## MARK SCHEME for the October/November 2015 series

## 0606 ADDITIONAL MATHEMATICS

0606/12

Paper 1, maximum raw mark 80

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## Abbreviations

answers which round to
correct answer only
dependent
follow through after error
ignore subsequent working
or equivalent
rounded or truncated
Special Case
seen or implied
without wrong working

1	$kx^{2} + (2k - 8)x + k = 0$ $b^{2} - 4ac > 0 \text{ so } (2k - 8)^{2} - 4k^{2} (>0)$ $4k^{2} - 32k + 64 - 4k^{2} (>0)$	M1 DM1 DM1	for attempt to obtain a 3 term quadratic in the form $ax^2 + bx + c = 0$ , where b contains a term in k and a constant for use of $b^2 - 4ac$ for attempt to simplify and solve for k
	leading to $k < 2$ only	A1	A1 must have correct sign
2	$\left(\frac{dy}{dx}\right) = -5x(+c)$ When $x = -1$ , $\frac{dy}{dx} = 2$ leading to	M1	for attempt to integrate, do not penalise omission of arbitrary constant.
	$\frac{\mathrm{d}x}{\mathrm{d}x} = -5x - 3$	A1	Must have $\frac{dy}{dx} = \dots$
	$y = -\frac{5x^2}{2} - 3x + d$	DM1	for attempt to integrate <i>their</i> $\frac{dy}{dx}$ , but
	When $x = -1$ , $y = 3$ leading to		penalise omission of arbitrary constant.
	$y = \frac{5}{2} - \frac{5x^2}{2} - 3x$	A1	
	Alternative scheme:		
	$y = ax^{2} + bx + c \text{ so } \frac{dy}{dx} = 2ax + b$ When $x = -1$ , $\frac{dy}{dx} = 2$	M1	for use of $y = ax^2 + bx + c$ , differentiation and use of conditions to give an equation in <i>a</i> and <i>b</i>
	$\int_{a}^{b} dx$	A1	for a correct equation
	$\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} = 2a$	DM1	for a second differentiation to obtain <i>a</i>
	so $a = -\frac{5}{2}$ , $b = -3$ , $c = \frac{5}{2}$	A1	for <i>a</i> , <i>b</i> and <i>c</i> all correct

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3	$\sqrt{(\sec^2 \theta - 1)} + \sqrt{(\csc^2 \theta - 1)} = \sec \theta \csc \theta$		
	$LHS = \tan\theta + \cot\theta$	B1	may be implied by the next line
	$=\frac{\sin\theta}{\cos\theta}+\frac{\cos\theta}{\sin\theta}$	B1	for dealing with $\tan \theta$ and $\cot \theta$ in terms of
			$\sin \theta$ and $\cos \theta$
	$=\frac{\sin^2\theta + \cos^2\theta}{\sin\theta\cos\theta}$	M1	for attempt to obtain as a single fraction
	$=\frac{1}{\sin\theta\cos\theta}$	M1	for the use of $\sin^2 \theta + \cos^2 \theta = 1$ in correct
	$\sin\theta\cos\theta$		context
	$= \sec\theta\csc\theta$	A1	Must be convinced as AG
	Alternate scheme:		
	$LHS = \tan\theta + \cot\theta$		
	$= \tan \theta + \frac{1}{\tan \theta}$	B1	may be implied by subsequent work
	$=\frac{\tan^2\theta+1}{\tan\theta}$	M1	for attempt to obtain as a single fraction
		1011	for attempt to obtain as a single fraction
	$=\frac{\sec^2\theta}{\tan\theta}$	B1	for use of the correct identity
	$=\frac{\sec\theta}{\tan\theta}\times\sec\theta$	M1	for 'splitting' sec <sup>2</sup> $\theta$
	$\tan \theta = \csc \theta \sec \theta$		
	- cosee see s	A1	Must be convinced as AG
4 (a) (i)	28	B1	
(ii)	20160	B1	
(iii)	$6 \times (5 \times 4 \times 3)$ oe to give 360 $6 \times (5 \times 4 \times 3) \times 2$	B1	for realising that the music books can be arranged amongst themselves and consideration of the other 5 books
	= 720	B1	for the realisation that the above arrangement can be either side of the clock.
(b)	Either ${}^{10}C_6 - {}^7C_6 = 210 - 7$	B1, B1	B1 for ${}^{10}C_6$ , B1 for ${}^7C_6$
	= 203	B1	
	Or $1W  5M = 63$	B1	for 1 case correct, must be considering more
	2W 4M = 105		than 1 different case, allow C notation
	3W 3M = 35 Total = 203	B1 B1	for the other 2 cases, allow <i>C</i> notation for final result
	10001 200	51	

