ADDITIONAL MATHEMATICS	**0606/12**
Paper 1	**October/November 2016**
MARK SCHEME	
Maximum Mark: 80	

Published

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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question			Answer	Marks	Part Marks
1	(a)	(i)	10	B1	
		(ii)	22	B1	
		(iii)	4	B1	
	(b)	(i)	$Q \subset R$	B1	
		(ii)	$P \cap Q = \varnothing$, or { }	B1	
2			$a = 1, \ b = -3, \ c = -1$	B3	**B1** for each
3			$3y^2 + 5y - 2 = 0$	B1, B1	**B1** for $5y$ or $5\log_3 x$, **B1** for –2
			$y = \dfrac{1}{3}, \ y = -2$	M1	for correct attempt at the solution of *their* quadratic equation
			$x = 3^{\frac{1}{3}}, \ x = 3^{-2}$	M1	for dealing with one base 3 logarithm correctly
			$x = 1.44, \ x = \dfrac{1}{9}$	A1, A1	**A1** for each
4	(i)		$32x^{10} - \dfrac{80}{3}x^7 + \dfrac{80}{9}x^4$	B3	**B1** for each term, powers of x must be simplified
	(ii)		Coefficients needed: $\left(3 \times their -\dfrac{80}{3}\right) + \left(1 \times their \ 32\right)$	M1	for dealing with 2 terms
			$= -48$	A1	Allow **A1** for $-48x^7$

Question	Answer	Marks	Part Marks
5 **(i)**	$\dfrac{dy}{dx} = \dfrac{3}{2(3x+2)}$	**B1**	for correct derivative of log function
	When $x = -\dfrac{1}{3}$, $y = 0$, $\dfrac{dy}{dx} = \dfrac{3}{2}$	**B1**	for $y = 0$
	Equation of normal: $y = -\dfrac{2}{3}\left(x + \dfrac{1}{3}\right)$	**M1** **A1**	**M1** for attempt at a gradient of a perpendicular from differentiation and the equation of the normal
(ii)	$Q\left(0, -\dfrac{2}{9}\right)$ or $(0, 0.22)$ or better	**B1 ft**	Follow through on *their c* from part (i)
	$R\left(0, \dfrac{1}{2}\ln 2\right)$ or $(0, 0.35)$ or better	**B1**	
	Area of PQR $= \dfrac{1}{2}\left(\dfrac{1}{2}\ln 2 + \dfrac{2}{9}\right) \times \dfrac{1}{3}$ $= 0.0948$	**B1**	Allow 0.095
6 **(a)**	**YX**, **XZ**	**B2**	**B2** for both with no extras **B1** for 1 correct with or without extras **B1** for both correct with extras **B0** for anything else
(b) **(i)**	$\dfrac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$	**B1, B1**	**B1** for $\dfrac{1}{18}$, **B1** for $\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$
(ii)	$\mathbf{C} = \mathbf{A}^{-1}\mathbf{B}$ $= \dfrac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}\begin{pmatrix} -4 & 2 \\ 10 & 4 \end{pmatrix}$ $= \begin{pmatrix} -1 & 1 \\ 2 & 0 \end{pmatrix}$	**M1** **A1, A1**	for pre-multiplication **A1** for any correct pair of elements, but must be from correct matrices

Question	Answer	Marks	Part Marks
7 **(i)**	$\left(0,\sqrt{3}\right)$ or $\left(0,1.73\right)$ or better	**B1**	
(ii)	$\left(\dfrac{\pi}{6},2\right)$ or $\left(0.524,2\right)$ or better	**B1, B1**	**B1** for each
(iii)	$\cos\left(x-\dfrac{\pi}{6}\right)=0$	**M1**	for correct attempt to solve trigonometric equation
	$x=\dfrac{2\pi}{3}$ oe or 2.09 or better	**A1**	
(iv)	$2\sin\left(x-\dfrac{\pi}{6}\right)$ (+c)	**B1**	
(v)	Area $=\left[2\sin\left(x-\dfrac{\pi}{6}\right)\right]_{0}^{\frac{2\pi}{3}}$	**M1**	for correct use of **their** limits, in radians, into $k\sin\left(x-\dfrac{\pi}{6}\right)$.
	$=2+1$ $=3$	**A1**	
8 **(i)**	$47-24=12\theta$ $\theta=\dfrac{23}{12}$, so $\theta=1.917$ or better	**M1**	for complete correct method to get $\theta=$
	$\theta=1.92$ to 2dp	**A1**	must have evidence of working to more than 2 dp, allow if 1.916 seen (truncated)
(ii)	$\sin\dfrac{\theta}{2}=\dfrac{CD\!\!\big/\!2}{12}$	**M1**	for a complete method, may use cosine rule to get *CD*
	CD = awrt 19.6 or 19.7	**A1**	
(iii)	Area of sector = awrt 138	**B1**	for sector area, allow unsimplified
	Area of triangle *AOB* = awrt 67 or 68	**M1**	for a correct attempt at area
	Area of segment = awrt 70 or 71	**M1**	for segment area (*their* sector area – *their* triangle area)
	$AD\times AB$ + segment area = 425	**M1**	for complete method to find *AD*
	leading to *AD* = awrt 18.1 or 18.0	**A1**	Allow **A1** for 18
	Alternative method: Area of sector = awrt 138	**B1**	for sector area
	Difference in length between *BC* (or *AD*) and *OM* where *M* is the midpoint of *CD* = 6.88, allow awrt 6.9	**M1**	for attempt to find difference between parallel sides
	Remaining area consists of two trapezia each of width 9.85 and each of area 143.4 $\dfrac{1}{2}\left(2BC-6.88\right)\times 9.85=143.4$ oe	**M1**	for area of one trapezium $\dfrac{1}{2}\left(2BC-their\ 6.88\right)\times their\ 9.85$ oe
		M1	for attempt to find either *BC* or *AD*
	leading to *AD* = awrt 18.1 or 18.0	**A1**	

