## MARK SCHEME for the June 2004 question papers

## 0580/0581 MATHEMATICS

0580/01, 0581/01
0580/02, 0581/02
0580/03, 0581/03
0580/04, 0581/04

Paper 1 (Core), maximum raw mark 56
Paper 2 (Extended), maximum raw mark 70
Paper 3 (Core), maximum raw mark 104
Paper 4 (Extended), maximum raw mark 130

These mark schemes are published as an aid to teachers and students, to indicate the requirements of the examination. They show the basis on which Examiners were initially instructed to award marks. They do not indicate the details of the discussions that took place at an Examiners' meeting before marking began. Any substantial changes to the mark scheme that arose from these discussions will be recorded in the published Report on the Examination.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes must be read in conjunction with the question papers and the Report on the Examination.

- CIE will not enter into discussion or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the June 2004 question papers for most IGCSE and GCE Advanced Level syllabuses.

Grade thresholds taken for Syllabus 0580/0581 (Mathematics) in the June 2004 examination.

|  | maximum | minimum mark required for grade: |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | mark <br> available | A | C | E | F |
| Component 1 | 56 | - | 41 | 28 | 23 |
| Component 2 | 70 | 58 | 38 | 26 | - |
| Component 3 | 104 | - | 77 | 50 | 39 |
| Component 4 | 130 | 93 | 57 | 37 | - |

The threshold (minimum mark) for B is set halfway between those for Grades A and C. The threshold (minimum mark) for D is set halfway between those for Grades C and E . The threshold (minimum mark) for G is set as many marks below the F threshold as the E threshold is above it.
Grade A* does not exist at the level of an individual component.

## TYPES OF MARK

Most of the marks (those without prefixes, and ' $B$ ' marks) are given for accurate results, drawings or statements.

- M marks are given for a correct method.
- B marks are given for a correct statement or step.
- A marks are given for an accurate answer following a correct method.


## ABBREVIATIONS

a.r.t. Anything rounding to
b.o.d. Benefit of the doubt has been given to the candidate
c.a.o. Correct answer only (i.e. no 'follow through')
e.e.o. Each error or omission
f.t. Follow through
o.e. Or equivalent

SC Special case
s.o.i. Seen or implied
ww Without working
www Without wrong working
Work followed through after an error: no further error made

- Work followed through and another error found
* Indicates that it is necessary to look in the working following a wrong answer


## June 2004

## INTERNATIONAL GCSE

| MARK SCHEME |
| :---: |
| MAXIMUM MARK: 56 |
| SYLLABUS/COMPONENT: 0580/01, 0581/01 |
| MATHEMATICS |
| Paper 1 (Core) |


| Page 1 | Mark Scheme | Syllabus | Paper |
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|  | MATHEMATICS - JUNE 2004 | $0580 / 0581$ | 1 |


| 1 |  | 39 | 1 |  |
| :---: | :---: | :---: | :---: | :---: |
| 2 |  | 842 | 1 | Ignore any or no units after answer. Allow 84200 cm . |
| 3 | (a) | $\frac{3}{4}$ final answer | 1 |  |
|  | (b) | $\frac{7}{100}$ final answer | 1 |  |
| 4 | (a) | 49 | 1 |  |
|  | (b) | 31 | 1 |  |
| 5 |  | 4.5(0) | 2 | M1 for $18 \times 25$ or 450 or 4 m 50 cm seen (18:450 and 18:4.5 also indicate M1) |
| 6 |  | $4 \frac{1}{2}$ or $\frac{9}{2}$ or $\frac{18}{4}$ or $4 \frac{2}{4}$ | 2 | M1 for $\frac{9}{4} \times \frac{2}{(1)}$ seen. <br> Allow SC1 for 4.5 or $4 \frac{1}{2}$ oe seen with incomplete or decimal working. ( $\frac{9}{4}$ or $\times \frac{2}{(1)}$ oe or $2.25 \div 0.5$ ) Answer only, no working, is 0 . |
| 7 |  | 141.5, 142.5 | 2 | 1 for each answer SC1 for both values correct but wrong way round. |
| 8 |  | $2 \mathrm{x}(2 \mathrm{y}-3 \mathrm{z})$ | 2 | M1 for 2( $2 x y-3 x z$ ) or $x(4 y-6 z)$ or $2 x$ (wrong expression) Allow omitted last bracket. |
| 9 |  | 190.48 or 190.47 or 190 | 2 | M1 for $200 \div 1.05$, implied by 190.(.....) <br> Not allow 190.5 or 190.4 or 190.00 for 2 marks |
| 10 | (a) | 0 | 1 | (a) and (b) reversed-no marks |
|  | (b) | 2 | 1 |  |


