## MATHEMATICS

Paper 3 (Core)


Candidates answer on the Question Paper.
Additional Materials: Electronic calculator Geometrical instruments

October/November 2004 Mathematical tables (optional) Tracing paper (optional) 2 hours

Candidate Name

Centre Number


Candidate Number


## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen in the spaces provided on the Question Paper.
You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
DO NOT WRITE IN THE BARCODE.
DO NOT WRITE IN THE GREY AREAS BETWEEN THE PAGES.

Answer all questions.
If working is needed for any question it must be shown below that question.
The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 104.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Given answers in degrees to one decimal place.

For $\pi$, use either your calculator value or 3.142.

| For Examiner's Use |
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This document consists of 15 printed pages and 1 blank page.
UNIVERSITY of CAMBRIDGE
International Examinations

1 (a) Two friends, Hatab and Yasin, went on a cycle ride.
Part of the distance-time graph for their journey is shown below.


For the first part of the journey they cycled at the same speed.
(i) Find their speed for the first part of the journey.

> Answer(a)(i)
$\qquad$ $\mathrm{km} / \mathrm{h}$ [1]
(ii) At 1100 they stopped for half an hour. Show this on the graph.
(iii) They continued on their ride and at 1245 they were 16 kilometres from home. Show this part of the journey on the graph.
(iv) They stopped again and then had a race going home.
(a) For how long did they stop?

Answer(a)(iv)(a) $\qquad$ $\min [1]$
(b) Who won the race?
Answer(a)(iv)(b)
(v) What was the total length of their journey?
$\qquad$ km [1]
(b) On a certain day the conversion rate between dollars (\$) and Indian rupees was

$$
\$ 1=45 \text { rupees. }
$$

(i) How many rupees were equivalent to $\$ 10$ ?

> Answer(b)(i)
$\qquad$ rupees [1]
(ii) Use this information to draw a conversion graph on the axes below.

(iii) Use your graph to find
(a) how many rupees were equivalent to $\$ 6.80$,
Answer(b)(iii)(a)
$\qquad$ rupees [1]
(b) how many dollars were equivalent to 480 rupees.

(a) Describe fully the single transformation that maps triangle $A$ onto triangle $B$.

Answer(a) $\qquad$
$\qquad$
(b) Describe fully the single transformation that maps triangle $A$ onto triangle $C$.

Answer(b) $\qquad$
(c) Find the centre and the scale factor of the enlargement that maps triangle $A$ onto triangle $D$.

Answer(c) centre $\qquad$ ,......... ) scale factor
(d) On the grid
(i) draw the image of triangle $A$ under a reflection in the line $x=-1$,
(ii) draw the image of triangle $B$ under a rotation of $180^{\circ}$ about ( $-4,-3$ ).


On the above diagram, $A B=2 \mathrm{~cm}, B D=6 \mathrm{~cm}, A E=10 \mathrm{~cm}$, angle $B C D=40^{\circ}$ and angle $B D E=90^{\circ}$.
(a) Write down the length of $A D$.

$$
\text { Answer(a) } A D=
$$

$\qquad$
(b) Calculate the length of $D E$.
(c) Calculate the size of angle $A E D$.

Answer (c) angle $A E D=$
(d) Calculate the length of $C D$.

Answer (d) $C D=$
cm [3]
(e) Find the length of $C E$.

4 (a)

(i) In the space below, using a ruler and compasses only, construct the above triangle accurately.
(ii) Using the triangle you have drawn, measure and write down the size of angle $A C B$.

$$
\text { Answer(a)(ii) angle } A C B=
$$

(b) In the diagram below two points, $P$ and $Q$, are joined by a straight line.
(i) On the diagram draw the locus of all the points that are 4 centimetres from the line $P Q$. 3
(ii) On the same diagram, using a straight edge and compasses only, construct the locus of the points that are equidistant from $P$ and $Q$.

## Show all your construction lines.

(iii) Shade the region which contains the points that are closer to $P$ than to $Q$ and are less than 4 centimetres from the line $P Q$.

5 (a)


In the diagram above $A B=B C$ and $A D=D C$.
(i) What is the special name of the quadrilateral $A B C D$ ?
Answer(a)(i)
(ii) On the diagram draw the line of symmetry.
(iii) Calculate the value of $y$.

$$
\operatorname{Answer(a)(iii)~} y=
$$

(b)

NOT TO SCALE

In the diagram above, the points $K, L, M$ and $N$ lie on the circle centre $O$.
$K N$ is parallel to $L M$.
Find the values of $p, q$ and $r$.
$\qquad$ , $q=$ $\qquad$ $r=$ $\qquad$

## NOT TO SCALE



(b) $p=$ =
(c)


The diagram above shows a regular seven-sided polygon.
Each of the interior angles measures $x^{\circ}$.
One of the angles is marked in the diagram.
Calculate the value of $x$, giving your answer correct to 1 decimal place.
Show all your working.

