## MARK SCHEME for the October/November 2013 series

## 9709 MATHEMATICS

9709/32

Paper 3, maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.



Page 2	Mark Scheme	Syllabus	Paper
	GCE A LEVEL – October/November 2013	9709	32

## Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

Page 3	Mark Scheme	Syllabus	Paper
	GCE A LEVEL – October/November 2013	9709	32

The following abbreviations may be used in a mark scheme or used on the scripts:

- AEF Any Equivalent Form (of answer is equally acceptable)
- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- CWO Correct Working Only often written by a 'fortuitous' answer
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)
- SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

## **Penalties**

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

	Page 4	Mark Scheme Sylla		us Paper	
		GCE A LEVEL – October/November 2013	9709	32	
1	Use correct q Obtain correc Justify the give	uotient or product rule et derivative in any form ven statement		M1 A1 A1	[3]
2	<i>EITHER:</i> Stat 2(3	the or imply non-modular equation $2^2(3^x - 1)^2 = (3^x)^2$ , or pair $a^x - 1 = \pm 3^x$	r of equations	M1	
	Obt	ain $3^x = 2$ and $3^x = \frac{2}{3}$ (or $3^{x+1} = 2$ )		A1	
	OR: Obt	ain $3^x = 2$ by solving an equation or by inspection		B1	
	Obt	ain $3^x = \frac{2}{3}$ (or $3^{x+1} = 2$ ) by solving an equation or by inspect	ion	B1	
	Use correct n Obtain final a	nethod for solving an equation of the form $3^x = a$ (or $3^{x+1} = a$ ) inswers 0.631 and -0.369	), where $a > 0$	M1 A1	[4]
3	EITHER: Inte	grate by parts and reach $kx^{\frac{1}{2}} \ln x - m \int x^{\frac{1}{2}} \cdot \frac{1}{x} dx$		M1*	
	Obt	ain $2x^{\frac{1}{2}} \ln x - 2 \int \frac{1}{x^{\frac{1}{2}}} dx$ , or equivalent		A1	
	Inte Sub Obt	egrate again and obtain $2x^{\frac{1}{2}} \ln x - 4x^{\frac{1}{2}}$ , or equivalent stitute limits $x = 1$ and $x = 4$ , having integrated twice ain answer $4(\ln 4 - 1)$ , or exact equivalent		A1 M1(dep*) A1	
	OR1: Usi	ng $u = \ln x$ , or equivalent, integrate by parts and reach $kue^{\frac{1}{2}u}$	$-m\int e^{\frac{1}{2}u}du$	M1*	
	Obt	ain $2ue^{\frac{1}{2}u} - 2\int e^{\frac{1}{2}u} du$ , or equivalent		A1	
	Inte Sub Obt	grate again and obtain $2ue^{\frac{1}{2}u} - 4e^{\frac{1}{2}u}$ , or equivalent stitute limits $u = 0$ and $u = \ln 4$ , having integrated twice ain answer $4\ln 4 - 4$ , or exact equivalent		A1 M1(dep*) A1	
	OR2: Usi	ng $u = \sqrt{x}$ , or equivalent, integrate and obtain $ku \ln u - m \int u$ .	$\frac{1}{u}$ du	M1*	
	Obt	ain $4u \ln u - 4 \int 1 du$ , or equivalent		A1	
	Inte	grate again and obtain $4u \ln u - 4u$ , or equivalent		A1	
	Sub	stitute limits $u = 1$ and $u = 2$ , having integrated twice or quo	ted $\int \ln u  \mathrm{d}u$		
	as <i>i</i> Obt	$u \ln u \pm u$ ain answer $8 \ln 2 - 4$ or exact equivalent		$M1(dep^*)$	
	OR3: Inte	grate by parts and reach $I = \frac{x \ln x \pm x}{\sqrt{x}} + k \int \frac{x \ln x \pm x}{x \sqrt{x}} dx$		M1*	
	Obt	ain $I = \frac{x \ln x - x}{\sqrt{x}} + \frac{1}{2}I - \frac{1}{2}\int \frac{1}{\sqrt{x}} dx$		A1	
	Inte Sub Obt	grate and obtain $I = 2\sqrt{x} \ln x - 4\sqrt{x}$ , or equivalent stitute limits $x = 1$ and $x = 4$ , having integrated twice ain answer $4 \ln 4 - 4$ , or exact equivalent		A1 M1(dep*) A1	[5]