| 11 | (a) | $110^{\circ}$ | 2 | B1 for Q $=35^{\circ}$ s.o.i.(can be on diagram) <br> 70 seen implies B1. |
| :--- | :--- | :--- | :--- | :--- |
| 12 | (a) | 3 | 1 |  |
|  | (b) | 0 | 1 |  |
| 13 | (a)(i) | $200 \quad 40$ | 1 | 1 |
|  | (a)(ii) | 5 f.t. | Only f.t. for simple mental calculation. E.g. $220 \div 40=5.5$ <br> or $200 \div 30=6$ or 7 or $6 \frac{2}{3}$ or 6.6 or 6.66 etc |  |
| 14 | (b) | 5.6 | B or $2^{\text {nd }}-$ dependent on M1, <br> M1 | 3 |
| 15 |  | 2.65 or <br> $2.649(\ldots)$. | M1 for a correct method for 1 bottle, implied by figs 615 or <br> 652 seen or figs 1625 or $153 \ldots .$. seen. <br> M1 (dep) for a complete correct method with consistent units. <br> (Implied by a correct pair of values seen. <br> Alt. Method completely correct is M2 |  |


| Page 2 | Mark Scheme | Syllabus | Paper |
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|  | MATHEMATICS - JUNE 2004 | $0580 / 0581$ | 1 |


| 16 | (a) | 13 | 2 | M1 for $-3+16$ seen |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | $\begin{aligned} & \frac{y-a}{b} \text { or } \frac{y-a}{b} \frac{a}{b} \text { oe } \\ & \text { Allow } \frac{a-y}{-b} \end{aligned}$ | 2 | M1 for a correct step, for clearly dividing by b or y - a seen. |
| 17 |  | Bar Chart | 4 | S1 correct scale and equal width bars. (Lost for vertical lines drawn) <br> B2 all bars correct height or B1 for any 2 bars correct height. Dots or line graph is B 0 . <br> L1 correct labels. |
| 18 | (a) | \$4.5(0) | 2 | M1 for $50 \mathrm{x}(0.25$ or 25 ) or $\$ 12.5(0)$ or 1250 seen, or $0.25-8 \div 50=(0.09)$ <br> or $25-800 \div 50=(9)$ |
|  | (b) * | 56.25 or 56 or 56.3 or 56.2 | 2f.t. | M1 for their (a)/8× 100 or their profit for 1 orange $\times 100$ their cost for 1 orange |
| 19 | (a) | $\begin{aligned} & 2826 \text { to } 2828 \text { or } \\ & 2830 \end{aligned}$ | 2 | M1 for $\pi \times 30^{2}$ or $\pi \times 0.3^{2}$ and method not spoilt. |
|  | (b) * | $\begin{aligned} & \text { 226.(080) to } \\ & 226 .(240) \text { or } 226 .(4 \ldots) \end{aligned}$ | 2f.t. | M1 for his (a) $\times 80$ s.o.i. or correct f.t. answer seen in cubic centimetres. |

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| 20 | (a) | 9 | 2 | M1 for $31+5$ or $\frac{31-5}{4}$ or $x-1.25=7.75$ |
| :--- | :--- | :--- | :--- | :--- |
| (b) | 14 | 2 | M1 for $4 y-20=36$ or $y-5=9$ or better. |  |
| 21 | (a) | 0015 or 1215 am <br> Ignore am added to <br> 0015 | 1 | Allow a clear time in words. E.g. 15 minutes after midnight. <br> Not 1215 or 2415 |
|  | (b)(i) * (bi) * | 749 min <br> Allow $7 \frac{1}{2}$ or 7.5 hours | 1f.t. | f.t. their (a) |

## June 2004

## INTERNATIONAL GCSE

| MARK SCHEME |
| :---: |
| MAXIMUM MARK: 70 |
| SYLLABUS/COMPONENT: 0580/02, 0581/02 |
| MATHEMATICS |
| Paper 2 (Extended) |


