MANN. FIRETREP ROCES, COM

## **UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS**

**International General Certificate of Secondary Education** 

## MARK SCHEME for the May/June 2010 question paper for the guidance of teachers

## 0580 MATHEMATICS

0580/41

Paper 41 (Extended), maximum raw mark 130

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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## **Abbreviations**

cao correct answer only cso correct solution only

dep dependent

ft follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

www without wrong working

Qu.	Answers	Mark	Part Marks
1 (a)	11:14	1	
(b)	50	2	<b>M1</b> for $(220 + 280) \div 10$ o.e.
(c)	12	2	<b>M1</b> for $21 \div (4+3) \times 4$ (or 3) o.e.
(d)	280	3	M1 for 0.35 × their 500 (175) M1 dependent × 1.60
(e)	240	2	M1 for dividing 264 by 1.1 oe
2 (a) (i)	4	1	
(ii)	5	1	
(iii)	4.75	3	M1 for $1 \times 2 + 1 \times 3 + 17 \times 4 + 12 \times 5 + 6 \times 6 + 3 \times 7$ condone one slip <b>then</b> M1 dependent result $(190) \div 40$
<b>(b)</b>	$\frac{190+3n}{40+n}$	2	SC1 for their $190 + 3n$
3 (a)	Triangle drawn with co-ords at (1, 4), (4, 2), (4, 4)	2	SC1 for 2 correct vertices or an enlargement of $\frac{1}{2}$ with wrong centre
(b) (i)	$\begin{pmatrix} -8 & -8 & -2 \\ 4 & 8 & 8 \end{pmatrix}$	2	B1 each row
(ii)	Triangle drawn at (-8, 4), (-8, 8), (-2, 8) ft (i)	2ft	SC1 for 2 correct ft vertices. Can also be correct regardless of (i)
(iii)	Reflection cao $y - axis \text{ or } x = 0$ cao	2	B1 Independent of (i) or (ii) Extra transformations lose all marks B1 Independent of (i) or (ii)
(c) (i)	Translation		<b>B1</b> Extra transformations lose all marks
	$\begin{pmatrix} -10 \\ -10 \end{pmatrix}$ o.e.	2	B1
(ii)	Rotation (0, 0) 90° clockwise oe	3	B1 Extra transformations lose all marks B1 Allow word origin for (0, 0) B1 Allow – 90° or 270° (anti-clockwise)
(d)	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	2	B1 each column

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4				In (b) and (c) isw any cancelling or changing to other forms, after correct answer seen. Penalty of – 1 for 2 sf decimals or percentages. Do not accept ratio or worded forms.
(a)	B and $\frac{2}{5}$ , $\frac{1}{4}$ oe		1	Allow any reasonable explanation, e.g. 2 out of 5 greater than 1 out of 4.
	$\frac{1}{3}, \frac{3}{4}, \frac{2}{5}, \frac{3}{5}$		4	B1 B1 B1 B1
(ii)	$\frac{6}{12}$ oe cao	www 2	2	$\frac{1}{2}$ , 0.5 etc M1 for $\frac{2}{3}$ ×their $\frac{3}{4}$ i.e. product of correct branches on their tree
(iii)	$\frac{42}{60}$ oe cao	www2	2	$\frac{7}{10}$ , 0.7 etc
(c)	$\frac{2}{60}$ oe cao	www2	2	M1 for their (ii) + their $\frac{1}{3}$ × their $\frac{3}{5}$ from their tree $\frac{1}{30}, 0.0333(3) \text{ etc}$ M1 for $\left(\frac{2}{3} \times \frac{1}{4} \times 0\right) + \frac{1}{3} \times \frac{2}{5} \times \frac{1}{4}$
5 (a)	200.5 to 201	www 2	2	<b>M1</b> for $0.5 \times 24 \times 26 \sin 40$ oe <b>A1</b>
(b)	17.2 (0)	www 4	4	M2 for $26^2 + 24^2 - 2 \times 26 \times 24 \cos 40$ or M1 for $\cos 40 = \frac{26^2 + 24^2 - BD^2}{2 \times 24 \times 26}$ A2 or A1 for 295.976
(c)	12.8 (12.77)	www 4	4	<b>B1</b> for Angle $C = 110$ soi accept on diagram <b>M2</b> for $(BC) = \frac{24 \sin 30}{\sin 110}$ oe <b>or M1</b> $\frac{\sin 110}{24} = \frac{\sin 30}{BC}$ oe i.e. a correct implicit statement soi <b>A1</b>
(d)	8.208 to 8.230	www 2	2	M1 for their (c) $\times$ sin40 oe