	Page 5	Mark Scheme	Syllabus	Paper	
	-	GCE A LEVEL – October/November 2013	9709	32	
4	Use correc	et product or quotient rule at least once		M1*	
	Obtain $\frac{dx}{dt}$	$\frac{dy}{dt} = e^{-t} \sin t - e^{-t} \cos t$ or $\frac{dy}{dt} = e^{-t} \cos t - e^{-t} \sin t$ , or equivalent		A1	
	Use $\frac{dy}{dx} = -$	$\frac{\mathrm{d}y}{\mathrm{d}t} \div \frac{\mathrm{d}x}{\mathrm{d}t}$		M1	
	Obtain $\frac{dy}{dx}$	$\frac{dt}{dt} = \frac{\sin t - \cos t}{\sin t + \cos t}$ , or equivalent		A1	
	EITHER: H	Express $\frac{dy}{dx}$ in terms of tan <i>t</i> only	N	[1(dep*)	
	S	Show expression is identical to $\tan\left(t - \frac{1}{4}\pi\right)$		A1	
	OR: H	Express $\tan\left(t - \frac{1}{4}\pi\right)$ in terms of $\tan t$		M1	
	S	Show expression is identical to $\frac{dy}{dx}$		A1	[6]
5	(i) ( ( (	Use Pythagoras Use the sin2A formula Obtain the given result		M1 M1 A1	[3]
	<b>(ii)</b> I	Integrate and obtain a $k \ln \sin \theta$ or $m \ln \cos \theta$ term, or obtain $p \ln \tan \theta$	n integral of the for	m M1*	
	(	Obtain indefinite integral $\frac{1}{2}\ln\sin\theta - \frac{1}{2}\ln\cos\theta$ , or equivalent,	or $\frac{1}{2}$ ln tan $\theta$	A1	
	2	Substitute limits correctly Obtain the given answer correctly having shown appropriate w	orking	[1(dep)* A1	[4]
6	(i) 5 U U S (	State or imply $AB = 2r\cos\theta$ or $AB^2 = 2r^2 - 2r^2\cos(\pi - 2\theta)$ Use correct formula to express the area of sector <i>ABC</i> in terms Use correct area formulae to express the area of a segment in terms State a correct equation in <i>r</i> and $\theta$ in any form Obtain the given answer (SR: If the complete equation is approached by adding two area above <i>BO</i> and <i>OC</i> give the first M1 as on the schem for using correct area formulae for a triangle <i>AOB</i> or <i>A</i> or <i>AOC</i> .]	of r and $\theta$ erms of r and $\theta$ sectors to the shade ne, and the second N OC, and a sector AC	B1 M1 M1 A1 A1 ed [1] DB	[5]
	(ii) U ( S	Use the iterative formula correctly at least once Obtain final answer 0.95 Show sufficient iterations to 4 d.p. to justify 0.95 to 2 d.p., o change in the interval (0.945, 0.955)	r show there is a sig	M1 A1 gn A1	[3]

	Page 6		Mark Scheme Syllabus		Paper	
			GCE A LEVEL – October/November 2013	9709	32	
7	(i)	State Use Obta Obta Obta	e or imply partial fractions are of the form $\frac{A}{x-2} + \frac{Bx+C}{x^2+3}$ a relevant method to determine a constant in one of the values $A = -1$ , $B = 3$ , $C = -1$ in a second value in the third value		B1 M1 A1 A1 A1	[5]
	(ii)	Use	correct method to obtain the first two terms of the expansion	ansions of $(x-2)$	<sup>-1</sup> ,	
		$\left(1-\right)$	$\left(\frac{1}{2}x\right)^{-1}$ , $\left(x^2+3\right)^{-1}$ or $\left(1+\frac{1}{3}x^2\right)^{-1}$	n in r <sup>2</sup> into ea	M1	
		parti Mult	al fraction iply out fully by $Bx + C$ , where $BC \neq 0$	A	1√+A1√ M1	
		Obta	in final answer $\frac{1}{6} + \frac{5}{4}x + \frac{17}{72}x^2$ , or equivalent		A1	[5]
		[Syn on A [In t for tl [If E M1A	anbolic binomial coefficients, e.g. $\begin{pmatrix} -1 \\ 1 \end{pmatrix}$ are not sufficient for $B, C.$ ] he case of an attempt to expand $(2x^2 - 7x - 1)(x - 2)^{-1}(x^2 + 1)^{-1}(x - 2)^{-1}(x - 2$	for the M1. The f.t. $(-3)^{-1}$ , give M1A1. final answer.] 0M1A0A0A0 in (	. is A1 ( <b>i</b> );	
8	(a) EII	THER:	Solve for <i>u</i> or for <i>v</i>		M1	
			Obtain $u = \frac{2i-6}{1-2i}$ or $v = \frac{5}{1-2i}$ , or equivalent		A1	
			<i>Either</i> : Multiply a numerator and denominator by conjug	gate of denominat	or,	
	OP	<b>.</b>	<i>Or:</i> Set <i>u</i> or <i>v</i> equal to $x + iy$ , obtain two equations b imaginary parts and solve for <i>x</i> or for <i>y</i> . Using $a + ib$ and $c + id$ for <i>u</i> and <i>v</i> equate real and imaging	y equating real a	nd M1	
	UK.		four equations in a, b, c and d Obtain $b + 2d = 2$ , $a + 2c = 0$ , $a + d = 0$ and $-b + c = 3$ , or Solve for one unknown	equivalent	M1 A1 M1	
	Ob Ob	tain fii tain fii	hal answer $u = -2$ –2i, or equivalent hal answer $v = 1 + 2i$ , or equivalent		A1 A1	[5]
	(b) Sho Sho	ow a c ow a c	ircle with centre –i ircle with radius l		B1 B1	
	She	ow cor	rect half line from 2 at an angle of $\frac{3}{4}\pi$ to the real axis		B1	
	Use	e a cor	rect method for finding the least value of the modulus		M1	
	Ob	tain fii	hal answer $\frac{5}{\sqrt{2}}$ -1, or equivalent, e.g. 1.12 (allow 1.1)		A1	[5]