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|  | MATHEMATICS - JUNE 2004 | $0580 / 0581$ | 2 |


| Question Number | Mark Scheme |  | Notes |
| :---: | :---: | :---: | :---: |
| 1 | 3h 20 m | 1 |  |
| 2 | 10.9 | 1 |  |
| 3 | $0.5^{3}<0.5^{2}<\sqrt{ } 0.5$ | 2* | M1 for $0.25,0.7 \ldots$. and 0.125 seen matched |
| 4 | $\frac{1}{2} p^{20}$ | 2 | B1 $\frac{1}{2}$ or $p^{20}$ |
| 5 | 24 | 2* | M1 $x / 4=6$ or $x-32=-8$ seen |
| 6 | 63756385 | 1,1 | B1 correct but reversed |
| 7 | 7 | 2* | $\begin{aligned} & \text { B1 for one of }-7 / 8,-1 / 8,-14 / 16,-2 / 16,-0.875 \text {, } \\ & -0.125 \end{aligned}$ |
| 8 (a) <br> (b) | $\begin{aligned} & 4 \\ & 4 \end{aligned}$ | $1$ | Not 90 or $\frac{1}{4}$ turn |
| 9 | 450 | 2* | M1 for $3000 \times 7.5 \times 2 / 100$ |
| $10 \begin{aligned} & \text { (a) } \\ & \text { (b) } \end{aligned}$ | $\begin{aligned} & 80000 \\ & 8 \times 10^{4} \end{aligned}$ | $\begin{gathered} 1 \\ 1 \sqrt{ } \\ \hline \end{gathered}$ | $8 \times 10^{4}$ |
| 11 | $x=8 \quad y=1$ | 3* | M1 double and add/subtract consistently A1 A1 or M1 rearrange and substitute correctly |
| 12 | 50, 5, 3 | 1, 1, 1 |  |
| 13 | $\sqrt{ }\left(\frac{c-e}{k}\right)$ | 3* | R1, R1 for any 2 correct steps moving $e, k$ or $\sqrt{ }$ Allow $d^{2}=(c-e) / k$ to score $\mathbf{R 2}$ as a single step |
| 14 (a) <br> (b) |  | $1$ $2^{*}$ | Arc must not continue outside rectangle. Radius of arc $4 \mathrm{~cm} \pm 1 \mathrm{~mm}$. Ignore shading M1 for $\frac{1}{4} \times \pi \times 4^{2}$ |
| 15 | 4 | 3* | M1 Area factor or ratio 9 M1 LSF 3 |
| 16 (a) <br> (b) <br> (c) | $\begin{aligned} & a+c \\ & a-c \text { or }-c+a \\ & -\frac{1}{2} a-\frac{1}{2} c \text { or }-\frac{1}{2}(a+c) \end{aligned}$ | $\begin{gathered} 1 \\ 1 \\ 2^{*} \end{gathered}$ | M1 A0 for answers simplifying to these seen |
| 17 |  | $\begin{gathered} 2^{*} \\ 2^{*} \\ 1 \end{gathered}$ | M1 2 arcs centre $B$ and $D$, line drawn A1 M1 construction arcs on $A D$ and CD and centre these for the bisector, line drawn A1 Dependent on at least $1+1$ in part (a) SC1, SC1 If accurate and no construction arcs |
| $\begin{array}{ll} 18 & \text { (a) } \\ & \text { (b) } \end{array}$ | $\begin{aligned} & 114 \\ & \text { (0) } 47 \text { cao } \end{aligned}$ | $\begin{aligned} & 2^{*} \\ & 3^{*} \end{aligned}$ | M1 $78^{2}+83^{2}$ <br> M1 for finding one angle by trigonometry correctly <br> M1 for clearly identifying bearing angle Scale drawing and answers with no working score zero |
| 19 (a) <br> (b) <br> (c) | $\begin{aligned} & 11 \\ & x+2 \end{aligned}$ <br> 3 | $\begin{gathered} 1 \\ 2^{*} \\ 2^{*} \end{gathered}$ | M1 $\frac{2(x+1)}{2}+1$ <br> M1 for explicit $g(1)$ or $g^{-1}(x)=\frac{x-1}{2}$ |
| 20 (a) | $3(2 x-y)(2 x+y)$ | 2 | B1 $(6 x-3 y)(2 x+y)$ o.e. |
| (b) | (i) $x^{2}-6 x+9$ <br> (ii) $p=3 \quad q=1$ | $\begin{aligned} & 2^{*} \\ & 2 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { M1 correct method } \\ & \text { B1, B1 } \end{aligned}$ |


