UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level Advanced International Certificate of Education

MARK SCHEME for the June 2004 question papers

	9709 MATHEMATICS
9709/01	Paper 1 (Pure 1), maximum raw mark 75
9709/02	Paper 2 (Pure 2), maximum raw mark 50
9709/03, 8719/03	Paper 3 (Pure 3), maximum raw mark 75
9709/04	Paper 4 (Mechanics 1), maximum raw mark 50
9709/05, 8719/05	Paper 5 (Mechanics 2), maximum raw mark 50
9709/06, 0390/06	Paper 6 (Probability and Statistics 1), maximum raw mark 50
9709/07, 8719/07	Paper 7 (Probability and Statistics 2), maximum raw mark 50

These mark schemes are published as an aid to teachers and students, to indicate the requirements of the examination. They show the basis on which Examiners were initially instructed to award marks. They do not indicate the details of the discussions that took place at an Examiners' meeting before marking began. Any substantial changes to the mark scheme that arose from these discussions will be recorded in the published *Report on the Examination*.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes must be read in conjunction with the question papers and the *Report on the Examination*.

• CIE will not enter into discussion or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the June 2004 question papers for most IGCSE and GCE Advanced Level syllabuses.



	maximum	minimum mark required for grade:			
	mark available	А	В	Е	
Component 1	75	63	56	31	
Component 2	50	37	33	18	
Component 3	75	61	55	29	
Component 4	50	38	34	18	
Component 5	50	36	32	17	
Component 6	50	38	34	19	
Component 7	50	42	37	22	

Grade thresholds taken for Syllabus 9709 (Mathematics) in the June 2004 examination.

The thresholds (minimum marks) for Grades C and D are normally set by dividing the mark range between the B and the E thresholds into three. For example, if the difference between the B and the E threshold is 24 marks, the C threshold is set 8 marks below the B threshold and the D threshold is set another 8 marks down. If dividing the interval by three results in a fraction of a mark, then the threshold is normally rounded down.

Mark Scheme Notes

- Marks are of the following three types:
 - M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
 - A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
 - B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

- The following abbreviations may be used in a mark scheme or used on the scripts:
 - AEF Any Equivalent Form (of answer is equally acceptable)
 - AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
 - BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
 - CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
 - CWO Correct Working Only often written by a 'fortuitous' answer
 - ISW Ignore Subsequent Working
 - MR Misread
 - PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
 - SOS See Other Solution (the candidate makes a better attempt at the same question)
 - SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √"marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 75

SYLLABUS/COMPONENT: 9709/01

MATHEMATICS Paper 1 (Pure 1)



Page 1 Mark S			Syllabus Paper
A AND AS LEV	'EL -	JUNE	2004 9709 1
1. (i) $a/(1-r) = 256$ and $a = 64$ $\rightarrow r = \frac{3}{4}$ (ii) $S_{10} = 64(1-0.75^{10})$ (1-0.75) $\rightarrow S_{10} = 242$	M1 A1 M1 A1	[2] [2]	Use of correct formula Correct only Use of correct formula – 0.75 ¹⁰ not 0.75 ⁹ Correct only
2. $\int_{0}^{1} \sqrt{3x+1} dx = (3x+1)^{1.5} \div 1.5$	B1		MI for $(3x+1)^{1.5} \div 1.5$
then 3	M1		For division by 3
→ [] at 1 – [] at 0 → 16/9 – 2/9 = 14/9 or 1.56	M1 A1	[4]	Must attempt [] at x=0 (not assume it is 0) and be using an integrated function Fraction or decimal. (1.56+C loses this A1)
3. (i) $\sin^2 \theta + 3\sin \theta \cos \theta = 4\cos^2 \theta$ divides by $\cos^2 \theta$ $\rightarrow \tan^2 \theta + 3\tan \theta = 4$ (ii) Solution $\tan \theta = 1$ or $\tan \theta = -4$	M1 A1 M1	[2]	Knowing to divide by $\cos^2 \theta$ Correct quadratic (not nec = 0) Correct solution of quadratic = 0
$\rightarrow \theta$ = 45° or 104.0°	A1	A1 [3]	Correct only for each one.
4. (i) Coeff of $x^3 = 6C3 \times 2^3$ =160	B1 B1	B1 [3]	B1 for 6C3 B1 for 2 ³ B1 for 160
(ii) Term in x ² = 6C2 x 2 ² = 60	B1		B1 for 60 (could be given in (i))
reqd coeff = 1 x (i) $- 3 \times 60$ $\rightarrow -20$	M1 A1	[3]	Needs to consider 2 terms co
5.			
(i) Area of sector = $\frac{1}{2} 6^2 0.8$ (14.4) Area of triangle = $\frac{1}{2} .10^2 .sin0.8$ (35.9) \rightarrow Shaded area = 21.5	M1 M1 A1	[3]	Use of $\frac{1}{2}r^2\theta$ with radians Use of $\frac{1}{2}absinC$ or $\frac{1}{2}$ bh with trig Correct only
(ii) Arc length = 6×0.8 (4.8) CD (by cos rule) or $2 \times 10\sin 0.4$ (7.8) \rightarrow Perimeter = $8 + 4.8 + 7.8 = 20.6$	M1 M1 A1	A1 [4]	Use of s=rθ with radians Any correct method – allow if in (i) Correct only

	Page 2	Mark S	Scheme		Syllabus	Paper
		A AND AS LEV	EL – JUN	E 2004	9709	1
6.	$\rightarrow x^2 + x - 6$ Solution of	x (or y) completely =0 or y ² –17y+66=0 ⁻ quadratic = 0 nd (–3, 11)	M1 A1 DM1 A1 [4]	Needs x or y remo Correct only (no Equation must = (Everything ok.	need for $= 0$	
			B1 √ M1 M1 A1 [4]	For his two points Use of y-step x-s Use of $m_1m_2 = -1$ Any form – needs	step (beware	
7.	Gradient of Gradient of	nal y–3 = 2(x–6) (y=2x–9)	M1 A1 DM1 DM1 A1 [5]	Any attempt at dif For $-\frac{1}{2}$ Use of m ₁ m ₂ = -1 Correct method for Ans given – bewa	or eqn of line	
	(ii) Vol = $\pi \int \frac{3}{2}$	$\frac{24}{x^2}dx = \pi \left[-324x^{-1}\right].$	M1 A1	Use of $\int y^2 dx$ for	r M. correct	(needs π) for λ
	Uses value	at x=6 – value at x= 4.5	DM1	Use of 6 and 4.5		
	54 π 7	$72 \pi = 18 \pi$	A1 [4]	Beware fortuitous	answers (ar	ns given)
8.	(i) $2h + 2r + \pi$ $\rightarrow h = 4 - r$		M1 A1 [2]	Reasonable atten correct formula fo Co in any form wi	r ½C or C.	4 lengths +
	(ii) A=2rh+½π	$r^2 \rightarrow A = r(8-2r-\pi r) + \frac{1}{2}\pi r^2$	M1	Adds rectangle +	¹ ∕₂xcircle (eq	n on own ok)
	\rightarrow A = 8r –	$2r^2 - \frac{1}{2}\pi r^2$	A1	Co beware fortuite	ous answers	(ans given)
	(iii) dA/dr = 8 – = 0 when i	$-4r - \pi r$ r = 1.12 (or 8/(4+ π))	[2] M1 A1 DM1 A1 [4]	Knowing to differe Setting his dA/dr t		•
	(iv) $d^2A/dr^2 = -$	$4 - \pi$	M1	Looks at 2 nd differ		er valid
	This is neg	ative \rightarrow Maximum	A1 [2]	complete method Correct deduction correct.		l ² A/dr ²