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6 (a)	32.5 cao www4	4	M1 for mid-values seen M1 for use of $\Sigma fx$ with x's anywhere in each interval $(10 \times 15 + 30 \times 30 + 20 \times 45)$
(b)	Histogram drawn	3	M1 ÷ 60 dependent on second M1  B1 Bars correct positions and widths – no gaps B2 Heights of bars 1, 1.5 and 2 (B1 for any two correct or for heights in the ratio 2:3:4)
7 (a)	4.53 or 4.526 – 4.530	3	SC2 for figs 453 or $4526 - 4530$ If SC0, M1 for $\pi \times (\text{figs } 31)^2 \times 15$
(b)	3.62 to 3.624 ft	2ft	M1 for their (a) $\times$ figs 8 oe
(c) (i)	$360 - 2 \times 90 - 60$ oe	2	E2 The 90's and the 60 must be clearly justified. Accept in diagram.  SC1 for 60 or two 90's soi in correct positions oe e.g 360 ÷ 3 scores 0
(ii)	0.649 (0.6492 to 0.6493)	2	<b>M1</b> for $\pi \times \text{figs } 62 \div 3$
(iii)	7.53 (7.527 or 7.528)	3	M1 for their (ii) × 3 M1 (indep) for 18 × figs 31 This M is spoiled by extra lengths.
(iv)	112.9 to 113 ft	1 <b>ft</b>	ft their (iii) × 15
8 (a)	0.25, 8, 16	3	B1 B1 B1
(b)	-5,4	2	B1 B1
(c) (i)	7 points plotted ft Curve through all 7 points exponential shape	P2ft C1ft	P1 for 5 or 6 points ft ft only if exponential shape
(ii)	6 points plotted ft Curve through all 6 points parabola shape	P2ft C1ft	P1 for 5 points ft ft only if parabola shape
(d) (i)	3.2 to 3.4	1	
(ii)	0.3 to 0.4 and 2	2	B1 B1
(iii)	3.1 to 3.4	1	
9 (a) (i)	-2.5 oe	2	<b>M1</b> for $5(w+1) = 3w$
(ii)	-3 or 1	2	<b>B1 B1</b> (If 0, <b>SC1</b> for $y + 1 = \pm 2$ )
(iii)	9.5 oe	В3	M2 for $5x + 5 - 3x + 6 = 2 \times 15$ Condone one slip (sign or numerical) on left hand side
			or M1 for $\frac{5(x+1)}{15} - \frac{3(x-2)}{15}$ or better, condoning one sign or numerical slip.