| Page 2 | Mark Scheme | Syllabus | Paper |
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| 21 (a) <br> (b) <br> (c) | $\begin{aligned} & 1.8 \\ & 450 \\ & 13 \end{aligned}$ | 2 $2^{*}$ $3^{*}$ | M1 convincing gradient calculation or use of $a=(v-u) / t$ <br> M1 for $20 \times 18+\frac{1}{2} \times 10 \times 18$ <br> M1 for finding total area under graph <br> ((b) +135 ) dep M1 for $\div 45$ $\square$ <br> If the vertical scale is consistently misread then M4 A0 is available |
| :---: | :---: | :---: | :---: |
| 22 (a) <br> (b) <br> (c) | $\begin{aligned} & \text { BA or (iii) } \\ & \left(\begin{array}{cc} 38 & 0 \\ 0 & 38 \end{array}\right) \\ & \frac{1}{38}\left(\begin{array}{cc} 4 & 6 \\ 5 & -2 \end{array}\right) \text { or }\left(\begin{array}{cc} 4 / 38 & 6 / 38 \\ 5 / 38 & -2 / 38 \end{array}\right) \end{aligned}$ | 2* | M1 checking order of all 4 matrices correctly M1 either column or row correct $\left(\begin{array}{cc} 2 / 19 & 3 / 19 \\ 5 / 38 & -1 / 19 \end{array}\right) \text { or }\left(\begin{array}{cc} 0.105 & 0.158 \\ 0.132 & -0.0526 \end{array}\right)$ |
|  | TOTAL | 70 |  |

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| MARK SCHEME |
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| MAXIMUM MARK: 103 |
| SYLLABUS/COMPONENT: 0580/03, 0581/03 |
| MATHEMATICS |
| Paper 3 (Core) |


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FINAL MARK SCHEME
0580/3
June 2004

| Question Number | Answer | Marks | Comments | Total |
| :---: | :---: | :---: | :---: | :---: |
| 1 a i | 51 | 1 |  |  |
| ii | 49 | 2 | M1 for clear evidence of ranking |  |
| iii | 46 | 2 | M1 for total/10, allowing errors in addition |  |
| b i | 20601608040 (360) | 2 | M1 for evidence of $\times 4$ oe seen or SC1 for 3 or 4 correct |  |
| ii | correct pie chart ( $\pm 2^{\circ}$ ) correct labels | $\begin{aligned} & 2 \\ & \text { L1 } \end{aligned}$ | 5 sectors only. Any order. Or SC1 for 3 or 4 correct or ft correct 4 or 5 correct or ft correct |  |
| iii a | 4/9 oe | 1 | allow (0).44..., 44 ....\%, but not 0.4 |  |
| iii b | 1/3 oe | 2 | M1 for their ( $(\mathrm{D}+\mathrm{E}) / \mathrm{T})$ from their table. Can be implied. For both parts -1 once for incorrect notation eg 4 out of $9,1: 3,4$ in 9 etc <br> 0.3 ww is zero |  |
|  |  |  |  | $\begin{array}{\|r\|} \hline 13 \\ \hline \end{array}$ |
| 2 a | 9 | 1 |  |  |
| b i | 6 | 1 |  |  |
| ii | 18 | 1 V | ft for $3 \times$ their bi (not strict ft ) |  |
| c i | (0). 6 | 2 | M1 for $3 \times 0.2$ |  |
| ii | 30 | $2 \sqrt{ }$ | M1 for their bii/ci (not strict ft) or $2 \times 3 / 0.2$ |  |
| d | (0). 02 | 2 | M1 for $2 \times 0.1 \times 0.1$ oe SC1 for fig 2 |  |
| e | $\begin{aligned} & \hline 4.8(0) 9(.00) \quad 14.4(0) \\ & 2.1(0) \\ & 30.3(0) \end{aligned}$ | $\begin{aligned} & 4 \\ & 1 \sqrt{ } \end{aligned}$ | B1 for each <br> ft from 4 total costs |  |
|  |  |  |  | $\begin{array}{\|r\|} \hline 14 \\ \hline 14 \end{array}$ |
| 3 a | $784-1$ | 3 | B2 for 3 correct or B1 for 2 correct |  |