Page 3

Mark Scheme A AND AS LEVEL – JUNE 2004

SyllabusPaper97091

$9. \overrightarrow{OA} = \begin{pmatrix} 1\\ 3\\ -1 \end{pmatrix}, \overrightarrow{OB} = \begin{pmatrix} 3\\ -1\\ 3 \end{pmatrix}, \overrightarrow{OC} = \begin{pmatrix} 4\\ 2\\ p \end{pmatrix}, \overrightarrow{OD} = \begin{pmatrix} -1\\ 0\\ q \end{pmatrix}$		Condone notation throughout.
(-1) (3) (p) (q)		Allow column vectors or i,j,k throughout
(i) $\overrightarrow{AB} = \mathbf{b} - \mathbf{a} = 2\mathbf{i} - 4\mathbf{j} + 4\mathbf{k}$	M1	Use of b–a , rather than b+a or a–b
Unit vector = $(2i - 4j + 4k) = \sqrt{(2^2 + 4^2 + 4^2)}$	M1	Dividing by the modulus of "his" \overrightarrow{AB}
$= \pm (2\mathbf{i} - 4\mathbf{j} + 4\mathbf{k}) 6$	A1	Co (allow – for candidates using a–b)
	[3]	
(ii) $\overrightarrow{OA.OC} = 4 + 6 - p$	M1	Use of $x_1x_2 + y_1y_2 + z_1z_2$
$= 0 \text{ for } 90^{\circ}$ $\rightarrow p = 10$	DM1 A1	Setting to 0 + attempt to solve co
	[3]	
(iii) $(-2)^2 + 3^2 + (q+1)^2 = 7^2$	M1	Correct method for length with ±d–a, d+a
\rightarrow (q+1) ² = 36 or q ² + 2q = 35	A1	Correct quadratic equation
g = 5 and g = -7	DM1 A1	Correct method of solution. Both correct.
	or B1 B1	Or B1 for each if $(q+1)^2=36$, $q=5$ only.
	[4]	
10. f: x \mapsto x ² -2x, g: x \mapsto 2x+3		
(i) $x^2 - 2x - 15 = 0$	M1	Equation set to 0 and solved.
End-points –3 and 5	A1	Correct end-points, however used
\rightarrow x < -3 and x > 5	A1	Co-inequalities – not ≤ or ≥
(ii) Uses dy/dx = $2x-2 = 0$ or $(x-1)^2 - 1$	[3] M1	Any valid complete method for x value
Minimum at $x = 1$ or correct form	A1	Correct only
Range of y is $f(x) \ge -1$	A1	Correct for his value of "x" – must be ≥
No inverse since not 1 : 1 (or equivalent)	B1	Any valid statement.
	[4]	
(iii) $gf(x) = 2(x^2 - 2x) + 3$ (2x ² - 4x +3)	M1	Must be gf not fg – for unsimplified ans.
$b^2 - 4ac = 16 - 24 = -8 \rightarrow -ve$	M1	Used on quadratic=0, even if fg used.
\rightarrow No real solutions.	A1	Must be using gf and correct assumption
[or gf(x)=0 \rightarrow f(x)=-3/2. Imposs from (ii)]	[3]	and statement needed.
(iv) $y = 2x + 3$ correct line on diagram	B2,1,0 [2]	3 things needed –B1 if one missing.g correct,
Either inverse as mirror image in y=x	[4]	 g⁻¹ correct – not parallel to g
or $y = g^{-1}(x) = \frac{1}{2} (x-3)$ drawn		• y=x drawn or statement re symmetry
DM1 for quadratic equation. Equation must be set to	0	

Formula \rightarrow must be correct and correctly used – allow for numerical errors though in b² and –4ac. Factors \rightarrow attempt to find 2 brackets. Each bracket then solved to 0.

GCE AS LEVEL

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/02

MATHEMATICS Paper 2 (Pure 2)



	Page	1 Mark Scheme	Syllabus	Paper	
		A AND AS LEVEL – JUNE 2004	9709	2	
1		logarithms to linearise an equation		M1	
	Obt	ain $\frac{x}{y} = \frac{\ln 5}{\ln 2}$ or equivalent		A1	
		ain answer 2.32		A1	3
2	(i)	Use the given iterative formula correctly at least ONCE with x_1 = Obtain final answer 3.142 Show sufficient iterations to justify its accuracy to 3 d.p.	3	M1 A1 A1	3
	(ii)	State any suitable equation e.g. $x = \frac{1}{5} \left(4x + \frac{306}{x^4} \right)$		B1	•
		Derive the given answer α (or x) = $\sqrt[5]{306}$		B1	2
3	(i)	Substitute x = 3 and equate to zero Obtain answer $\alpha = -1$		M1 A1	2
	(ii)	At any stage, state that x = 3 is a solution EITHER: Attempt division by (x–3) reaching a partial quotient of Obtain quadratic factor $2x^2 + 5x + 2$ Obtain solutions x = -2 and x = -½ OR: Obtain solution x = -2 by trial and error Obtain solution x = -½ similarly [If an attempt at the quadratic factor is made by inspection, the I unknown factor of $2x^2 + bx + c$ and an equation in b and/or c.]		B1 M1 A1 B1 B2 if it reaches	4 an
4	(i)	State answer R = 5 Use trigonometric formulae to find α Obtain answer α = 53.13°		B1 M1 A1	3
	(ii)	Carry out, or indicate need for, calculation of $\sin^{-1}(4.5/5)$ Obtain answer 11.0° Carry out correct method for the second root e.g. $180^{\circ} - 64.16^{\circ}$ Obtain answer 62.7° and no others in the range [Ignore answers outside the given range.]	– 53.13°	M1 A1√ M1 A1√	4
	(iii)	State least value is 2		В1√	1
5	(i)	State derivative of the form $(e^{-x} \pm xe^{-x})$. Allow $xe^{x} \pm e^{x}$ {via quotie Obtain correct derivative of $e^{\pm x} - xe^{-x}$ Equate derivative to zero and solve for x Obtain answer x = 1	ent rule}	M1 A1 M1 A1	4
	(ii)	Show or imply correct ordinates 0, 0.367879 , 0.27067 Use correct formula, or equivalent, with h = 1 and three ordinate Obtain answer 0.50 with no errors seen	es	B1 M1 A1	3
	(iii)	Justify statement that the rule gives an under-estimate		B1	1

Γ	Page 2		Mark Scheme	Syllabus	Paper	
			A AND AS LEVEL – JUNE 2004	9709	2	
6	(i)		e that $\frac{dx}{dt} = 2 + \frac{1}{t}$ or $\frac{dy}{dt} = 1 - \frac{4}{t^2}$, or equivalent		B1	
		Use	$\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$		M1	
		Obta	in the given answer		A1	3
	(ii)	Subs	stitute t = 1 in $\frac{dy}{dx}$ and both parametric equations		M1	
		Obta	in $\frac{dy}{dx} = -1$ and coordinates (2, 5)		A1	
		State	e equation of tangent in any correct horizontal form e.g. $x + y$	y = 7	A1√	3
	(iii)	Equa	ate $\frac{dy}{dx}$ to zero and solve for t		M1	
			in answer t = 2 in answer y = 4		A1 A1	
		Show	w by any method (but <u>not via</u> $\displaystyle rac{d}{dt}(y')$) that this is a minimum	ı point	A1	4
7	(i)	Make Obta Use	e relevant use of the $cos(A + B)$ formula e relevant use of cos2A and sin2A formulae in a correct expression in terms of cosA and sinA $sin^2A = 1 - cos^2A$ to obtain an expression in terms of cosA in given answer correctly		M1* M1* A1 M1(d A1	ep*) 5
	(ii)	Repl	ace integrand by $\frac{1}{4}\cos 3x + \frac{3}{4}\cos x$, or equivalent		B1	
		Integ	prate, obtaining $\frac{1}{12}$ sin3x + $\frac{3}{4}$ sinx, or equivalent		B1 +	B1√
		Use	limits correctly in given anser		M1 A1	5

