</b> <b>working</b>	om correct		