MARK SCHEME for the May/June 2012 question paper

for the guidance of teachers

9709 MATHEMATICS

9709/11

Paper 1, maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• Cambridge will not enter into discussions or correspondence in connection with these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2012 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

Page 2	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2012	9709	11

Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

Page 3	Page 3 Mark Scheme: Teachers' version		Paper
	GCE AS/A LEVEL – May/June 2012	9709	11

The following abbreviations may be used in a mark scheme or used on the scripts:

- AEF Any Equivalent Form (of answer is equally acceptable)
- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- CWO Correct Working Only often written by a 'fortuitous' answer
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)
- SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures - this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

	Page 4	Mark Scheme: Teachers	Syllabus 9709	Paper				
		GCE AS/A LEVEL – May/	GCE AS/A LEVEL – May/June 2012			11		
1	$\tan 2x = 2$ 2x = 63.4 or 24 x = 31.7 or 121		M1 A1 A1A1√ [↑]	4] C	1 solution sufficient For 2^{nd} A1 allow 90 + 1 st soln prov. only 2 solns in range. Alt methods possible 2 elements correct, 3 rd element correct 2 elements correct. Identifying reqd term SC B3 for [560(x) ⁶] as answer			
2	$[7C3] \times [(2x^3)^4]$ 35 × 2 ⁴ × (-1) ³ -560(x ⁶) as an	$[(-1/x^2)^3]$ seen soi beading to their answer soi swer	B1B1 B1 B1	2 t				
3		$\overline{3}$ (or area $\triangle AQC = \frac{\sqrt{3}}{2}$) $PR = \frac{1}{2} (\sqrt{3})^2 \times \frac{\pi}{3} = \frac{\pi}{2}$	B1 B1√ ^h M1A1√ ^h	s f	soi Allow 1.73 soi ft <i>their</i> $\sqrt{3}$ Allow 1.73 ft <i>their</i> $\sqrt{3}$. Allow 1.57. SCA1 for $\pi/7$ from $\frac{1}{2}(\sqrt{3})^2 \times \frac{\pi}{6}$ provided $\Delta = \frac{\sqrt{3}}{2}$			
	Shaded region	$= \sqrt{3} - \frac{\pi}{2} \text{oe cao}$	A1	5]	2 (11) 6	2		
4	$\left(\frac{\mathrm{d}M}{\mathrm{d}r}\right) = 3kr^2$	$k = \frac{3.2}{1000}$ or $\frac{2}{625}$ or 0.0032 oe $\frac{h}{h}$ used e.g. $3 \times k \times 10^2 \times 0.1$	M1A1 B1 M1 A1	C	Must eventually make ao. Non-calculus mo 0.09696) can score or	ethods (e.g. \rightarrow		
5	$(3\sqrt{x}-2)$ $\sqrt{x} = \frac{2}{3} \text{ or}$ $x = \frac{4}{9} \text{ or}$ $OR (6x+2)^2$ $(9x-4)(4)$	$\frac{1}{4} \text{ (or } 0.444, 0.25)$ $= 49x \rightarrow 36x^2 - 25x + 4 = 0$	M1 M1 A1 A1 M1A1 M1 A1	C 1 H H	Expressing as a clear be e.g. $(3t - 2)(2t - 1)$ solution sufficient. Both solutions require Attempt to square bot Attempt to solve (or f	= 0 Accept e.g. $t = 2/3$ ed cao th sides		
	uл		M1 A1 M1 A1	ł	Apply $b^2 - 4ac(=0)$ Attempt to equate der	rivatives		

	Page 5	Mark Scheme: Teachers' version				Syllabus Pape		
		GCE AS/A LEVEL – May/June 20				9709	11	
6	(i) $2p^2 - 2p + 2 + 12p + 6 \rightarrow 2p^2 + 10p + 8$ u.v = 0 $(p+1)(p+4) = 0 \rightarrow p = -1$ or $p = -4$			[3]	Scala	Correct method for scalar product Scalar product = 0 cao Both solutions required		
	$20 = \sqrt{41}$	0 + 18 = 20 $\overline{41} \text{ or } \mathbf{v} = \sqrt{13}$ $\times \sqrt{13} \times \cos \theta \text{ oe}$ or 0.523 rads	M1 M1 M1 A1	[4]	Corre	of $x_1x_2 + y_1y_2 + z_1$ ect method for mo onnected correctl	oduli	
7	(a) $S_{10} = \frac{1}{2[2]}$ $S_{10} = 5[2 - S_{10}]$ $S_{10} = 10 - 5$	$-9\sin^2 x$]	M1 M1 A1	[3]	Use o	ect formula with of $c^2 + s^2 = 1$ in a = 10, b = 45		
		$<)\frac{1}{3}\tan^2\theta < 1$ oe $<)\theta < \frac{\pi}{3}$	M1 A1	[2]	Allow	w < Allow <		
		$= \frac{1}{1 - \frac{1}{3} \tan^2 \frac{\pi}{6}}$ = $\frac{9}{8}$ or 1.125	M1 A1	[2]	cao			
8	(i) $(x-2)^2 -$	4 + <i>k</i>	B1B1	[2]	a =	2, <i>b</i> = -4		
	(ii) $f(x) > k - 4$	or $[k-4, \infty]$ or $(k-4, \infty)$ oe	B1 √	[1]	ft the	<i>ir k</i> -4 . Accept	>	
	(iii) smallest v	alue of $p = 2$	B1 √	[1]	ft the	ir 2		
		$\frac{1}{y+4-k}$ + $\sqrt{x+4-k}$ s x > k-4 or [k-4, ∞]	M1 A1√ ^k A1 B1√ ^k	[4]	cao	m <i>their</i> part (i) m <i>their</i> part (ii).	Accept >	