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GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 75

SYLLABUS/COMPONENT: 9709/03, 8719/03

MATHEMATICS AND HIGHER MATHEMATICS Paper 3 (Pure 3)



	Page 1	Mark Scheme	Syllabus	Paper		
		A AND AS LEVEL – JUNE 2004	9709/8719	3		
1	Show corr	rect sketch for $0 \le x < \frac{1}{2}\pi$			B1	
	Show corr	rect sketch for $\frac{1}{2}\pi < x < \frac{3}{2}\pi$ or $\frac{3}{2}\pi < x \le 2\pi$			B1	
	Show con	npletely correct sketch			B1	3
	[SR: for a	graph with $y = 0$ when $x = 0$, π , 2π but otherwise of correct	shape, aware	d B1.]		
2	EITHER:	State or imply non-modular inequality $(2x+1)^2 < x^2$ or co	rresponding c	quadratic		
		equation or pair of linear equations $(2x + 1) = \pm x$			B1	
		Expand and make a reasonable solution attempt at a 3-te	rm quadratic,	or solve two)	
		linear equations			M1	
		Obtain critical values $x = -1$ and $x = -\frac{1}{3}$ only			A1	
		State answer $-1 < x < -\frac{1}{3}$			A1	
	OR:	Obtain the critical value $x = -1$ from a graphical method ,	or by inspecti	on, or by		
		solving a linear inequality or equation			B1	
		Obtain the critical value $x = -\frac{1}{3}$ (deduct B1 from B3 if extr	a values are	obtained)	B2	
		State answer $-1 < x < -\frac{1}{3}$			B1	4
		[Condone \leq for <; accept -0.33 for $-\frac{1}{3}$.]				

3	EITHER:	State $6y \frac{dy}{dx}$ as the derivative of $3y^2$	B1	
		State $\pm 4x \frac{dy}{dx} \pm 4y$ as the derivative of $-4xy$	B1	
		Equate attempted derivative of LHS to zero and solve for $\frac{dy}{dx}$	M1	
		Obtain answer 2	A1	
		[The M1 is conditional on at least one of the B marks being obtained. Allow any		
		combination of signs for the second B1.]		
	OR:	Obtain a correct expression for <i>y</i> in terms of <i>x</i>	B1	
		Differentiate using chain rule	M1	
		Obtain derivative in any correct form	A1	
		Substitute $x = 2$ and obtain answer 2 only	A1	4
		[The M1 is conditional on a reasonable attempt at solving the quadratic in y being made	le.]	

	Page	2	Mark Scheme	Syllabus	Paper		
			A AND AS LEVEL – JUNE 2004	9709/8719	3		
4	(i)	State	e or imply $2^{-x} = \frac{1}{y}$			B1	
		Obta	in 3-term quadratic e.g. $y^2 - y - 1 = 0$			B1	2
	(ii)	Solve	e a 3-term quadratic, obtaining 1 or 2 roots			M1	
		Obta	in answer $y = (1 + \sqrt{5})/2$, or equivalent			A1	
		Carry	, out correct method for solving an equation of the form $2^x =$	a, where a	> 0, reaching	J	
		a rati	o of logarithms			M1	
		Obta	in answer $x = 0.694$ only			A1	4
5	(i)	Make	e relevant use of formula for sin 2θ or cos 2θ			M1	
			e relevant use of formula for $\cos 4\theta$			M1	
		Com	plete proof of the given result			A1	3
	(ii)	Integ	rate and obtain $\frac{1}{8}(\theta - \frac{1}{4}\sin 4\theta)$ or equivalent			B1	
		Use	limits correctly with an integral of the form $a\theta$ + $b\sin 4\theta$, when	re <i>ab</i> ≠ 0		M1	
		Obta	in answer $\frac{1}{8}(\frac{1}{3}\pi + \frac{\sqrt{3}}{8})$, or exact equivalent			A1	3
6	Sep	arate	variables and attempt to integrate			M1	
	Obt	ain tei	rms $\frac{1}{3}\ln(y^3+1)$ and x, or equivalent		A	1 + A1	
	Eva	luate	a constant or use limits $x = 0$, $y = 1$ with a solution containing	g terms $k \ln($	$(y^3 + 1)$ and x,		
	or e	quival	ent			M1	
	Obt	ain an	y correct form of solution e.g. $\frac{1}{3}\ln(y^3+1) = x + \frac{1}{3}\ln 2$			A1√	
	Rea	irrang	e and obtain $y = (2e^{3x} - 1)^{\frac{1}{3}}$, or equivalent			A1	6
	[f.t.	is on <i>l</i>	k ≠ 0.]				
7	(i)	Fyalı	uate cubic when $x = -1$ and $x = 0$			M1	
'	(")		y given statement correctly			A1	2
			Iculations are not given but justification uses correct stateme	ents about sig	gns, award B		-
			2				

(ii) State
$$x = \frac{2x^3 - 1}{3x^2 + 1}$$
, or equivalent B1
Rearrange this in the form $x^3 + x + 1 = 0$ (or vice versa) B1 **2**

F	Page	3	Mark SchemeSyllabusPaperA AND AS LEVEL – JUNE 20049709/87193	7	
	/····				
	(iii)		the iterative formula correctly at least once	M1	
			in final answer –0.68	A1	
			w sufficient iterations to justify its accuracy to 2d.p., or show there is a sign change val (–0.685, –0.675)	A1	3
		Interv	var (~0.003, ~0.073)		J
8	(i)	EITH	•	M1	
			Obtain roots $\frac{1}{2} + i\frac{\sqrt{3}}{2}$ and $\frac{1}{2} - i\frac{\sqrt{3}}{2}$ or equivalent	A1	
		OR:	Substitute $x + iy$ and solve for x or y	M1	
			Obtain correct roots	A1	2
	(ii)	State	e that the modulus of each root is equal to 1	B1√	
		State	e that the arguments are $\frac{1}{3}\pi$ and $-\frac{1}{3}\pi$ respectively	$B1\sqrt{+}B1\sqrt{-}$	3
		[Acce	ept degrees and $\frac{5}{3}\pi$ instead of $-\frac{1}{3}\pi$. Accept a modulus in the form $\sqrt{\frac{p}{q}}$ or \sqrt{n} , wh	ere	
			<i>n</i> are integers. An answer which only gives roots in modulus-argument form earns		h
			mplied moduli and B1 for both the implied arguments.]		
	()		<i>HER</i> : Verify $z^3 = -1$ for each root		
	(111)	EITH		B1 + B1	
		OR:	: State $z^3 + 1 = (z+1)(z^2 - z + 1)$	B1	
			Justify the given statement	B1	
		OR:	: Obtain $z^3 = z^2 - z$	B1	
			Justify the given statement	B1	2
9	(i)	State	e or imply $f(x) = \frac{A}{x-1} + \frac{B}{x-2} + \frac{C}{x+1}$	B1	
		EITH	<i>IER</i> : Use any relevant method to obtain a constant	M1	
			Obtain one of the values: $A = -1$, $B = 4$ and $C = -2$	A1	
			Obtain the remaining two values	A1	
		OR:	Obtain one value by inspection	B1	
			State a second value	B1	
			State the third value $A = Br + C$	B1	4
		[Apply	ly the same scheme to the form $\frac{A}{x-2} + \frac{Bx+C}{x^2-1}$ which has $A = 4$, $B = -3$ and $C = 1$.]	