| Page 2 | Mark Scheme | Syllabus | Paper |
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|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| b | 13 correct or ft correct points ( $\pm 1 / 2$ a square) <br> Correct curve cao | $\begin{array}{\|l} \hline \mathrm{P} 3 \mathrm{~V} \\ \mathrm{C} 1 \end{array}$ | $\mathrm{P} 2 \sqrt{ }$ for 11 or 12 correct or P1 $\sqrt{ }$ for 7 to 10 correct <br> reasonable parabola shape, no straight line segments, pointed maximum etc |  |
| c | $\begin{array}{\|l\|} \hline-2.7 \text { to }-2.9 \\ 2.7 \text { to } 2.9 \end{array}$ | $\begin{array}{\|l\|} \hline 1 \\ 1 \end{array}$ |  |  |
| d | $\begin{array}{\|r\|} \hline-1 \\ 5 \end{array}$ | $\begin{array}{\|l\|} \hline 1 \\ 1 \end{array}$ |  |  |
| e | correct line drawn $-3 \leq x \leq 3$ | 2 | M1 for incomplete line or freehand line or both their (in)correct points correctly plotted |  |
| f | 2 | 2 | M1 for attempt at $\Delta y / \Delta x$ from their straight line graph |  |
| g | $\begin{array}{\|l} \hline-3 \\ \hline \end{array}$ | $\begin{array}{\|l\|} \hline 1 \\ 1 \\ \hline \end{array}$ | -1 if $y$ values given as well |  |
|  |  |  |  | $\begin{array}{\|c\|} \hline 17 \\ \hline 17 \\ \hline \end{array}$ |
| 4 a | 120 | 1 |  |  |
| b | 70 | 2 | M1 for $t+2 t+75+75=360$ oe $3 t$ and 210 implies M1 |  |
| c i | 130 oe (eg 180-50) | 2 | M1 for angle sum of triangle(=180) used |  |
| ii | $\begin{aligned} & 100 \text { oe (eg } \\ & 360-100-160) \end{aligned}$ | 2 | M1 for angle sum of quadrilateral(=360) used |  |
| iii | $x=70$ and $y=30$ | 3 | $\sqrt{ }$ M1 for attempted elimination of one variable (be generous) A1 for each answer. no ft. correct answers reversed implies M1A1 |  |
|  |  |  |  | $\begin{array}{\|c\|} \hline 10 \\ \mathbf{1 0} \end{array}$ |
| 5 a | (0). 2 | 1 |  |  |
| b i | Tangent and radius mentioned | 1 | or described. |  |


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| ii | 8 cao | 1 |  |  |
| :---: | :---: | :---: | :---: | :---: |
| iii | art 1.78 | 3 | M1 for (their) $8^{2}-7.8^{2}$ oe M1 (indep) for square root indicated or used 1.77 ww implies M2. 1.8 ww is zero |  |
| iv | 6.9 (2 sig figs only) | $3 \sqrt{ }$ | ft for answer correct to 2 sig figs (not strict ft) (3.9×theirbiii) or M1 for $0.5 \times 7.8 \times$ their biii + A1 for answer to more than 2 sig figs |  |
|  |  |  |  | 9 |
| 6 ai | translation cao <br> 10 $-2$ | $\begin{aligned} & \hline \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \end{aligned}$ | or translated <br> -1 for incorrect notation or a description <br> SC1 for both answers correct but inverted |  |
| ii | rotation or turn centre the origin oe <br> (+) 90 (anticlockwise) | M1 <br> A1 <br> A1 | allow quarter turn for M1A1 |  |
| b i | correct reflection drawn | 2 | SC1 for reflection in $x$-axis |  |
| ii | correct enlargement drawn | 2 | SC1 for scale factor 2, wrong centre |  |
|  |  |  |  | $\begin{aligned} & \hline 10 \\ & 19 \\ & \hline \end{aligned}$ |
| 7 ai | pentagon | 1 |  |  |
| ii | 540 | 2 | M1 for $3 \times 180$, or $5 \times 180-360$ or $(180-360 / 5) \times 5$ or $6 \times 90$ |  |
| iii | 108 cao | 1 |  |  |
| b i | $110 \text { or } x=70 \text { or } y=20$ completion | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | may be on diagram Beware of circular arguments |  |
| ii | art 50.2 | 2 | M1 for $\tan \left({ }^{-1}\right)$ and 120/100 |  |
| iii | 120(.2) | $1 \sqrt{ }$ | ft for 70+their bii |  |


