MARK SCHEME for the May/June 2013 series

9709 MATHEMATICS

9709/21

Paper 2, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.



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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

- AEF Any Equivalent Form (of answer is equally acceptable)
- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- CWO Correct Working Only often written by a "fortuitous" answer
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)
- SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR–2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

1	Eith	ge 4	Mark Scheme GCE AS LEVEL – May/June 2013	Syllabus 9709		
1	Eith				Paper 21	
		<u>er</u> State Obta	g pair of equat	tions M1 A1		
	State answer 3			B1		
		Use logarithmic method to solve an equation of the form $2^x = k$, where $k > 0$ State answer 2.58 Or State or imply one value for 2^x , e.g. 8, by solving an equation or by inspection State answer 3		ere $k > 0$	M1	
					A1	
	<u>Or</u>			nspection	B1 B1	
			second value for 2^x		B1	
			logarithmic method to solve an equation of the form $2^x = k$, wh	ere $k > 0$	M1	
			answer 2.58		A1	[5]
2	Use	$2\ln x = \ln x$	(x^2)		M1	
			dition or subtraction of logarithms		M1	
			quadratic equation in x		A1	
			ble solution attempt at a 3-term quadratic previous M marks)		DM1	
	State	$x = \frac{3}{5}$ and	d no other solutions		A1	[5]
3	(i)	Either				
	()	Use sin 2.	$x = 2\sin x \cos x \text{ to convert integrand to } k \sin^2 2x$ $x = 1 - 2\sin^2 2x$		M1 M1	
			ect expression $\frac{1}{2} - \frac{1}{2}\cos 4x$ or equivalent		A1	
		\underline{Or} Use \cos^2	$x = \frac{1 - \cos 2x}{2}$ and/or $x = \frac{1 - \cos 2x}{2}$ to obtain an equation in co	$\cos 2x$ only	M1	
		Use cos ²	$2x = \frac{1 + \cos 4x}{2}$		M1	
		State corr	ect expression $\frac{1}{2} - \frac{1}{2}\cos 4x$ or equivalent		A1	[3]
	(ii)	State corr	ect integral $\frac{3}{2}x - \frac{3}{8}\sin 4x$, or equivalent		B1	
			o substitute limits, using exact values		M1	
		-	ven answer correctly		A1	[3]
4		Substitut	3 agusta ta gara		N <i>I</i> 1	
4	(i)	Substitute	$x = -\frac{3}{2}$, equate to zero		M1	
			x = -1 and equate to 8		M1	
			correct equation in any form		A1	
			elevant pair of equations for <i>a</i> or for <i>b</i> = 2 and $b = -6$		M1	۲ <i>4</i> ٦
			$-2 \operatorname{and} v = 0$		A1	[5]

Page 5		ge 5	Mark Scheme	Syllabus	Paper	r
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	(ii)	observatio Obtain qu Obtain lin [Condone	either division by $2x + 3$ and reach a partial quotient of $x^2 + 5$ notient $x^2 - 4x + 3$ near factors $x - 1$ and $x - 3$ e omission of repetition that $2x + 3$ is a factor.] factors $x - 1$, $x - 3$ obtained by remainder theorem or inspecti		M1 A1 A1	[3]
5	(i)	Obtain co $Use \ \frac{dy}{dx} =$	act rule to differentiate y prrect derivative in any form $\frac{dy}{dt} \div \frac{dx}{dt}$ ven answer correctly		M1 A1 M1 A1	[4]
	(ii)	Obtain $\frac{dy}{dy}$ Form equ	e $t = 0$ in $\frac{dy}{dx}$ and both parametric equations $\frac{y}{x} = 2$ and coordinates (1, 0) ation of the normal at their point, using negative reciprocal of vect equation of normal $y = -\frac{1}{2}x + \frac{1}{2}$ or equivalent	Their $\frac{dy}{dx}$	B1 B1 M1 A1	[4]
6	(i)		ecognisable sketch of a relevant graph, e.g. $y = \cot x$ or $y = 4x$ second relevant graph and justify the given statement	z – 2	B1 B1	[2]
	(ii)		sign of $4x - 2 - \cot x$ at $x = 0.7$ and $x = 0.9$, or equivalent the argument correctly with appropriate calculations		M1 A1	[2]
	(iii)	Show that	t given equation is equivalent to $x = \frac{1 + 2 \tan x}{4 \tan x}$, or vice versa		B1	[1]
	(iv)		erative formula correctly at least once nal answer 0.76		M1 A1	
			ficient iterations to justify its accuracy to 2 d.p. or show there erval (0.755, 0.765)	is a sign change	B1	[3]

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7	(i)	State $R =$	$\sqrt{29}$		B1	
,	(1)		formula to find α		M1	
		Obtain α	$=21.80^{\circ}$ with no errors seen		A1	[3]
	(ii)	Carry out	evaluation of $\sin^{-1}\left(\frac{4}{R}\right) (\approx 47.97^{\circ})$		M1	
		Carry out	correct method for one correct answer		M1	
		Obtain or	e correct answer e.g. 13.1°		A1	
			correct method for a further answer		M1	
		Obtain re	maining 3 answers 55.1° , 193.1° , 235.1° and no others in t	he range	A1	[5]
	(iii)	Greatest	value of $10 \sin 2\theta + 4 \cos 2\theta = 2\sqrt{29}$		M1	
		$\frac{1}{116}$			A1	[2]

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