Page 4	Mark Scheme	Syllabus	Paper
	A AND AS LEVEL – JUNE 2004	9709/8719	3

- (ii) Use correct method to obtain the first two terms of the expansion of $(x-1)^{-1}$ or $(x-2)^{-1}$ or $(x+1)^{-1}$ M1
 - Obtain any correct unsimplified expansion of the partial fractions up to the terms in x^3 (deduct A1 for each incorrect expansion) $A1\sqrt{+} A1\sqrt{+} A1\sqrt{-}$ Obtain the given answer correctlyA1**5**

[Binomial coefficients involving -1, e.g. $\binom{-1}{1}$, are not sufficient for the M1 mark. The f.t. is on *A*, *B*, *C*.] [Apply a similar scheme to the alternative form of fractions in (i), awarding M1*A1 $\sqrt{A1}\sqrt{for}$ the expansions, M1(dep*) for multiplying by Bx + C, and A1 for obtaining the given answer correctly.] [In the case of an attempt to expand $(x^2 + 7x - 6)(x - 1)^{-1}(x - 2)^{-1}(x + 1)^{-1}$, give M1A1A1A1 for the expansions and A1 for multiplying out and obtaining the given answer correctly.] [Allow attempts to multiply out $(x - 1)(x - 2)(x + 1)(-3 + 2x - \frac{3}{2}x^2 + \frac{11}{4}x^3)$, giving B1 for reduction to a product of two expressions correct up to their terms in x^3 , M1 for attempting to multiply out at least as far as terms in x^2 , A1 for a correct expansion up to terms in x^3 .] [Allow the use of Maclaurin, giving M1A1 \sqrt{for} f(0) = -3 and f'(0) = 2, A1 \sqrt{for} f "(0) = -3, A1 \sqrt{for} f "'(0) = $\frac{33}{2}$, and A1 for obtaining the given answer correctly (f.t. is on *A*, *B*, *C* if used).]

10 (i) State *x*-coordinate of *A* is 1

(ii)	Use product or quotient rule	M1
	Obtain derivative in any correct form e.g. $-\frac{2\ln x}{x^3} + \frac{1}{x} \cdot \frac{1}{x^2}$	A1
	Equate derivative to zero and solve for In x	M1

B1

1

Obtain $x = e^{\frac{1}{2}}$ or equivalent (accept 1.65)	A1
1	

Obtain $y = \frac{1}{2e}$ or exact equivalent not involving ln A1 5

[SR: if the quotient rule is misused, with a 'reversed' numerator or x^2 instead of x^4 in the denominator, award M0A0 but allow the following M1A1A1.]

(iii) Attempt integration by parts, going the correct wayM1Obtain $-\frac{\ln x}{x} + \int \frac{1}{x} \cdot \frac{1}{x} dx$ or equivalentA1Obtain indefinite integral $-\frac{\ln x}{x} - \frac{1}{x}$ A1Use x-coordinate of A and e as limits, having integrated twiceM1Obtain exact answer $1 - \frac{2}{e}$, or equivalentA1If $u = \ln x$ is used, apply an analogous scheme to the result of the substitution.]

-	age 5		Mark Scheme	Syllabus	Paper
			A AND AS LEVEL – JUNE 2004	9709/8719	3
	(i) <i>El</i>		Obtain a vector in the plane e.g. \overrightarrow{PQ} = -3i + 4j +k		
	(.)		Use scalar product to obtain a relevant equation in a	abcea-3	a + 4b + c =
			6a - 2b + c = 0 or $3a + 2b + 2c = 0$	a, o , o o.g. o	
			State two correct equations in a, b, c		
			Solve simultaneous equations to obtain one ratio e.	g.a:b	
			Obtain $a : b : c = 2 : 3 : -6$ or equivalent		
			Obtain equation $2x + 3y - 6z = 8$ or equivalent		
			[The second M1 is also given if say <i>c</i> is given an art	oitrary value a	nd <i>a</i> or <i>b</i> is f
			The following A1 is then given for finding the correct	t values of <i>a</i> a	nd <i>b</i> .]
	C	OR:	Substitute for P, Q, R in equation of plane and state	3 equations i	n a, b, c, d
			Eliminate one unknown, e.g. d, entirely		
			Obtain 2 equations in 3 unknowns		
			Solve to obtain one ratio e.g. <i>a</i> : <i>b</i>		
			Obtain $a : b : c = 2 : 3 : -6$ or equivalent		
			Obtain equation $2x + 3y - 6z = 8$ or equivalent		
			[The first M1 is also given if say <i>d</i> is given an arbitra	ary value and t	wo equation
			two unknowns, e.g. <i>a</i> and <i>b</i> , are obtained. The follow	wing A1 is for	two correct
			equations. Solving to obtain one unknown earns the	e second M1	and the follow
			A1 is for finding the correct values of <i>a</i> and <i>b</i> .]		
	I	OR:	Obtain a vector in the plane e.g. \overrightarrow{QR} = 6 i –2 j + k		
			Find a second vector in the plane and form correctly	/ a 2-paramete	er equation for
			the plane		
			Obtain equation in any correct form e.g. $\mathbf{r} = \lambda (-3\mathbf{i} + 2\mathbf{j})$	4 j +k) + μ(6i –	2j + k) + i – l
			State 3 equations in <i>x</i> , <i>y</i> , <i>z</i> , λ , and μ		
			Eliminate λ and μ		
			Obtain equation $2x + 3y - 6z = 8$ or equivalent		
	(OR:	Obtain a vector in the plane e.g. $\overrightarrow{PR} = 3\mathbf{i} + 2\mathbf{j} + 2\mathbf{k}$		
			Obtain a second vector in the plane and calculate the	ne vector prod	uct of the two
			vectors, e.g. $(-3i + 4j + k) \times (3i + 2j + 2k)$		
			Obtain 2 correct components of the product		
			Obtain 2 concer components of the product		
			Obtain correct product e.g. $6\mathbf{i} + 9\mathbf{j} - 18\mathbf{k}$ or equivalent	nt	

6

Page 6	Mark Scheme Syllabus Paper		
	A AND AS LEVEL – JUNE 2004 9709/8719 3		
(ii) <i>EITHEI</i>	State equation of SN is $\mathbf{r} = 3\mathbf{i} + 5\mathbf{j} - 6\mathbf{k} + \lambda(2\mathbf{i} + 3\mathbf{j} - 6\mathbf{k})$ or equivalent	B1√	
	Express x, y, z in terms of λ e.g. (3 + 2 λ , 5 +3 λ , -6 -6 λ)	B1√	
	Substitute in the equation of the plane and solve for λ	M1	
	Obtain \overrightarrow{ON} = i + 2 j , or equivalent	A1	
	Carry out method for finding SN	M1	
	Show that <i>SN</i> = 7 correctly	A1	
OR:	Letting $\overrightarrow{ON} = x\mathbf{i} + y\mathbf{j} + z\mathbf{k}$, obtain two equations in x, y, z by equating scalar		
	product of \overrightarrow{NS} with two of $\overrightarrow{PQ}, \overrightarrow{QR}, \overrightarrow{RP}$ to zero B1	I√+ B1√	
	Using the plane equation as third equation, solve for x , y , and z	M1	
	Obtain \overrightarrow{ON} = i +2 j , or equivalent	A1	
	Carry out method for finding SN	M1	
	Show that SN = 7 correctly	A1	
OR:	Use Cartesian formula or scalar product of \overrightarrow{PS} with a normal vector to find SN	M1	
	Obtain SN = 7	A1	
	State a unit normal $\hat{\mathbf{n}}$ to the plane	B1√	
	Use $\overrightarrow{ON} = \overrightarrow{OS} \pm 7\hat{\mathbf{n}}$	M1	
	Obtain an unsimplified expression e.g. 3 i + 5 j –6 k $\pm 7(\frac{2}{7}i + \frac{3}{7}j - \frac{6}{7}k)$	A1√	
	Obtain \overrightarrow{ON} = i +2j, or equivalent, only	A1	e

GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/04

MATHEMATICS Paper 4 (Mechanics 1)



F	Page 1	Mark Scher	ne		Syllabus Paper
-		A AND AS LEVEL -		004	9709 4
1	(i)	$F = 13 \cos \alpha$	M1	•	For resolving forces horizontally
	(::)	Frictional component is 12 N $R = 1.1 \times 10 + 13 \sin \alpha$	A1 M1	2	For reaching fores worthally (2)
	(ii)	$R = 1.1 \times 10 + 13 \sin \alpha$			For resolving forces vertically (3 terms needed)
		Normal component is 16 N	A1	2	
	(iii)	Coefficient of friction is 0.75	B1 ft	1	
2		$X = 100 + 250 \cos 70^{\circ}$	B1		
		$Y = 300 - 250 \sin 70^{\circ}$	B1		
		$R^2 = 185.5^2 + 65.1^2$	M1		For using $R^2 = X^2 + Y^2$
		<i>R</i> = 197	A1 ft		ft only if one B1 is scored or if
					the expressions for the
					candidate's <i>X</i> and <i>Y</i> are those of the equilibrant
		$\tan \alpha = 65.1/185.5$	M1		For using $\tan \alpha = Y/X$
		$\alpha = 19.3$	A1 ft	6	ft only if one B1 is scored
			/	Ũ	SR for sin/cos mix (max 4/6)
					$X = 100 + 250 \sin 70^{\circ}$ and
					$Y = 300 - 250\cos 70^{\circ}$
					(334.9 and 214.5) B1
					Method marks as scheme M1 M ²
			OR		$R = 398$ N and $\alpha = 32.6$ A1
		316(.227766) or 107(.4528) or	B1		Magnitude of the resultant of
		299(.3343)			two of the forces
		71.565° or 37.2743 ° or	B1		Direction of the resultant of two
		–51.7039 °			of the forces
		$R^2 = 316.2^2 + 250^2 -$	M1		For using the cosine rule to find
		$2 \times 316.2 \times 250 \cos 38.4^{\circ}$ $R^2 = 107.5^2 + 100^2 -$			R
		$R = 107.5 + 100 - 2 \times 107.5 \times 100 \text{ cos} 142.7^{\circ}$			
		$R^2 = 299.3^2 + 300^2 -$			
		2×299.3×300cos38.3°			
		<i>R</i> = 197	A1 ft		ft only if one B1 is scored
		$sin(71.6 - \alpha) = 250sin38.4 \div 197$	M1		For using the sine rule to find α
		$sin(37.3 - \alpha) = 100sin142.7 \div 197$			
		$sin(51.7 + \alpha) = 300sin38.3 \div 197$	A1 ft		ft only if one D1 is secred
		$\alpha = 19.3^{\circ}$			ft only if one B1 is scored
3	(i)	Distance AC is 70 m	B1		
J	(i)	$7 \times 10 - 4 \times 15$	ы M1		For using AB = AC - BC
		Distance AB is 10 m	A1	3	
	(ii)	x(m)	M1		Graph consists of 3 connected
	(,	\wedge			straight line segments with, in
					order, positive, zero and
					negative slopes. $x(t)$ is single
					valued and the graph contains
			A 4		the origin
			A1		1 st line segment appears steeper than the 3 rd and the 3 rd
		$10 \xrightarrow{10} \xrightarrow{10} \xrightarrow{1} \xrightarrow{1} \xrightarrow{1} \xrightarrow{1} \xrightarrow{1} \xrightarrow{1} \xrightarrow{1} 1$			line segment does not terminate
		10 15 30			on the <i>t</i> -axis
			A1 ft	3	Values of <i>t</i> (10, 15 and 30) and
					x (70, 70, 10) shown, or can be
					read without ambiguity from the
					SCALES
					SR (max 1out of 3 marks) For first 2 segments correct B1
					I OF ITST Z SEGMENTS CONECT DI

Page 2	Mark Scheme	Syllabus	Paper	
	A AND AS LEVEL – JUNE 2004	9709	4	

	1	1			
4	(i)	KE = 0.2g(0.7)	M1		For using KE = PE lost and PE
					lost = <i>mgh</i>
		Kinetic energy is 1.4 J	A1	2	
	(ii)	$R = 0.2 \times 10 \times \cos 16.3^{\circ}$	B1		1.92
	. ,	<i>F</i> = 0.288 N	B1 ft		From 0.15 <i>R</i> (may be implied by
					subsequent exact value 0.72,
					1.36 or 0.68)
		WD = 0.72 J or <i>a</i> = 1.36	B1 ft		From 2.5 <i>F</i> or from
		or resultant downward force			$0.2a = 0.2 \times 10 \times (7/25) - F$
		= 0.272 N			(may be implied by subsequent
		0.2.12.11			exact value 0.68)
		KE = 1.4 – 0.72 or	M1		For using KE = PE lost – WD
		$KE = \frac{1}{2} 0.2(2 \times 1.36 \times 2.5)$ or			or
		0.272×2.5			KE = $\frac{1}{2}mv^2$ and v^2 = 2as or
		0.212 ~ 2.5			KE = 72 mv and $v = 2as$ of $KE = resultant downward force$
				_	× 2.5
		Kinetic energy is 0.68 J	A1 ft	5	

5	(i)	$10t^2 - 0.25t^4$ (+ <i>C</i>)	M1 DM1		For integrating <i>v</i> For including constant of integration and attempting to evaluate it
		Expression is $10t^2 - 0.25t^4 - 36$	A1	3	
	(ii)	Displacement is 60 m	A1 ft	1	Dependent on both M marks in (i); ft if there is not more than one error in <i>s</i> (<i>t</i>)
	(iii)	$(t^2 - 36)(1 - 0.25t^2) = 0$	M1		For attempting to solve $s = 0$ (depends on both method marks in (i)) or $\int_0^t v dt = 36$ (but not -36) for t^2 by factors or formula method
		Roots of quadratic are 4, 36 $t = 2, 6$	A1 A1 ft	3	ft only from 3 term quadratic in t^2

6	(i)		M1		For using Newton's 2 nd law (3 terms needed)
		$DF - 400 = 1200 \times 0.5$ 20000 = 1000 <i>v</i> Speed is 20 ms ⁻¹	A1 M1 A1	4	For using $P = Fv$
	(ii)	20000/v - 400 = 0	M1		For using $P = Fv$ and Newton's 2^{nd} law with $a = 0$ and $F = 400$
		$v_{\rm max} = 50 \ {\rm ms}^{-1}$	A1	2	AG
	(iii)	$20000 = \frac{1500000}{\Delta T} \text{ or}$ distance = 1500 000/400 = 3750 and time = 3750/50 Time taken is 75 s	M1 A1	2	For using $P = \frac{\Delta W}{\Delta T}$ or for using 'distance = work done/400' and 'time =distance/50'