6 (a) Complete the table below for $y=x^{2}-2 x$.

| $x$ | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 8 |  |  | -1 |  | 3 | 8 |

(b) On the grid below, draw the graph of $y=x^{2}-2 x$ for $-2 \leqslant x \leqslant 4$.

(c) The line $y=2$ is drawn on the diagram.

Use your graph to find the values of $x$ that solve the equation $x^{2}-2 x=2$.

$$
\begin{aligned}
& \text { Answer(c) } \quad x= \\
& \text { or } x=
\end{aligned}
$$

(d) Complete the table below for $y=4-x$.

| $x$ | -4 | 0 | 4 |
| :---: | :---: | :---: | :---: |
| $y$ | 8 |  |  |

(e) On the grid above, draw the line $y=4-x$ for $-4 \leqslant x \leqslant 4$.
(f) Write down the $x$ coordinates of the points of intersection of the graphs of $y=x^{2}-2 x$ and $y=4-x$.

$$
\begin{aligned}
& \text { Answer(f) } \quad x= \\
& \text { or } x=
\end{aligned}
$$

7 (a) Rajeesh thought of a number.
He multiplied this number by 2 .
He then added 10.

The answer was 42.
(i) What was the number Rajeesh first thought of?

## Answer(a)(i)

(ii) Simon thought of a number $x$.

He multiplied this number by 3 and then added 8 .
Write down an expression in $x$ for his answer.

## Answer(a)(ii),

(b) Simplify $-8 a+7 b-a-2 b$.
Answer(b)
(c) Factorise fully $6 a-9 a^{2}$.
Answer(c)
(d) Make $t$ the subject of the formula

$$
v=u+a t .
$$

$$
\operatorname{Answer}(d) t=
$$

(e) Solve the simultaneous equations

$$
\begin{gathered}
8 x+2 y=13, \\
3 x+y=4 .
\end{gathered}
$$

8 (a) The list shows the rainfall in millimetres in Prestbury for the 12 months of 2002.

| 61 | 146 | 22 | 54 | 67 | 94 | 141 | 22 | 37 | 167 | 87 | 170 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(i) Write down the mode.

> Answer(a)(i)
$\qquad$ mm [1]
(ii) Find the median.
Answer(a)(ii)
$\qquad$ mm [2]
(iii) Calculate the mean.

Answer(a)(iii) mm [2]
(b) During the years 1996-2000 the total rainfall in Prestbury was 5400 millimetres.

The pie chart shows how this was spread over the five years.

(i) Measure the angles of the sectors for 1998, 1999 and 2000. Write your answers in the table below.
(ii) Work out the annual rainfall, in millimetres, for each of the years 1998, 1999 and 2000. Write your answers in the table below.

Answers (b)(i) and (ii)

| Year | Angle (degrees) | Rainfall (mm) |
| :---: | :---: | :---: |
| 1996 | 54 | 810 |
| 1997 | 60 | 900 |
| 1998 |  |  |
| 1999 |  |  |
| 2000 | 360 | 5400 |
| Total |  |  |

(iii) What do you notice about the trend in the rainfall from 1996 to 2000?

Answer(b)(iii) $\qquad$

9 (a) A pattern of numbers is shown below.

(i) On the diagram complete row 6 .
(ii) The last numbers in each row form a sequence.

$$
1,4,9,16,25
$$

(a) What is the special name given to these numbers?
Answer(a)(ii)(a)
(b) Write down the last number in the 10th row.
Answer(a)(ii)(b)
(c) Write down an expression for the last number in the $n$th row.
Answer(a)(ii)(c)
(iii) The numbers in the middle column of the pattern form a sequence.

$$
1,3,7,13,21,31, \ldots \ldots \ldots \ldots \ldots
$$

(a) Write down the next number in this sequence.
Answer(a)(iii)(a)
(b) The expression for the $n$th number in this sequence is $n^{2}-n+1$. Work out the 30th number.
Answer(a)(iii)(b)
(b) Another pattern of numbers is shown below.

| row |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $-\ldots$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10

(i) What is the last number in the 10th row?
Answer(b)(i)
(ii) Find an expression for the last number in the $n$th row.
Answer(b)(ii)
(iii) What is the first number in the 10th row?
Answer(b)(iii)
(iv) Find an expression for the first number in the $n$th row.

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