	Page 7	Mark Scheme	Syllabus	Paper	•
		GCE A LEVEL – October/November 2013	9709	32	
0	(i) FIT	$HER$ : Obtain a vector parallel to the plane, e.g. $\overrightarrow{AR} = -2\mathbf{i} + A$	i_k	<b>B</b> 1	
,	(1) LIII	TEX. Obtain a vector parametric the plane, e.g. $AB = -21 + 4$ .	J = K	_0	
		Use scalar product to obtain an equation in <i>a</i> , <i>b</i> , <i>c</i> , e. 3a - 3b + 3a = 0 or $a + b + 2a = 0$	.g. $-2a+4b-c =$	=U, M1	
		Obtain two correct equations in $a$ $b$ $c$		A 1	
		Solve to obtain ratio $a : b : c$		M1	
		Obtain $a:b:c=3:1:-2$ , or equivalent		Al	
		Obtain equation $3x + y - 2z = 1$ , or equivalent		A1	
	ORI	: Substitute for two points, e.g. A and B, and ob	tain $2a-b+2c=$	= <i>d</i>	
		and $3b + c = d$		B1	
		Substitute for another point, e.g. C, to obtain a third eq	uation and elimin	ate	
		one unknown entirely from the three equations	-	M1	
		Obtain two correct equations in three unknowns, e.g. ir	n <i>a, b, c</i>	Al	
		Solve to obtain their ratio, e.g. $a:b:c$ Obtain $a:b:a-2:1:2$ $a:a:d-2:2:1$	$a \cdot b \cdot d = 2 \cdot 1 \cdot 1$	MI	
		Obtain $a:b:c=5.12$ , $a:c:a=52.1$ , $a:b:c:d=-1:-2:1$	$a \cdot b \cdot a = 5 \cdot 1 \cdot 1$		
		$v \cdot c \cdot a = -1 \cdot -2 \cdot 1$ Obtain equation $3x + y = 2z - 1$ or equivalent		Α1 Δ1	
		$\overrightarrow{y} = 22 = 1, \text{ or equivalent}$			
	OR2	C: Obtain a vector parallel to the plane, e.g. $BC = 3i - 3j + 3j$	- 3 <b>k</b>	BI	
		Obtain a second such vector and calculate their vector j	product		
		e.g. $(-2\mathbf{i}+4\mathbf{j}-\mathbf{k})\times(3\mathbf{i}-3\mathbf{j}+3\mathbf{k})$		M1	
		Obtain two correct components of the product		A1	
		Obtain correct answer, e.g. $9i + 3j - 6k$		B1 -c=0, M1 A1 A1 A1 A1 A1 A1 A1 A1 A1 A	
		Substitute in $9x + 3y - 6z = d$ to find d		MI	
		Obtain equation $9x + 3y - 6z = 3$ , or equivalent		Al	
	OR3	C: Obtain a vector parallel to the plane, e.g. $\overrightarrow{AC} = \mathbf{i} + \mathbf{j} + 2$	k	B1	
		Obtain a second such vector and form correctly a 2-pa	rameter equation	for	
		the plane	-	M1	
		Obtain a correct equation, e.g. $\mathbf{r} = 3\mathbf{i} + 4\mathbf{k} + \lambda(-2\mathbf{i} + 4\mathbf{j})$	$(-\mathbf{k}) + \mu(\mathbf{i} + \mathbf{j} + 2\mathbf{k})$	a) A1	
		State three correct equations in $x, y, z, \lambda, \mu$		A1	
		Eliminate $\lambda$ and $\mu$		M1	
		Obtain equation $3x + y - 2z = 1$ , or equivalent		A1	[6]
	(ii) Obta	ain answer $\mathbf{i} + 2\mathbf{j} + 2\mathbf{k}$ , or equivalent		B1	[1]