F	Page 3	Mark Scher				Syllabus	Paper	
		A AND AS LEVEL –	JUNE	2004	4 9709 4			
7	(i)	25 = 30t - 5t ² → t ² - 6t + 5 = 0 → (t - 1)(t - 5) = 0 or $v^2 = 30^2 - 500; t_{up} = (20 - 0)/10$	M1		attempti	g 25 = <i>ut</i> – ½ ng to solve fo ing <i>v</i> ² = <i>u</i> ² – · 0)/ <i>g</i>	or t	
		$t = 1, 5 \text{ or } t_{up} = 2$ Time = 5 - 1 = 4 s or Time = 2×2 = 4s or 1 < t < 5 $s_1 = 30t - 5t^2$ and $s_2 = 10t - 5t^2$	A1 A1	3				
	(ii)	$s_1 = 30t - 5t^2$ and $s_2 = 10t - 5t^2$	M1		For using and P_2	g <i>s</i> = <i>ut</i> − ½	gt^2 for P_1	
		30t - 10t = 25	M1			$g s_1 = s_2 + 2$ ng to solve for		
		<i>t</i> = 1.25	A1		actompti	ig to conto h		
		$v_1 = 30 - 10 \times 1.25$ or $v_2 = 10 - 10 \times 1.25$ or or	M1			g v = u – gt for calculation ing into		
		$v_1^2 = 30^2 - 2 \times 10(29.6875)$ or $v_2^2 = 10^2 - 2 \times 10(4.6875)$			$v_1^2 = 30^2$ calculati	2 – 2×10s ₁ o ng s ₂ and su = 10 ² – 2×10	bstituting	
		Velocities 17.5ms^{-1} and -2.5ms^{-1}	A1	5	$1110 v_2$ -	- 10 - 2 × 10	13 2	
			OR	0				
	(ii)	$v_1 = 30 - 10t$, $v_2 = 10 - 10t$	M1		For usin	g v = u - gt for	or P_1 and	
	()	→ $v_1 - v_2 = 20$	M1		P ₂ and e For using	liminating t g $v^2 = u^2 - 2g$ and then $s_1 =$	gs for P_1	
		$(30^{2} - v_{1}^{2}) \div 20 =$ $(10^{2} - v_{2}^{2}) \div 20 + 25$ $v_{1} - v_{2} = 20, v_{1}^{2} - v_{2}^{2} = 300$	A1					
			M1			ing simultane is in v_1 and v_2		
		Velocities are 17.5 ms ⁻¹ and – 2.5 ms ⁻¹	A1	5				
	(iii)	$t_{\rm up} = 3$	B1					
		3 – 1.25 Time is 1.75 s or 1.25 < <i>t</i> < 3	M1 A1	3	For using	g <i>t</i> _{up and above} =	= $t_{\rm up} - t_{\rm equal}$	
	I		OR	3				
	(iii)	0 = 17.5 - 10t	M2			g 0 = <i>u – gt</i> iswer found		
		Time is 1.75 s or 1.25 < <i>t</i> < 3	A1			1 out of 3 n		
					0 = 17.5		ÉB1 ft	

GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/05, 8719/05

MATHEMATICS AND HIGHER MATHEMATICS Paper 5 (Mechanics 2)



Page 1	Mark Scheme	Syllabus	Paper
	A AND AS LEVEL – JUNE 2004	9709/8719	5

Mechanics 2

1	For taking moments about the edge of the platform	M1
	$(75g \times 0.9 = 25g \times x + 10g \times 1.1)$ (3 term equation)	
	Two terms correct (unsimplified)	A1
	Completely correct (unsimplified)	A1
	Distance <i>MC</i> = 3.16m	A1

4

4

<u>NB:</u> If moments taken about other points, the force of the platform on the plank must be present at the edge of the platform for M1

2	(i)	Evaluates $\frac{2r\sin\alpha}{3\alpha} \times \cos\frac{\pi}{4}$	M1	
		Obtains given answer correctly	A1	2

(ii)	For taking moments about AB	M1
	{ $(5 \times 10 + \frac{1}{4}\pi 5^2)\overline{x} = (5 \times 10) \times 5 + \frac{1}{4}\pi 5^2(10 + \frac{20}{3\pi})$ }	
	For the total area correct and the moment of the rectangle correct	
	(unsimplified)	A1
	For the moment of CDE correct (unsimplified)	A1
	Distance is 7.01 cm	A1

3

For applying Newton's 2nd law and using $a = v \frac{dv}{dx}$ M1

$$0.6v\frac{dv}{dx} = -\frac{3}{x^3}$$
 A1

For separating the variables and integrating M1 $3x^{-2}$

$$0.3v^2 = -\frac{5x}{(-2)}$$
 (+C) A1 ft

(ft omission of minus sign in line 2 only)

For using = 0 when x = 10 M1

$$v^2 = \frac{5}{x^2} - \frac{1}{20}$$
 (aef) A1 ft

(ft wrong sign in line 4 only)

Speed is
$$\frac{\sqrt{3}}{2}$$
 ms⁻¹ (=0.866) A1 7

Page	2	Ma	ark Scheme	Syllabus	Paper]
		A AND AS	LEVEL – JUNE 2004	9709/8719	5	
4 (i)			the hinge is $\frac{2.4}{2.5}(0.7)$ or 0	0.7cos16.26° (=0.6	672) E	31
	[May	be implied in mome	nt equation]			
	For t	aking moments abou	it the hinge (3 term equat	ion)	Ν	/11
	0.67	2F = 68 x 1.2 + 750 >	< 2.4		A	\1 ft
	Forc	e is 2800 N			A	1
(ii)	X = 7	784	(ft for 0.28 <i>F</i>)		E	31 ft
	For r	esolving vertically (4	term equation)		Ν	/11
	Y = '	1870	(ft for 0.96 <i>F</i> –	818)	A	\1 ft

<u>SR</u>: For use of 680 N for weight of the beam: (i) B1, M1, A0. In (ii) ft 680, so 3/3 possible.

5	(i)	For using EPE = $\frac{\lambda x^2}{2L}$	M1

EPE gain =
$$2\left(\frac{200x^2}{2\times4}\right)$$
 (=50x²) A1

GPE loss = $10g (4 + x)$	B1
For using the principle of conservation of energy to form an equation	M1
containing EPE, GPE and KE terms	

$$[\frac{1}{2}10^{2} + 50x^{2} = 10g (4 + x)]$$

Given answer obtained correctly

ALTERNATIVE METHOD:

 $T = \frac{200x}{4}$ B1

A1

5

$$100 - 2\left(\frac{200x}{4}\right) = 10v\frac{dv}{dx}$$
 M1

$$\frac{1}{2}v^2 = 10x - 5x^2$$
 (+C) A1
Use $x = 0$, $2 = 8g$ M1

$$^{2} = 10(8 + 2x - x^{2})$$
 A1

(ii)For using = 0 and factorizing or using formula method for solvingM1
$$x = 4$$
 (only)A12