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|  | MATHEMATICS - JUNE 2004 | $0580 / 0581$ | 3 |


| iv | 300 | 1 V | ft for 180+their biii -1 for answers reversed |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\begin{array}{r} 10 \\ \hline 10 \\ \hline \end{array}$ |
| 8 ai | 6 ( $\pm 0.1$ ) | 1 |  |  |
| ii | 10 | $2 \sqrt{ }$ | $\sqrt{ } \mathrm{SC} 1$ for $10^{n}$ where $n$ is an integer. (ft 60/their ai) |  |
| iii | 73 to 76 | 1 |  |  |
| b | both lines drawn ( $\pm 0.1$ cm) | 2 | B1 for each line. Ignore any curves at ends, lines must be at least 5 cm long. Allow dotted etc |  |
| c | mediator drawn ( $\pm 0.1 \mathrm{~cm}$ and $1^{\circ}$ ) with two pairs of arcs | 2 | B1 for correct line with no arcs or correct arcs with no line |  |
| d | complete circle, radius $4( \pm 0.1) \mathrm{cm}$ drawn, centre C | 2 | SC1 for incomplete circle |  |
| e | L marked correctly | 1 | be convinced |  |
|  |  |  |  | 11 |
| 9 a i | 12 | 1 |  |  |
| ii | 20 | 1 |  |  |
| iii | $2 n+2$ oe | 2 | M1 for $2 n+k$ where $k$ is an integer |  |
| b i a | 20 | 1 |  |  |
| b i b | 25 | 1 |  |  |
| ii | 48 | 2 | M1 for 12 seen (as diagram no.) |  |
| iii | 100 | 2 | M1 for 10 seen |  |
|  |  |  |  | $\begin{array}{r} 10 \\ 21 \\ \hline \end{array}$ |

June 2004

## INTERNATIONAL GCSE

| MARK SCHEME |
| :---: |
| MAXIMUM MARK: 130 |
| SYLLABUS/COMPONENT: 0580/04, 0581/04 |
| MATHEMATICS |
| Paper 4 (Extended) |


| Page 1 | Mark Scheme | Syllabus | Paper |
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| Page 2 | Mark Scheme | Syllabus | Paper |
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|  | MATHEMATICS - JUNE 2004 | $0580 / 0581$ | 4 |


| Q4(a) | $\left(\mathrm{AC}^{2}=\right) 9.5^{2}+11.1^{2}-2 \times 9.5 \times 11.1 \cos 70$ | M2 | Allow M1 for $\frac{9.5^{2}+11.1^{2}-\mathrm{AC}^{2}}{2 \times 9.5 \times 11.1}=\cos 70$ |
| :---: | :---: | :---: | :---: |
|  | square root of correct combination (141.3279...) or 11.888... | M1 | Dep. on previous M2. Must be convinced that errors are due to slips not incorrect combination. |
|  | 11.9 (cm) | A1 | www4 Scale drawing gets M0A0. |
| (b) | (Opp. angles of) cyclic quadrilateral (add to 180) | B1 | Condone 180-70=110 o.e. (not spoilt) |
| (c) | 70-37 attempted s.o.i. | M1 | e.g. 32 or 34 or 43 , but be convinced. |
|  | $\frac{\mathrm{AD}}{\sin 33}=\frac{\text { their }(\mathrm{a})}{\sin 110} \quad \text { o.e. }$ | M1 | Dep. on first M1 |
|  | $(\mathrm{AD}=)$ their (a) $\mathrm{x} \sin 33$ | M1 |  |
|  | $\text { art } 6.89 \text { or } 6.90(\mathrm{~cm})$ | A1 | Would imply M3 if nothing incorrect seen earlier. Condone 6.9 www4 Scale drawing gets M0A0 |
| (d)(i) | 70 | B1 | If not 70, ft for method in (ii), but not from 90 or60 |
| (ii) | $(\mathrm{h}=) \frac{\text { their }(\mathrm{a}) \mathrm{x} \tan 55 \text { or }}{2} \frac{\operatorname{their}(\mathrm{a})}{2 \mathrm{xtan} 35}$ | M1 | $(\mathrm{EC} \text { or } \mathrm{EA}=) \frac{\text { their(a) }}{2 \sin 35} \text { or } \frac{\text { their(a) }}{2 \cos 55} \quad(10.37 \ldots)$ |
|  | $(\operatorname{area}=) 0.5 \times$ their(a) $x$ their(h) o.e. | M1 | Dep. on first M1 <br> (area $=$ ) $0.5 \times$ EC x EA x $\sin 70$ or Hero's Method |
|  | 50.4 to $50.8\left(\mathrm{~cm}^{2}\right)$ | A1 | www3 13 |
| Q5(a) | $10 / x$ or $10 \div x$ o.e. | B1 | Ignore all units in answers to Question 5. <br> Not $x=10 / x$ |
| (b) | $\frac{10}{x}-\frac{10}{x+1}=\frac{1}{2} \quad \text { o.e. }$ | M2 | Condone 30 for $1 / 2$ <br> If M0 give $\mathbf{S c} 1$ for $\frac{10}{x+1}$ s.o.i. |
|  | $20(x+1)-20 x=x(x+1) \quad$ o.e. | MA1 | Dep on M2. No longer condoning 30 o.e. <br> Sc1 for $20 x-20(x+1)=x(x+1)$ o.e. after B1Sc1 |
|  | $x^{2}+x-20=0$ | E1 | No error of any kind at any stage and sufficient working to convince you (at least 1 extra step) |
| (c) | $(x+5)(x-4) \quad(=0)$ | M1 | $\frac{-1 \pm \sqrt{ }\left[1^{2}-4.1 .(-20)\right]}{2}$ No errors or ambiguities |
|  | -5 and 4 c.a.o. | A1 | www2 |
| (d) | Rejects negative solution <br> 2.5 (hours) <br> c.a.o. | $\begin{aligned} & \text { R1 } \\ & \text { B1 } \end{aligned}$ | May be explicit or implicit and could be in (c) Condone 2 hrs 30 (mins) or 150 mins |