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5	(i)	$\frac{dy}{dx} = (x-3)\frac{4x}{2x^2+1} + \ln(2x^2+1)$	B1	for correct differentiation of ln function
			M1	for attempt to differentiate a product
		when $x = 2$ , $\frac{dy}{dx} = -\frac{8}{9} + \ln 9$ oe	A1	for correct product, terms must be bracketed where appropriate
		or 1.31 or better	A1	for correct final answer
(	ii)	$\partial y \approx$ (answer to (i)) × 0.03	M1	for attempt to use small changes
		= 0.0393, allow awrt 0.039	A1FT	follow through on <i>their</i> numerical answer to (i) allow to 2 sf or better
6	(i)	$A \cap B = \{3\}$	B1	
(	ii)	$A \cup C = \{1, 3, 5, 6, 7, 9, 11, 12\}$	B1	
(i	ii)	$A' \cap C = \{1, 5, 7, 11\}$	B1	
(i	v)	$(D \cup B)' = \{1, 9\}$	B1	
(	<b>(v)</b>	Any set containing up to 5 positive even numbers $\leq 12$	B1	
7	(i)	Gradient = $\frac{0.2}{0.8} = 0.25$	M1	for attempt to find the gradient
		b.8 b = 0.25	A1	
		Either $6 = 0.25(2.2) + c$ Or $5.8 = 0.25(1.4) + c$	M1	for a correct substitution of values from either point and attempt to obtain <i>c</i> or
		leading to $A = 233$ or $e^{5.45}$	A1	solution by simultaneous equations dealing with $c = \ln A$
		Alternative schemes:		
		Either Or $(22)^{b}$		
		$6 = b(2.2) + c \qquad e^{6} = A(e^{2.2})^{b}$ $5.8 = b(1.4) + c \qquad e^{5.8} = A(e^{1.4})^{b}$	M1	for 2 simultaneous equations as shown
			DM1	for attempt to solve to get at least one
		Leading to $A = 233$ or $e^{5.45}$ and $b = 0.25$	A1, A1	solution for one unknown A1 for each
(	ii)	Either $y = 233 \times 5^{0.25}$	M1	for correct use of either equation in attempt
		Or $\ln y = 0.25 \ln 5 + \ln 233$		to obtain y using <i>their</i> value of A and of $\vec{b}$ found in (i)
		leading to $y = 348$	A1	

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	1		1
8	$\frac{dy}{dx} = \frac{2(x^2+5)^{\frac{1}{2}} - \frac{1}{2}(2x)(x^2+5)^{-\frac{1}{2}}(2x-1)}{x^2+5}$ or $\frac{dy}{dx} = 2(x^2+5)^{-\frac{1}{2}} - \frac{1}{2}(2x)(x^2+5)^{-\frac{3}{2}}(2x-1)$	B1 M1 A1	for $\frac{1}{2}(2x)(x^2+5)^{-\frac{1}{2}}$ for a quotient or $-\frac{1}{2}(2x)(x^2+5)^{-\frac{3}{2}}$ for a product allow if either seen in separate working for attempt to differentiate a quotient or a <b>correct</b> product for all correct, allow unsimplified
	When $x = 2$ , $y = 1$ and $\frac{dy}{dx} = \frac{4}{9}$ (allow 0.444 or 0.44)	B1, B1	B1 for each
	Equation of tangent: $y - 1 = \frac{4}{9}(x - 2)$ (9y = 4x + 1)	M1 A1	for attempt at straight line, must be tangent using <i>their</i> gradient and y allow unsimplified.
9 (i)	$\frac{2}{3}(4+x)^{\frac{3}{2}}(+c)$	B1,B1	B1 for $k(4+x)^{\frac{3}{2}}$ only, B1 for $\frac{2}{3}(4+x)^{\frac{3}{2}}$ only
(ii)	Area of trapezium = $\left(\frac{1}{2} \times 5 \times 5\right)$	M1	Condone omission of $c$ for attempt to find the area of the trapezium
	= 12.5 Area = $\left[\frac{2}{3}(4+x)^{\frac{3}{2}}\right]_{0}^{5} - \left(\frac{1}{2} \times 5 \times 5\right)$	A1 M1	for correct use of limits using $k(4+x)^{\frac{3}{2}}$ only
	$= \left(\frac{2}{3} \times 27\right) - \frac{16}{3} - \frac{25}{2}$	A1	(must be using 5 and 0) for $18 - \frac{16}{3}$ or equivalent
	$=\frac{1}{6}$ or awrt 0.17	A1	
	Alternative scheme: Equation of <i>AB</i> $y = \frac{1}{5}x + 2$	M1	for a correct attempt to find the equation of $AB$
	Area = $\int_{0}^{\delta} \sqrt{4 + x} - \left(\frac{1}{5}x + 2\right) dx$ = $\left[\frac{2}{3}(4 + x)^{\frac{3}{2}} - \frac{x^{2}}{10} - 2x\right]_{0}^{\delta}$	M1	for correct use of limits using $k(4+x)^{\frac{3}{2}}$ only (must be using 5 and 0)
	$= \left(\frac{2}{3} \times 27\right) - \frac{16}{3} - \frac{25}{2}$ $= \frac{1}{6} \text{ or awrt } 0.17$	A1 A1 A1	for $18 - \frac{16}{3}$ or equivalent for 12.5 or equivalent