Page 8		Mark Scheme	Syllabus	Paper
		GCE A LEVEL – October/November 2013	9709	32
(iii)	EITH	<i>ER</i> : Use $\frac{\overrightarrow{OA}.\overrightarrow{OD}}{\left \overrightarrow{OD}\right }$ to find projection <i>ON</i> of <i>OA</i> onto <i>OD</i>		M1
		Obtain $ON = \frac{4}{3}$		A1
		Use Pythagoras in triangle <i>OAN</i> to find <i>AN</i> Obtain the given answer		M1 A1
	OR1:	Calculate the vector product of $\overrightarrow{OA}$ and $\overrightarrow{OD}$ Obtain answer $6\mathbf{i} + 2\mathbf{j} - 5\mathbf{k}$		M1 A1
	OR2:	Divide the modulus of the vector product by the modul Obtain the given answer Taking general point <i>P</i> of <i>OD</i> to have position vector	lus of $\overrightarrow{OD}$ $\lambda(\mathbf{i}+2\mathbf{j}+2\mathbf{k})$ , forr	M1 A1 m
		an equation in $\lambda$ by either equating the scalar produc	t of $\overrightarrow{AP}$ and $\overrightarrow{OP}$ t	0
		zero, or using Pythagoras in triangle <i>OPA</i> , or setting the	the derivative of $\left  \overline{AF} \right $	5
		to zero		M1
		Solve and obtain $\lambda = \frac{4}{9}$		A1
		Carry out method to calculate <i>AP</i> when $\lambda = \frac{4}{9}$		M1
	OR3:	Obtain the given answer Use a relevant scalar product to find the cosine of <i>AOL</i>	O or ADO	A1 M1
		Obtain $\cos AOD = \frac{4}{9}$ or $\cos ADO = \frac{5}{3\sqrt{10}}$ , or equivale	ent	A1
	OR1.	Use trig to find the length of the perpendicular Obtain the given answer Use cosine formula in triangle 40D to find cos 40D o	$r\cos 4DQ$	M1 A1 M1
	01.4.	Obtain $\cos AOD = \frac{8}{18}$ or $\cos ADO = \frac{10}{6\sqrt{10}}$ , or equiva	lent	A1
		Use trig to find the length of the perpendicular		M1
		Obtain the given answer		A1 [4]
(i)	State	or imply $V = \pi h^3$		B1
	State	or imply $\frac{\mathrm{d}V}{\mathrm{d}t} = -k\sqrt{h}$		B1
	Use -	$\frac{\mathrm{d}V}{\mathrm{d}t} = \frac{\mathrm{d}V}{\mathrm{d}h} \cdot \frac{\mathrm{d}h}{\mathrm{d}t}$ , or equivalent		M1
	Obtai	n the given equation		A1 [4]
	[The	M1 is only available if $\frac{dV}{dh}$ is in terms of h and has	been obtained by	a
	corre	ct method.]		
	[Allo	w B1 for $\frac{dv}{dt} = k\sqrt{h}$ but withhold the final A1 until the po	larity of the constar	nt
	$\frac{k}{3\pi}$ l	has been justified.]		
	(iii) (i)	Page o(iii) $EITH$ (iii) $EITH$ $OR1:$ $OR1:$ $OR2:$ $OR2:$ $OR3:$ $OR3:$ $OR3:$ $OR4:$ $OR$	<b>r dge oMark SchemeGCE A LEVEL – October/November 2013</b> (iii) EITHER: Use $\frac{\overline{O4}.\overline{OD}}{ \overline{OD} }$ to find projection ON of OA onto ODObtain $ON = \frac{4}{3}$ Use Pythagoras in triangle OAN to find ANObtain the given answerOR1: Calculate the vector product of $\overline{O4}$ and $\overline{OD}$ Obtain the given answerOR2: Taking general point P of OD to have position vectora equation in $\lambda$ by either equating the scalar productzero, or using Pythagoras in triangle OPA, or setting the to zeroSolve and obtain $\lambda = \frac{4}{9}$ Obtain the given answerOR3: Use a relevant scalar product to find the cosine of AODObtain the given answerOR3: Use a relevant scalar product to find the cosine of AODObtain the given answerOR3: Use a relevant scalar product to find the cosine of AODObtain the given answerOR3: Use a relevant