Question	Answer	Marks	Part Marks
9 (i)	$p\left(\dfrac{3}{2}\right):$ $\dfrac{27a}{8}-\left(4\times\dfrac{9}{4}\right)+\dfrac{3b}{2}+18$ $(=0)$	M1	for attempt at $p\left(\dfrac{3}{2}\right)$
	$p'\left(\dfrac{3}{2}\right)=\left(3a\times\dfrac{9}{4}\right)-\left(8\times\dfrac{3}{2}\right)+b$ $(=0)$	M1	for differentiation and attempt at $p'\left(\dfrac{3}{2}\right)$
	leading to $9a+4b+24=0$ oe and $27a+4b-48=0$ oe	M1	for solution of simultaneous equations, to get either a or b
	leading to $a=4$, $b=-15$	A1	for both
(ii)	$(x+2)(2x-3)^2$ oe	M1, A1	M1 for attempt at long division or factorisation
(iii)	$(x+2)(2x-3)^2=x+2$ $x+2=0$, $x=-2$	B1	Must be using $(x+2)$ correctly using part (ii) to get $x=-2$
	$(2x-3)^2=1$	M1	for solution of the quadratic equation
	leading to $x=1$, $x=2$	A1	
10 (a) (i)	$20U+\dfrac{1}{2}\left(U+\dfrac{U}{2}\right)10=165$	M1	for realising that area under the graph is needed and attempt to find an area
		DM1	for equating their area to 165 and attempt to solve
	leading to $U=6$	A1	
(ii)	Gradient of line: -0.3	M1, A1	M1 for use of the gradient, must be negative
(b) (i)	27	B1	
(ii)	$t^2=8\ln 4$ $t=3.33$ or better	M1 A1	for a correct attempt to solve $e^{\frac{t^2}{8}}=4$
(iii)	acceleration $=3\dfrac{2t}{8}e^{\frac{t^2}{8}}\left(e^{\frac{t^2}{8}}-4\right)^2$	M1, A1	M1 for a correct attempt to differentiate using the chain rule
	When $t=1$, $a=6.98$	M1, A1	M1 for use of $t=1$ in their acceleration

Question	Answer	Marks	Part Marks
11 (i)	$\ln y = \ln A + x \ln b$	**B1**	may be implied, if equation not seen specifically, by correct values for A and b
	Gradient: $\ln b = -\dfrac{0.12}{8}$, $= -0.015$	**M1**	for use of gradient to obtain $\ln b$
	$b = 0.985$	**A1**	Allow **A1** for $e^{-0.015}$
	Intercept: $\ln A = 0.26$	**DM1**	for use of one of the given points correctly
	$A = 1.30$	**A1**	Allow **A1** for $e^{0.26}$ or 1.3
	Alternative 1		
	$\ln y = \ln A + x \ln b$	**B1**	
	$0.2 = 4 \ln b + \ln A$	**M1**	for one correct equation
	$0.08 = 12 \ln b + \ln A$	**DM1**	for attempt to obtain either $\ln A$ or $\ln b$ from simultaneous equations
	$A = 1.30$ and $b = 0.985$	**A1**, **A1**	Allow **A1** for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
	Alternative 2		
	$1.22 = Ab^4$	**B1**	
	$1.08 = Ab^{12}$	**B1**	
		M1	for correct attempt to obtain b or A, must already have **B2**
	$A = 1.30$ and $b = 0.985$	**A1**, **A1**	Allow **A1** for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
(ii)	When $x = 6$, $\ln y = 0.17$	**M1**	for $\ln y = their \ln A + 6 \; their \ln b$ or $y = their \, A \times (their \; b)^6$
	$y = 1.19$	**A1**	allow awrt 1.18 to 1.20
(iii)	When $y = 1.1$, $\ln y = 0.095$	**M1**	for $\ln 1.1 = their \ln A + x \; their \ln b$ or $1.1 = their A \times (their b)^x$
	$x = 11$	**A1**	allow 10.5 to 11.5

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