Page 3			Mark Scheme	Syllabus	Paper	
			A AND AS LEVEL – JUNE 2004	9709/8719	5	
6 ((i)	2 =	$VT\sin 35^\circ - 5T^2$ or $2 = 25\tan 35^\circ - \frac{25^2 \times 10}{2V^2\cos^2 35^\circ}$	Ţ	I	B1
		25	= VTcos35°		F	B1
		For	obtaining V^2 or T^2 in $AV^2 = B$ or $CT^2 = D$ form where	e A,B,C,D are	ł	
		nur	nerical		r	M1
		[[(2	5tan35° – 2)cos²35°]V² = 3125 (aef) or			
		5 <i>T</i> 2	² = 25tan35° – 2 (aef)]			
		V=	17.3 or <i>T</i> = 1.76			A1
		T =	1.76 or <i>V</i> = 17.3 (ft <i>VT</i> = 30.519365)		I	B1 ft
((ii)	For	using $\dot{y} = V \sin 35^\circ - gT$ (must be compone	ent of V for M1) [M1
		\dot{y}_M	$(= 9.94 - 17.61 = -7.67) < 0 \rightarrow$ moving downwards		/	A1 ft
		(ft d	on V and T)			
		For	using $_{\rm M}^{2} = (V\cos 35^{\circ})^{2} + \dot{y}_{\rm M}^{2}$		r	M1
			$^{2} = ((14.20)^{2} + (-7.67)^{2})$ or		-	
		、…	using the principle of conservation of energy			
		$(\frac{1}{2})$	$m(v_M^2 - 17.3^2) = -mg \times 2$)			
		М	= 16.1 ms ⁻¹		/	A1
L	LINES	S 1	AND 2 ALTERNATIVE METHODS			
		ED	Compare 25 with $\frac{1}{2}R\left(\frac{1}{2}\frac{v^2\sin 70^\circ}{2}\right)$		1	M1
<u>1</u>			Compare 25 with $\frac{1}{2}K[\frac{1}{2}]$		I	VII

EITHER Compare 25 with
$$\frac{1}{2}R\left(\frac{1}{2}\frac{v \sin 70^{\circ}}{g}\right)$$
 M1

$$25 > 14.1 \rightarrow \text{moving downwards}$$
 A1

OR Compare 1.76 with time to greatest height
$$\left(\frac{V\sin 35^\circ}{g}\right)$$
 M1

$$1.76 > 0.994 \rightarrow moving downwards$$
 A1

OR
$$\frac{dy}{dx} = \tan 35^\circ - \frac{g.10}{V^2 \cos^2 35^\circ} (= -0.54)$$
 used M1

As
$$tan\phi$$
 is negative \rightarrow moving downwards A1

Page	4		Mark Scheme	Syllabus	Paper
		A AND	AS LEVEL – JUNE 2004	9709/8719	5
(i)	Tco	os60° = 0.5g	(<i>T</i> = 10)		В
	Fo	r applying Newton's	s 2^{nd} law horizontally and using a :	$=\frac{v^2}{r}$	М
	•	ust be a componen		7	
	T s	$\sin 60^\circ = \frac{0.5v^2}{0.15\sin 60^\circ}$	$\frac{1}{2}$ (for an equation in V ²)		A
		r substituting for T			Μ
	=	1.5			A
ALTI	ERN	ATIVELY:			
	<i>a</i> =	$=\frac{v^2}{0.15\sin 60^\circ}$			В
			s 2 nd law perpendicular to the strin	g	М
		ig cos30° = 0.5(acc	os60°)		A
		r substituting for a	(1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,		Μ
			5tan60°) (for an equation in V^2)		
	=	1.5			A
()	(-)	<i>T</i> · 450 0.5(0	.9) ²		
(ii)	(a)	$T\sin 45^\circ = \frac{0.5(0)}{0.15\sin^2}$	$\overline{n45^{\circ}}$		В
		Tension is 5.4 N			В
	(b)	For resolving forc	es vertically		М
		$5.4\cos 45^\circ + R = 0$).5g		A
		Force is 1.18 N			A

GCE A AND AS LEVEL AICE

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/06, 0390/06

MATHEMATICS Paper 6 (Probability and Statistics 1)



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1 (i) $\overline{x}_A = 139$ (138.75) $\sigma_A = 83.1$	B1 B1 2	For the mean For the sd
(ii) team B smaller standard deviation	B1 B1 dep 2	Independent mark Need the idea of spread SR If team A has a smaller sd then award B1only for 'teamA, smaller sd'
 2 (i) axes and labels points (3,0) (15,160) (20,320) (35,480) (60,640) 	B1 B1 B1 3	For correct uniform scales and labels on both axes, accept Frequency, %CF, Number of people, allow axes reversed, allow halves For 3 correct points All points correct and reasonable graph inc straight lines
(ii) accept 60 – 70 for straight lines 40 – 70 for curve	M1 A1 2	For subtracting from 640 can be implied For correct answer, reasonably compatible with graph
3 (i) x 1 2 3 4 5 6 P(X = x) $\frac{11}{36}$ $\frac{9}{36}$ $\frac{7}{36}$ $\frac{5}{36}$ $\frac{3}{36}$ $\frac{1}{36}$	M1 A1 A1 3	For 36 in the uncancelled denominator somewhere, accept decimals eg 0.305 recurring or 0.306 etc For 3 correct probabilities All correct
(ii) E(X) = $1 \times \frac{11}{36} + 2 \times \frac{9}{36} + 3 \times \frac{7}{36} + 4 \times \frac{5}{36} + 5 \times \frac{3}{36} + 6 \times \frac{1}{36} = \frac{91}{36}$	M1 A1 2	For calculation of $\sum xp$ where all probs < 1
4 (i) $z = \frac{350 - 450}{120}$ = -0.833 % small = 1 - 0.7975 = 0.2025 or 20.25%	M1 A1 A1 3	For standardising accept 120 or $\sqrt{120}$, no c For correct <i>z</i> value, + or -, accept 0.83 For answer rounding to 0.202 or 0.203
(ii) $0.7975 \div 2 = 0.39875$ each $\Phi z_2 = 0.60125$ $z_2 = 0.257$ $x = 120 \times 0.257 + 450$ = 481	M1 M1dep M1 M1dep A1 5	For dividing their remainder by 2 For adding their above two probs together or subt from 1 For finding the <i>z</i> corresponding to their probability For converting to <i>x</i> from a <i>z</i> value For answer, rounding to 481

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5	(a) (i) 3 ×5× ₃ C ₁ × ₅ = 90	3×2 or $_{5}C_{1} \times {}_{3}C_{1} \times 2$	M1 A1	2	For multiplying For correct ans			
	(ii) (3×5× = 69	2) + (3×3) + (5×2×3)	M1 M1 A1	3	For summing o S&M,S&D,M&I $3 \times 5 \times a + 3 \times$ for integers a,b For correct ans) 3× b + 5× ∶ b,c		I
((b) ₁₄ C ₅ × ₉ C ₅ = 252252	× ₄ C ₄ or equivalent	M1 M1 A1	3	For using com For multiplying groups For correct ans NB 14!/5!5!4! s correct answer	choices for swer scores M2 a	• two or thr	
6 ((i)	0.9 Win	B1		For top branch 0.1)	es correct (0.65, 0.9,	
	0.65 1 st in	0.1 Lose 0.6 Win	B1		For bottom bra 0.8, 0.2)	nches corre	ect (0.35,	
\leq	0.35 1 st out-	0.8 2 nd in 0.4 Lose	B1		For win/lose op 0.4)	otion after 2	nd in (0.6,	
		0.2 2 nd out Lose	B1	4	For all labels ir end of bottom l	0	al lose at	
	(ii) 0.65×0.1+ = 0.247	0.35×0.8×0.4 + 0.35×2	M1 M1 A1	3	For evaluating For 1 st out 2 nd i lose For correct ans	n lose, or 1	ose seen st out 2 nd o	out
((iii) $\frac{0.65 \times 0.1}{0.247}$		M1		For dividing the their answer to		l lose by	
	= 0.263	(= 5/19)	A1ft	2	For correct ans 0.65×0.1/their	•	on	