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10 (i)		All sides are equal to the radii of the circles which are also equal	B1	for a convincing	g argument	
(ii)		Angle $CBE = \frac{2\pi}{3}$	B1	must be in terms of $\pi$ , allow 0.667 $\pi$ , or better		
(iii)		$DE = 10\sqrt{3}$	M1	for correct attempt to find <i>DE</i> using <i>their</i> angle <i>CBE</i>		
			A1	for correct $DE$ ,	allow 17.3 of	r better
		Arc $CE = 10 \times \frac{2\pi}{3}$	M1	for attempt to find $CBE$ (20.94)	nd arc length	with <i>their</i> angle
		Perimeter = $20 + 10\sqrt{3} + \frac{20\pi}{3}$	M1	for $10 + 10 + D$	E + an arc le	ngth
		= 58.3  or  58.2	A1	allow unsimpli	fied	
(iv)		Area of sector: $\frac{1}{2} \times 10^2 \times \frac{2\pi}{3} = \frac{100\pi}{3}$	M1	for sector area unsimplified, m	-	-
		Area of triangle: $\frac{1}{2} \times 10^2 \times \sin \frac{2\pi}{3} = 25\sqrt{3}$	M1	for triangle area must be the sam unsimplified, m	ne as <i>their</i> an	
		Area $=\frac{100\pi}{3} + 25\sqrt{3}$ or awrt 148	A1	allow in either t	form	

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11 (a) (i)	$(x+3)^2-5$	B1, B1	B1 for 3, B1 for – 5
(ii)	$y \ge 4 \text{ or } f \ge 4$	B1	Correct notation or statement must be used
(iii)	$y = \sqrt{x+5} - 3$	M1	for a correct attempt to find the inverse function
	Domain $x \ge 4$	A1 B1FT	must be in the correct form and positive root only Follow through on <i>their</i> answer to (ii), must be using x
(b)	$h^2g(x) = h^2(e^x)$	M1	for correct order
	$=h(5e^x+2)$	M1	for dealing with $h^2$
	$=25e^{x}+12$		
	$25e^x + 12 = 37,$	DM1	for solution of equation (dependent on both previous M marks)
	leading to $x = 0$	A1	
	Alternative scheme 1:		
	$hg(x) = h^{-1}(37)$	M1	for correct order
	$h^{-1}(37) = 7$	M1	for dealing with $h^{-1}(37)$
	$5e^x + 2 = 7,$	DM1	for solution of equation (dependent on both
	leading to $x = 0$	A1	previous M marks)
	Alternative scheme 2:		
	$g(x) = h^{-2}(37)$	M1	for correct order
	$h^{-2}(37) = 1$	M1	for dealing with $h^{-2}(37)$
	$e^x = 1,$	DM1	for solution of equation (dependent on both
	leading to $x = 0$	A1	previous M marks)

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12		2. ( 1( 0 2. 10 75 0	<b>M</b> 1	Construction of the international structure in		
12		$x^{2} + 6x - 16 = 0$ or $y^{2} + 10y - 75 = 0$ leading to	M1	for attempt to obtain a 3 term quadratic in terms of one variable only		
		(x+8)(x-2) = 0 or $(y-5)(y+15) = 0$	DM1	for attempt to solve quadratic equation		
		so $x = 2, y = 5$ and $x = -8, y = -15$	A1, A1	A1 for each 'pair' of values.		
		Midpoint $(-3, -5)$	B1			
		Gradient = 2, so perpendicular gradient = $-\frac{1}{2}$				
		Perpendicular bisector:				
		$y + 5 = -\frac{1}{2}(x + 3)$	M1	for attempt at straight line equation, must be		
		(2y + x + 13 = 0)		using midpoint and perpendicular gradient		
		Point <i>C</i> (-13, 0)	M1	for use of $y = 0$ in <i>their</i> line equation (but not $2x - y + 1 = 0$ )		
		Area $=\frac{1}{2}\begin{vmatrix} -13 & 2 & -8 & -13 \\ 0 & 5 & -15 & 0 \end{vmatrix}$	M1	for correct attempt to find area, may be using <i>their</i> values for <i>A</i> , <i>B</i> and <i>C</i> ( <i>C</i> must lie on the		
		=125	A1	<i>x</i> -axis)		
		Alternative method for area:				
		$CM^2 = 125, \ AB^2 = 500$	M1	for correct attempt to find area may be using		
		Area $=\frac{1}{2} \times \sqrt{125} \times \sqrt{500}$		<i>their</i> values for <i>A</i> , <i>B</i> and <i>C</i>		
		= 125	A1			