scalar product to find the cosine of AODObtain the given answerOR4: Use cosine formula in triangle ADD to find cos AOD on the given answerOR4: Use cosine formula in triangle ADD to find cos ADD on $\frac{5}{3\sqrt{10}}$ , or equivaleUse trig to find the length of the perpendicularObtain the given answerOR4: Use cosine formula in triangle ADD to find cos ADD on $\frac{8}{18}$ or cos $ADO = \frac{10}{6\sqrt{10}}$ , or equivaleUse trig to find the length of th	<b>(iii)</b> EITHER: Use $\frac{\overline{OA},\overline{OD}}{ \overline{OD} }$ to find projection <i>ON</i> of <i>OA</i> onto <i>OD</i> Obtain <i>ON</i> = $\frac{4}{3}$ Use Pythagoras in triangle <i>OAN</i> to find <i>AN</i> Obtain the given answer <i>OR1:</i> Calculate the vector product of $\overline{OA}$ and $\overline{OD}$ Obtain the given answer <i>OR2:</i> Calculate the vector product of $\overline{OA}$ and $\overline{OD}$ Obtain the given answer <i>OR2:</i> Taking general point <i>P</i> of <i>OD</i> to have position vector $\lambda(i+2j+2k)$ , for an equation in $\lambda$ by either equating the scalar product of $\overline{AP}$ and $\overline{OP}$ to zero, or using Pythagoras in triangle <i>OPA</i> , or setting the derivative of $ \overline{AI} $ to zero Solve and obtain $\lambda = \frac{4}{9}$ Carry out method to calculate <i>AP</i> when $\lambda = \frac{4}{9}$ Obtain the given answer <i>OR3:</i> Use a relevant scalar product to find the cosine of <i>AOD</i> or <i>ADO</i> Obtain the given answer <i>OR3:</i> Use a relevant scalar product to find the cosine of <i>AOD</i> or <i>ADO</i> Obtain the given answer <i>OR4:</i> Use cosine formula in triangle <i>ADD</i> to find cos <i>AOD</i> or cos <i>ADO</i> Obtain cos <i>AOD</i> = $\frac{4}{9}$ or cos <i>ADO</i> = $\frac{10}{6\sqrt{10}}$ , or equivalent Use trig to find the length of the perpendicular Obtain the given answer <i>OR4:</i> Use cosine formula in triangle <i>ADD</i> to find cos <i>AOD</i> or cos <i>ADO</i> Obtain the given answer (i) State or imply $V = \pi h^3$ State or imply $\frac{dV}{dt} = -k\sqrt{h}$ Use $\frac{dV}{dt} = \frac{dV}{dh}$ , $\frac{dV}{dt}$ , or equivalent Obtain the given equation [The M1 is only available if $\frac{dV}{dh}$ is in terms of <i>h</i> and has been obtained by correct method.] [Allow B1 for $\frac{dV}{dt} = k\sqrt{h}$ but withhold the final A1 until the polarity of the constar $\frac{k}{3\pi}$ has been justified.]

Page 9	)	Mark Scheme	Syllabus	Paper	
		GCE A LEVEL – October/November 2013	9709	32	
(ii)	Sepa	rate variables and integrate at least one side		M1	
	Obta	in terms $\frac{2}{5}h^{\frac{2}{2}}$ and $-At$ , or equivalent		A1	
	Use	$t = 0, h = H$ in a solution containing terms of the form $ah^{\frac{5}{2}}$	and $bt + c$	M1	
	Use a	$t = 60, h = 0$ in a solution containing terms of the form $ah^{\frac{3}{2}}$	and $bt + c$	M1	
	Obta	in a correct solution in any form, e.g. $\frac{2}{5}h^{\frac{5}{2}} = \frac{1}{150}H^{\frac{5}{2}}t + \frac{2}{5}H^{\frac{5}{2}}t$	$I^{\frac{5}{2}}$	A1	
(ii)	Obta	in final answer $t = 60 \left( 1 - \left( \frac{h}{H} \right)^{\frac{5}{2}} \right)$ , or equivalent		A1	[6]

(iii) Substitute 
$$h = \frac{1}{2}H$$
 and obtain answer  $t = 49.4$  B1 [1]