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7 (i) $P(0) = (0.8)^{15}$ (= 0.03518) $P(1) = {}_{15}C_1 \times (0.2) \times (0.8)^{14}$ (= 0.1319) $P(2) = {}_{15}C_2 \times (0.2)^2 \times (0.8)^{13}$ (= 0.2309) $P(X \le 2) = 0.398$	B1 B1 B1 3	For correct numerical expression for P(0) For correct numerical expression for P(1) or P(2) For answer rounding to 0.398
(ii) $1 - (0.8)^n \ge 0.85$ $0.15 \ge (0.8)^n$ n = 9	M1 M1 dep A1 3	For an equality/inequality involving 0.8, <i>n</i> , 0.85 For solving attempt (could be trial and error or lg) For correct answer
(iii) $\mu = 1600 \times 0.2 = 320$, $\sigma^2 = 1600 \times 0.2 \times 0.8 = 256$ P($X \ge 290$) or P(X<350) $= 1 - \Phi\left(\frac{289.5 - 320}{\sqrt{256}}\right) = 1 - \Phi(-1.906)$ $= \Phi(1.906) = 0.972$	B1 M1 M1 M1 A1 5	For both mean and variance correct For standardising , with or without cc, must have $$ on denom For use of continuity correction 289.5 or 290.5 For finding an area > 0.5 from their <i>z</i> For answer rounding to 0.972

GCE A AND AS LEVEL

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SYLLABUS/COMPONENT: 9709/07, 8719/07

MATHEMATICS AND HIGHER MATHEMATICS Paper 7 (Probability and Statistics 2)



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	= 15 or <i>p</i> = 0.25 > 15 or <i>p</i> > 0.25	B1	1	For H_0 and H_1 correct
(ii) Test s z = ± -	$\frac{21.5 - 15}{\sqrt{60 \times 0.25 \times 0.75}} = 1.938$	M1		For attempt at standardising with or without cc, must have $$ something with 60 in on the denom
	st statistic $\frac{\frac{22}{60} - \frac{0.5}{60} - \frac{15}{60}}{\sqrt{\frac{0.25 \times 0.75}{60}}} = 1.938$	A1		For 1.94 (1.938)
CV z =	1.645 Claim justified	M1 A1ft		For comparing with 1.645 or 1.96 if 2-tailed, signs consistent, or comparing areas to 5% For correct answer(ft only for correct one-tail
		Am	4	test)
Var = (= 3.5 + 2.9 + 3.1 = 9.5 $0.3^{2} + 0.25^{2} + 0.35^{2} (=0.275)$ = 0.524	B1 M1 A1	3	9.5 as final answer For summing three squared deviations For correct answer
or <i>z</i> =	$\frac{9-9.5}{\frac{1}{4}} = -1.907$ $\frac{1}{4} = -1.907$ $\frac{36-38}{\sqrt{4 \times their var}} = -1.907$ $\sqrt{4 \times their var}$ $\sqrt{1} = 0.9717 = 0.972$	M1 M1 A1	3	For standardising, no cc For $\sqrt{\frac{their \text{ var}}{4}}$ or $\sqrt{4 \times their}$ var) in denom - no 'mixed' methods. For correct answer
	Y) = 2E(X) –3E(Y) = 16 – 18	M1		For multiplying by 2 and 3 resp and subt
= - 2 (ii) Var (2. = 19.2 = 73.2	X-3 <i>Y</i>) = 4Var (<i>X</i>) +9Var (<i>Y</i>) + 54	A1 B1 M1 M1 A1	2	For correct answer For use of var (Y) = 6 For squaring 3 and 2 For adding variances (and nothing else) For correct final answer
4 (i) $\bar{x} = 375$ σ^{2}_{n-1}	5.3 = 8.29	B1 M1 A1	3	For correct mean (3.s.f) For legit method involving <i>n</i> -1, can be implied For correct answer
(ii) <i>p</i> = 0.1	9 or equiv.	B1		For correct p
0.19 ± 2	$.055 \times \sqrt{\frac{0.19 \times 0.81}{200}}$	M1		For correct form $p \pm z \times \sqrt{\frac{pq}{n}}$ either/both sides
	≤ <i>p</i> < 0.247	B1 A1	4	For $z = 2.054$ or 2.055 For correct answer

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5 (i) $\frac{c-54}{3.1/\sqrt{10}} = -1.282$	B1 M1	For + or – 1.282 seen For equality/inequality with their $z (\pm)$ (must have used tables), no $\sqrt{10}$ needed (c can be
$c = 54 - 1.282 \times \frac{3.1}{\sqrt{10}} = 52.74$	A1	numerical) For correct expression (c can be numerical,
V10	A1 4	but signs must be consistent) For correct GIVEN answer. No errors seen.
(11) P(-52.74) = 4 + 5(52.74 - 51.5)	B1	For identifying the outcome for a type II error
(ii) $P(\bar{x} > 52.74) = 1 - \Phi\left(\frac{52.74 - 51.5}{3.1/\sqrt{10}}\right)$ = $1 - \Phi(1.265) = 1 - 0.8971$	M1 A1	For standardising , no $\sqrt{10}$ needed For ± 1.265 (accept 1.26-1.27)
= 0.103 or 0.102	A1 4	For correct answer
6 (i) P(5) = $e^{-6} \times \frac{6^5}{5!} = 0.161$	M1	For an attempted Poisson P(5) calculation,
5!	A1 2	any mean For correct answer
(ii) $P(X \ge 2) = 1 - \{P(0) + P(1)\}$ = 1 - $e^{-1.6}(1+1.6)$	B1 M1	For μ = 1.6, evaluated in a Poisson prob For 1 – P(0) – P(1) or 1 – P(0) – P(1) – P(2)
= 0.475	A1 3	For correct answer
(iii)	M1	For multiplying P(1) by P(4) any (consistent) mean
P(1 then 4 5) = $\frac{(e^{-3} \times 3) \times (e^{-3} \times \frac{3^4}{4!})}{e^{-6} \times \frac{6^5}{4!}}$	M1	For dividing by P(5) any mean
5!	A1 3	For correct answer
= 0.156 or 5/32		
7 (i) $c \int_{0}^{5} t(25-t^2) dt = 1$	M1	For equating to 1 and a sensible attempt to integrate
$c\left[\frac{25t^2}{2} - \frac{t^4}{4}\right]_0^5 = 1$	A1	For correct integration and correct limits
$c\left[\frac{625}{2} - \frac{625}{4}\right] = 1 \implies c = \frac{4}{625}$	A1 3	For given answer correctly obtained
4 Γ ₂₅ .2.4 ¹⁴	M1*	For attempting to integrate $f(t)$ between 2
(ii) $\int_{2}^{4} ct(25-t^2) dt = \left[\frac{25ct^2}{2} - \frac{ct^4}{4}\right]_{2}^{4} = c[136] - c[46]$		and 4 (or attempt 2 and 4)
$=\frac{72}{125}$ (0.576)	M1*dep	For subtracting their value when t = 2 from their value when t = 4
125 (0.070)	A1 3	For correct answer
(iii) $\int_{0}^{5} ct^{2}(25-t^{2}) dt = \left[\frac{4}{625} \times \frac{25t^{3}}{3} - \frac{4}{625} \times \frac{t^{5}}{5}\right]_{0}^{5}$	M1*	For attempting to integrate <i>t</i> f(<i>t</i>), no limits needed
0	A1 M1*dop	For correct integrand can have c (or their c)
$=\frac{8}{3}$	M1*dep	For subtracting their value when t=0 from their value when t=5
	A1 4	For correct answer