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| Q6(a)(i) <br> (ii) <br> (b) <br> (c) | $\begin{aligned} & \frac{2 \times \pi \times 7^{3}}{3}+\frac{\pi \times 7^{2} \times 13}{3} \\ & \mathbf{1 3 8 4 . 7} \text { to } \mathbf{1 3 8 6} \text { or } \mathbf{1 3 8 0} \text { or } \mathbf{1 3 9 0}\left(\mathbf{c m}^{3}\right) \\ & \text { their(a)(i) } \times 0.94 \\ & \mathbf{1 . 3 ~ ( \mathbf { k g } )} \\ & \\ & (\mathrm{~L}=) \sqrt{ }\left(13^{2}+7^{2}\right) \\ & \pi \times 7 \times \text { theirL } \\ & \mathbf{3 2 4} \text { to } \mathbf{3 2 6}\left(\mathrm{cm}^{2}\right) \\ & \\ & \text { CSA of hemisphere }=2 \times \pi \times 7^{2} \quad \text { s.o.i. } \\ & \text { their(b) + their CSA } \\ & \mathbf{6 3 1 . 7} \text { to } \mathbf{6 3 4} \\ & \underline{411.58} \\ & \text { their total } \\ & \mathbf{( \$ ) 0 . 6 4 9} \text { to } \mathbf{0 . 6 5 2} \underline{\text { or } \mathbf{6 4 . 9} \text { to } \mathbf{6 5 . 2} \underline{\text { cents }}} \end{aligned}$ | M1 <br> A1 <br> M1 <br> A2 $\sqrt{ }$ <br> M1 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 <br> M1 <br> A1 | www2 $\sqrt{ } \text { ft } \frac{\text { their(a)(i) }}{1000} \times 0.94$ <br> www3 If A2 not scored, allow A1 $\sqrt{ }$ for $1.30 \ldots$ <br> Implied by $\sqrt{ } 218$ or $14.7 \ldots$. or 14.8 Dep. on first M1. <br> www3 <br> 307.7 to 308 if no working <br> Dep. on first M1 <br> Seen or implied by subsequent working. <br> Dep. on a total <br> www5 |
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| Q7(a)(i) <br> (ii) <br> (iii) <br> (iv) | ```Venn Diagram with 12, 8, 7, 3 or with \(20-x, x, 15-x, 3\) 8 \(\begin{array}{ll}\frac{\mathbf{1 2}}{\mathbf{3 0}} & \text { o.e } \\ \frac{\mathbf{1 2}}{\mathbf{2 0}} & \text { o.e. }\end{array}\)``` | $\begin{aligned} & \mathbf{B 2} 2 \\ & \\ & \text { B1 } \sqrt{ } \\ & \text { B2 } \sqrt{ } \\ & \text { B2 } \sqrt{ } \end{aligned}$ | -1 each error/omission. Condone lack of labels. <br> $\sqrt{ }$ ft their 8 on diagram, but not $x$ <br> $\sqrt{ } \quad \mathbf{f t}$ (their 12)/30 from (i) or (ii) <br> Sc1 for $k / 30$ where $k<30$ <br> $\sqrt{ } \mathbf{f t}$ (their 12)/20 from (i) or (ii) if their $12<20$ <br> Sc1 for $m / 20$ where $m<20$ |
| (b)(i) | $3 / 9$ x $4 / 10$ <br> $\mathbf{1 2}$  <br> $\mathbf{9 0}$  <br> o.e.  <br> $1-$ their(b)(i)  <br> $\mathbf{7 8}$ o.e. c.a.o. | M1 <br> A1 <br> M1 <br> A1 $\sqrt{ }$ | In all of Q7, accept fractions, decimals or \%. Mark as ISW for wrong cancelling. Dec. or \% need to be exact or accurate to 3 sf. No ratios. Other inappropriate notation is -1 once. $\begin{aligned} & \text { or } 6 / 9 \times 6 / 10+6 / 9 \times 4 / 10+3 / 9 \times 6 / 10 \\ & \sqrt{ } \text { ft } 1-\text { their }(\mathrm{b})(\mathrm{i}) \end{aligned}$ |
| (iii) (iv) |  | M1 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 | Allow a slip in 1 digit, but must use 4 fractions multiplied. <br> Simplest 5/36 <br> Alt. method. Must see all 14 combinations. Dep. on first M1. Must add them <br> Simplest 17/20 |