Page 6			Mark Scheme: Teachers' version				Syllabus	Paper		
GCE AS/A LEVEL – May/June 2				June 20	12		9709	11		
9	9 (i) $M = (1, 4)$ gradient $= \frac{1}{2}$ soi grad of $MB = -2$ soi			B1B1 M1		Use				
	Equation $MB: y - 4 = -2(x - 1)$ When $y = 0, x = 3$ or $B = (3, 0)$			A1√ [≜] A1√ [≜]	[5]	Or $y = -2x + 6$ ft on <i>their</i> $\frac{1}{2}$ or <i>M</i> ft result of putting $y = 0$ into <i>their</i> eqn				
	(ii)		$B = -\frac{2}{6}$; grad of $BC = \frac{6}{2}$ oe	M1√			At least one correct $ eq^{h}$			
		$m_1 m_2 = -$	$l(\Rightarrow AB \perp AC)$	A1	[2]	AG	Allow omitted c	onclusion		
	· · ·	$D = (-1, 8)$ $AD = \sqrt{40}$		B1 B1	[2]					
10	(i)		$3x^{2} - 4x + 1 (<)5$ (3x + 2)(x - 2) < 0 M1 M1				mpt differentiate of mpt to factorise of	•		
		$-\frac{2}{3} < x <$ Allow <	2 or $\left[-\frac{2}{3}, 2\right]$ or $\left(-\frac{2}{3}, 2\right)$.	A2	[4]	SC A	Allow A1 for $-\frac{2}{3}$	and 2 seen		
	(ii)		$-1 = 0 \Longrightarrow (3x - 1)(x - 1) = 0$	M1		Deri	vative = 0 & <u>any</u>	attempt to solve		
		$x = \frac{1}{3}$ or 1	l	A1		Both				
		$y = \frac{4}{27} $ or	r 0	A1		Both				
		f''(x) = 6x	$-4 \rightarrow f''\left(\frac{1}{3}\right) = -2 \ (<0);$							
		f''(1) = 2 (M1		Or of	ther valid method			
		max at $\left(\frac{1}{3}\right)$	$\left(\frac{4}{27}\right); \text{ min at } (1, 0) \text{ cao}$	A1	[5]		w just x values or n for identification	• •		

Page 7 Mark Scheme: Teachers' version						Syllabus	Paper
GCE AS/A LEVEL – May/June 2012						9709	11
11	(i) $x = -\frac{1}{y}$	$\frac{4}{y^2} - 1$	B1	[1]	AG	At least 1 step of	f working needed
	(ii) $\int \left(\frac{4}{y^2}\right)^2$	$\frac{4}{2} - 1 dy = \left[-\frac{4}{y} - y \right]$	B1B1				
	Uppe	er limit = 2	B1		For -	$-\frac{4}{v}, -y$	
	$\left[\left(-\frac{2}{2}\right)\right]$	$\left(\frac{4}{2}-2\right)-(-4-1)$	M1		Appl	y limits 1 and <i>the</i>	
	1		A1	[5]	SC B	2 for $\int 2(x+1)^{-\frac{1}{2}}$	$dx - 3 \rightarrow 1$
	(iii) (π)∫	$x^{2} dy = (\pi) \int \left(\frac{16}{y^{4}} - \frac{8}{y^{2}} + 1 \right) dy$	B1B1				
	$(\pi)\left[-\frac{1}{2}\right]$	$\frac{-16}{3y^3} + \frac{8}{y} + y$	B1				
	$(\pi) \Big[\Big($	$\left(\frac{-16}{24} + 4 + 2\right) - \left(\frac{-16}{3} + 8 + 1\right)$	M1		Appl	y limits 1 and <i>the</i>	vir 2 'correctly'
	$\frac{5\pi}{3}$		A1	[5]			