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(b) (i)	(u-10)(u+1)	2	SC1 for $(u+a)(u+b)$ where $ab = -10$ or $a+b=-9$
(ii)	-1, 10	1 <b>ft</b>	Only <b>ft B2</b> or <b>SC1</b> in <b>(i)</b> but can recover to correct answer only if new working or if <b>(i)</b> not attempted
(c) (i)	$\frac{(x+1)(x+2)}{2} = x^2 \qquad \text{oe}$	M1	
	$((x+1)(x+2) =)x^2 + x + 2x + 2$	B1	Allow $3x$ for $x + 2x$
	$x^2 + x + 2x + 2 = 2x^2$		
	$x^2 - 3x - 2 = 0$	E1	Established without any omissions or errors
(ii)	$\frac{-(-3) \pm \sqrt{(-3)^2 - 4(1)(-2)}}{2(1)}$	2	<b>B1</b> for $\sqrt{(-3)^2 - 4(1)(-2)}$ or better seen anywhere.
			If in form $\frac{p+\sqrt{q}}{r}$ or $\frac{p-\sqrt{q}}{r}$ then <b>B1</b> for
			-(-3) and $2(1)$ or better
			Brackets and full line may be implied later
	-0.56, 3.56	2	<b>B1 B1 SC1</b> for -0.6 or -0.562 to -0.561 <b>and</b> 3.6 or 3.561 to 3.562
(iii)	12.7 or 12.67 to 12.69 ft	1 <b>ft</b>	ft their positive x squared
(iii) 10 (a)	12.7 or 12.67 to 12.69 ft $20x + 100y \le 1200$	1 <b>ft</b>	<b>ft</b> their positive <i>x</i> squared
` ′			ft their positive x squared
10 (a)	$20x + 100y \le 1200$	1	ft their positive x squared
10 (a) (b)(i)	$20x + 100y \le 1200$ $x + y \ge 40$	1 1	Each line ruled and long enough to enclose
10 (a) (b)(i) (ii)	$20x + 100y \le 1200$ $x + y \ge 40$ $y \ge 2$	1 1 1	Each line ruled and long enough to enclose required region.  If <b>L0</b> , <b>SC1</b> if freehand but otherwise accurate
10 (a) (b)(i) (ii)	$20x + 100y \le 1200$ $x + y \ge 40$ $y \ge 2$ $x + y = 40 \text{ cao}$	1 1 1 L1	Each line ruled and long enough to enclose required region.
10 (a) (b)(i) (ii)	$20x + 100y \le 1200$ $x + y \ge 40$ $y \ge 2$ x + y = 40 cao y = 2 cao Required region only region left not shaded or otherwise clearly indicated	1 1 1 L1 L1	Each line ruled and long enough to enclose required region.  If <b>L0</b> , <b>SC1</b> if freehand but otherwise accurate and enclose region
10 (a) (b)(i) (ii) (c)	$20x + 100y \le 1200$ $x + y \ge 40$ $y \ge 2$ x + y = 40 cao y = 2 cao Required region only region left not shaded or otherwise clearly indicated cao	1 1 1 L1 L1 R2	Each line ruled and long enough to enclose required region.  If <b>L0</b> , <b>SC1</b> if freehand but otherwise accurate and enclose region
10 (a) (b)(i) (ii) (c)	$20x + 100y \le 1200$ $x + y \ge 40$ $y \ge 2$ x + y = 40 cao y = 2 cao Required region only region left not shaded or otherwise clearly indicated cao 5 cao 50 cao, 2 cao	1 1 1 L1 L1 R2	Each line ruled and long enough to enclose required region.  If <b>L0</b> , <b>SC1</b> if freehand but otherwise accurate and enclose region <b>SC1</b> if one boundary error – see diagrams
10 (a) (b)(i) (ii) (c) (d) (e)	$20x + 100y \le 1200$ $x + y \ge 40$ $y \ge 2$ x + y = 40 cao y = 2 cao Required region only region left not shaded or otherwise clearly indicated cao 5 cao 50 cao, 2 cao 270 ft	1 1 1 L1 L1 R2 1 2 1ft	Each line ruled and long enough to enclose required region.  If <b>L0</b> , <b>SC1</b> if freehand but otherwise accurate and enclose region <b>SC1</b> if one boundary error – see diagrams <b>B1 B1 ft</b> $5 \times \text{their } x + 10 \times \text{their } y$
10 (a) (b)(i) (ii) (c) (d) (e)  11 (a)	$20x + 100y \le 1200$ $x + y \ge 40$ $y \ge 2$ x + y = 40 cao y = 2 cao Required region only region left not shaded or otherwise clearly indicated cao 5 cao 50 cao, 2 cao 270 <b>ft</b> Reasonable diagram, 25, 13, 62 64, 19, 146 $n^2$ oe	1 1 1 L1 L1 R2 1 1 2 1ft 4 3	Each line ruled and long enough to enclose required region.  If <b>L0</b> , <b>SC1</b> if freehand but otherwise accurate and enclose region <b>SC1</b> if one boundary error – see diagrams  B1 B1  ft 5 × their x + 10 × their y  B1 B1 B1 B1 diagram may be freehand  B1 B1 B1  B1
10 (a) (b)(i) (ii) (c)  (d) (e)  11 (a) (b) (c)	$20x + 100y \le 1200$ $x + y \ge 40$ $y \ge 2$ x + y = 40 cao y = 2 cao Required region only region left not shaded or otherwise clearly indicated cao 5 cao 50 cao, 2 cao 270 ft Reasonable diagram, 25, 13, 62 64, 19, 146 $n^2$ oe 2n + 3 oe	1 1 1 L1 L1 R2 1 1 2 1ft 4 3	Each line ruled and long enough to enclose required region.  If <b>L0</b> , <b>SC1</b> if freehand but otherwise accurate and enclose region <b>SC1</b> if one boundary error – see diagrams  B1 B1  ft 5 × their x + 10 × their y  B1 B1 B1 B1 diagram may be freehand  B1 B1 B1
10 (a) (b)(i) (ii) (c) (d) (e)  11 (a) (b)	$20x + 100y \le 1200$ $x + y \ge 40$ $y \ge 2$ x + y = 40 cao y = 2 cao Required region only region left not shaded or otherwise clearly indicated cao 5 cao 50 cao, 2 cao 270 <b>ft</b> Reasonable diagram, 25, 13, 62 64, 19, 146 $n^2$ oe	1 1 1 L1 L1 R2 1 1 2 1ft 4 3	Each line ruled and long enough to enclose required region.  If <b>L0</b> , <b>SC1</b> if freehand but otherwise accurate and enclose region <b>SC1</b> if one boundary error – see diagrams  B1 B1  ft 5 × their x + 10 × their y  B1 B1 B1 B1 diagram may be freehand  B1 B1 B1  B1