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| Q8(a)(i) | Rotation (only) <br> 90 (anticlockwise)(about O) or $1 / 4$ turn | $\begin{array}{\|l\|} \hline \text { B1 } \\ \hline \text { B1 } \end{array}$ | "only" --- no other transformation mentioned. <br> Ignore all matrices, except in (v). <br> Do not allow "turn" for rotation <br> Accept 270 clockwise or -270 |
| :---: | :---: | :---: | :---: |
| (ii) | $\begin{aligned} & \text { Translation (only) } \\ & (-2) \\ & (-5) \end{aligned}$ | B1 | Not translocation, transformation, transportation. eg 2 to left and 5 down. Condone ( $-2-5$ ) and lack of brackets. |
| (iii) | Reflection (only) $y=-x$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ |  |
| (iv) | 180 (or $1 / 2$ turn) Rotation (only) Centre (1, $\mathbf{- 1 )}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | Enlargement sf=-1 earns B2 Sc1 for "Point Symmetry" |
| (v) | Enlargement (only) <br> Scale Factor 2 (centre O) | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | Accept 20 for scale factor 2 02 |
| (vi) | Shear (only) $y$ axis invariant or parallel to $y$ axis | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | Ignore any mention of scale factor. |
| (b) | B | B2 |  |
| (c)(i) | $\left(\begin{array}{rr} 1 & 0 \\ 0 & -1 \end{array}\right)$ | B2 | Sc1 for a correct column |
| (ii) | $\left(\begin{array}{ll} 1 & 0 \\ 1 & 1 \end{array}\right)$ | B2 | Sc1 for a correct column $\mathbf{1 8}$ |
| $\begin{array}{r} \text { Q9 (a) } \\ \text { (b) } \\ \text { (c) } \end{array}$ | $\begin{array}{llll} 15 x+25 y \leq 2000 & \text { seen } & \\ y \leq x & \text { o.e. } & \text { c.a.o. } \\ y \geq 35 & \text { o.e. } & \text { c.a.o. } \end{array}$ | $\begin{array}{\|l\|} \hline \text { B1 } \\ \text { B2 } \\ \text { B1 } \end{array}$ | Allow $0.15 x+0.25 y \leq 20$ but no others. Sc1 for any other sign between $x$ and $y$ |
| $\begin{gathered} \text { (d)(i) } \\ \text { (ii) } \end{gathered}$ | Scales correct and full length. <br> $\mathbf{3} \boldsymbol{x}+\mathbf{5} \boldsymbol{y}=\mathbf{4 0 0}$ correct $(1 \mathrm{~mm})$ at $(0,80)$ and $(100,20)$ and long enough. $\begin{aligned} & y=x \text { correct } \\ & y=\mathbf{3 5} \text { correct } \end{aligned}$ | $\begin{aligned} & \text { S1 } \\ & \text { B2 } \\ & \text { L1 } \\ & \text { L1 } \end{aligned}$ | Reversed scales S0 <br> Sc1 for either point correct. |
|  | Shading correct (in or out) | B1 V | $\sqrt{ } \mathbf{f t}$ from slips in lines that do not compromise the idea of the triangle. |
| (e) | 38 c.a.o. | B1 |  |
| (f) | Identifying any point(s) in their area (enclosed by 3 lines or 3 lines and 1 axis). <br> $(75,35)$ s.o.i. <br> c.a.o. <br> (\$) 6.2(0) or 620 (cents) | M1 <br> A1 <br> B1 $\sqrt{ }$ | Implies M1 <br> $\sqrt{ } \mathbf{f t}$ their $(75,35)$ evaluated for whole numbers only. <br> Condone lack of units but not wrong units. www3 |

